

A FUNCTIONAL CALCULUS FOR QUOTIENT BOUNDED OPERATORS

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Abstract. If (X, \mathcal{P}) is a sequentially locally convex space, then a quotient bounded operator $T \in Q_{\mathcal{P}}(X)$ is regular (in the sense of Waelbroeck) if and only if it is a bounded element (in the sense of Allan) of algebra $Q_{\mathcal{P}}(X)$. The classic functional calculus for bounded operators on Banach space is generalized for bounded elements of algebra $Q_{\mathcal{P}}(X)$.

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