

# MULTI-CLASS DECISION PROCEDURES FOR THE INSPECTION OPERATION

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**Abstract.** Increasing the amount of inspection activities and inspecting a large fraction of the items are two approaches that are used to improve products' quality. In this paper, as in a precedent article by Jaraiedi, et al.[5], 100% inspection in combination with multiple-criteria decision (MCD) response is considered. Three different inspection procedures for the multi-stage inspection are presented. Performance of these three procedures are derived and the Average Outgoing Quality (AOQ), Average False Rejected (AFR), and Overall Average Fraction Inspected (SAFI) for all procedures are compared. Two examples are discussed in depth to illustrate numerical comparisons of these procedures.

**Keywords:** Quality, Multi-Criteria Inspection, AOQ, AFR, SAFI

## 1. Introduction

Quality improvement is regarded as one of the key points affecting both the consumers' purchasing decisions and a firm's competitive position. Every process in a production system eventually influences the product's quality and an inspection function is a key operation in any production process. Due to reduction in the costs of inspection systems and the increasing requirements of the marketplace, the use of 100% inspection at one or more stages of a manufacturing process is now economically viable in many instances. In many manufacturing processes, 100% inspection is also becoming increasingly important to the detection of moderate shifts in the performance of a process. An example of such a process is the manufacture of integrated circuits, as remarked in Pesotchinsky [8]. Inspection may be done on a sample taken from a lot or on the entire lot. Sampling schemes are established to provide the manufacturer and the customer an acceptable quality level. However, some researchers have made a strong argument against the use of sampling inspection. A policy of zero or 100% inspection was recommended, when the process quality remains at a stable level, by Deming [3]. Ott [7] gave an exam-

**Table 1: Multi-Class Decision Outcome Matrix**

DECISIONS	PRODUCTS CONFORMING	PRODUCTS NONCONFORMING
ACCEPT SURE	$P(\text{NO ERROR}) = 1 - \alpha_1 - \alpha_2 - \alpha_3$	$P(\text{accept sure}) = \beta_1$
ACCEPT NOT SURE	$P(\text{accept not sure}) = \alpha_3$	$P(\text{accept not sure}) = \beta_2$
REJECT NOT SURE	$P(\text{reject not sure}) = \alpha_2$	$P(\text{reject not sure}) = \beta_3$
REJECT SURE	$P(\text{reject sure}) = \alpha_1$	$P(\text{NO ERROR}) = 1 - \beta_1 - \beta_2 - \beta_3$

ple for multiple 100% inspection of a TV component. One method of improving the outgoing quality is to subject the lot to repeated or multiple inspections such that the few nonconforming items that might have escaped detection at the first inspection would be caught during the subsequent inspections. Unfortunately, this also tends to increase the cost of the inspection operation, but it can maintain the product quality at an acceptable level. Beany and Case [2] presented the AOQ for both single and double sampling inspection, with perfect inspection as well as error-prone inspection. Multi-class decision inspection is based on the realization that the inspectors usually have to make a decision on how to classify the product even if they are not sure whether or not it is conforming. They need other response categories to describe their unsure judgement and make further inspections on those items. In most cases, inspection may not result in rigid classification of items into rejected or accepted categories; it is more reasonable to interpret inspector behaviour by using a rating method, as described by Green and Swets [4]. Contrary to the binary decision method where the inspector is allowed only two responses (accept/reject), the rating method allows any number of responses. A three-class procedure for acceptance sampling plans by variables was presented by Newcombe and Allen[6]. Baker [1] used the rating method to analyse the performance of single inspection process; he devised four categories for the responses given by the inspectors. They are "Accept-Sure", "Accept-Not Sure", "Reject-Not Sure", and "Reject-Sure". Eight possible outcomes associated with this multi-class decision are shown in Table 1.

### 1.1. Measuring the Performance of Inspection

A perfect inspection model is one in which the inspector never makes a mistake. For instance, given an inspection activity consisting of 100 items in which five are nonconforming, not only does the inspector find the five, he/she also classifies the remaining 95 as conforming items. Given this assumption, the modelling problem reduces to that of deriving the best quality control policy. Average Outgoing Quality (AOQ), and Average Fraction Inspected (AFI) are two common performance measures of an inspection operation, and Average False Rejected (AFR) is a relatively new measure of an inspection operation. The AOQ and AFR depend upon several factors, prominent among which is the inspector's decision mechanism to accept or reject an item. AFI for single sampling inspection is basically the ratio of the number of items that are inspected to the number of items produced in the long run. While AOQ is a measure of the desirable outgoing quality level, AFR is employed to measure reworked or scrapped cost of the rejected items. AFI is employed to measure time/cost efficiency of the inspection method. The definition and features of these three measures are presented below. Average Outgoing Quality (AOQ) gives the expected fraction of nonconforming items in the accepted lots as a function of incoming quality level, and, thus, is the most common indicator of the outgoing quality level. It can be computed as:

$$AOQ = \frac{\text{Expected number of nonconforming items which were undetected}}{\text{Total number of items which were accepted}}$$

The AOQ measure has a numerical range of values from zero to unity. The Average False Rejected (AFR) is based upon the second measure of Wallack and Adams[10]. AFR gives the expected fraction of conforming items in the rejected lots as a function of wasted, reworked or scrapped cost. It may be defined as:

$$AFR = \frac{\text{Expected number of conforming items which were rejected}}{\text{Total number of items which were rejected}}$$

The AFR measure has the same numerical range as AOQ which is from one to unity. Average Fraction Inspected (AFI) gives the expected fraction of inspected items to the number of products in the lot as a function of incoming quality, and, thus, is the most common indicator of the inspection efficiency. That is:

$$AFI = \frac{\text{Expected number of items which were inspected}}{\text{Total number of items at the beginning}}$$

## 2. Multi-Class Inspection Procedures

Consider a multi-stage inspection scheme. In the first stage, the inspector classifies all items (100% inspection) into the four categories devised by Baker[1]. During the next stage, the items in one or more categories from the preceding stage are re-inspected and classified into these four categories again. Inspection is repeated until

**Table2: Multi-Class Decision in the Multi-stage Inspection Procedures**

	Accept Sure	Accept Not Sure	Reject Not Sure	Reject Sure
PROCEDURE 1	Reinspection	Reject		
PROCEDURE 2	Reinspection			Reject
PROCEDURE 3	Reinspection		Reject	

the desirable quality level is reached. In this paper, three inspection procedures are considered, as summarized in Table 2.

The expressions for AOQ, AFR, AFI, and SAFI of these three procedures in each stage are derived in the following sections. The reader is referred to Tsai [9] for a complete derivations of the expressions for AOQ, AFR, AFI, and SAFI for each procedure. Note that these expressions can be written in the form of a multiple of P and/or (1-P) and one or two constants that are functions of the inputs for  $\alpha$  and  $\beta$  at each stage. Here, P is the probability of an item being nonconforming. The difference between the three procedures is mainly based on the values of these constants.

### 2.1. Symbols and Notations

Symbols and notations used for various derivations are summarized below.

$\alpha_{i1}$  = probability that a conforming item is classified as "Reject-Sure" in stage i

$\alpha_{i2}$  = probability that a conforming item is classified as "Reject-Not Sure" in stage i

$\alpha_{i3}$  = probability that a conforming item is classified as "Accept-Not Sure" in stage i

$\beta_{i1}$  = probability that a nonconforming item is classified as "Accept-Sure" in stage i

$\beta_{i2}$  = probability that a nonconforming item is classified as "Accept-Not Sure" in stage i

$\beta_{i3}$  = probability that a nonconforming item is classified as "Reject-Not Sure" in stage i

$(AS_c)_i$  = expected number of conforming items classified as "Accept-Sure" in stage i

$(AN_c)_i$  = expected number of conforming items classified as "Accept-Not Sure" in stage i

$(RN_c)_i$  = expected number of conforming items classified as “Reject-Not Sure” in stage  $i$

$(RS_c)_i$  = expected number of conforming items classified as “Reject-Sure” in stage  $i$

$(AS_n)_i$  = expected number of nonconforming items classified as “Accept-Sure” in stage  $i$

$(AN_n)_i$  = expected number of nonconforming items classified as “Accept-Not Sure” in stage  $i$

$(RN_n)_i$  = expected number of nonconforming items classified as “Reject-Not Sure” in stage  $i$

$(RS_n)_i$  = expected number of nonconforming items classified as “Reject-Sure” in stage  $i$

## 2.2. Procedure 1

The items in the “Accept-Sure” category from preceding stage will be reinspected in the next stage, other items are regarded as rejected. The inspection process of Procedure 1 and the corresponding probabilities are shown in Figure 1. The probability of an item being nonconforming is  $P$ , while the probability of being conforming is  $1 - P$ . Expressions for the AOQ, AFR, AFI, and SAFI in stage  $k$  are derived as follows. Expected number of conforming items classified into “Accept-Sure”,

$$(AS_c)_k = N(1 - P) \prod_{i=1}^k (1 - \alpha_{i1} - \alpha_{i2} - \alpha_{i3})$$

Expected number of conforming items classified into “Accept-Not Sure”,

$$(AN_c)_k = N(1 - P)\alpha_{k3} \prod_{i=1}^{k-1} (1 - \alpha_{i1} - \alpha_{i2} - \alpha_{i3})$$

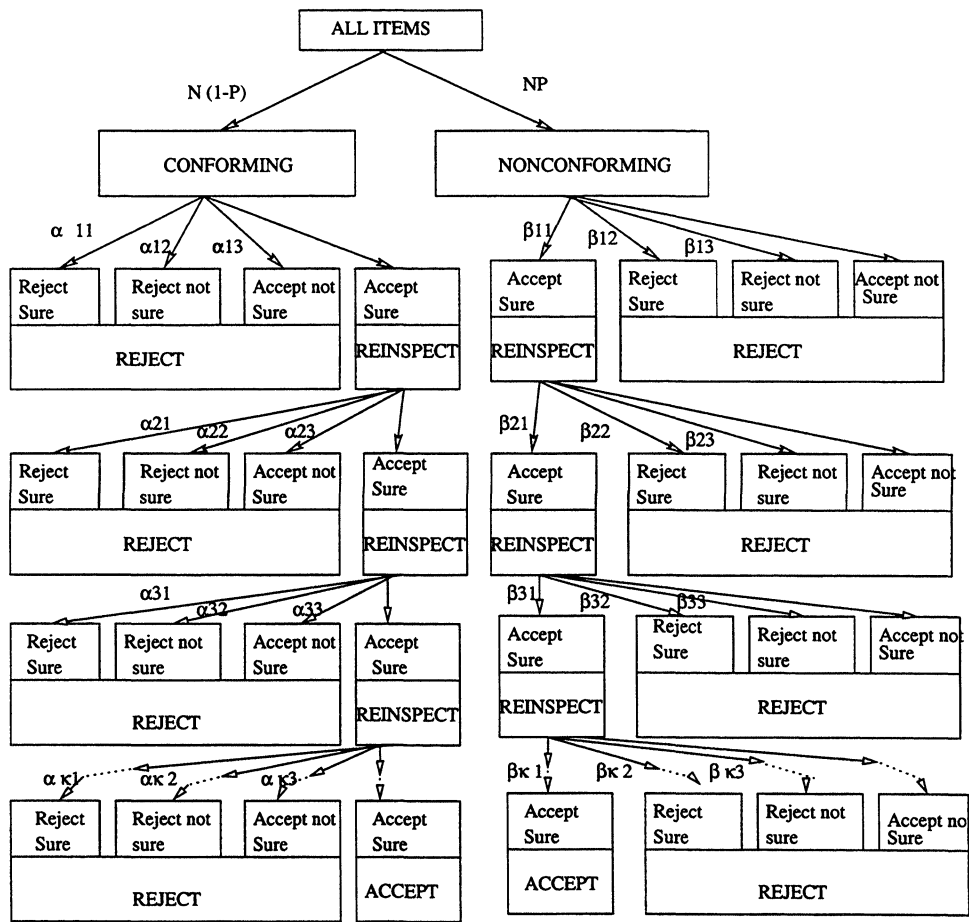
Expected number of conforming items classified into “Reject-Not Sure”,

$$(RN_c)_k = N(1 - P)\alpha_{k2} \prod_{i=1}^{k-1} (1 - \alpha_{i1} - \alpha_{i2} - \alpha_{i3})$$

Expected number of conforming items classified into “Reject-Sure”,

$$(RS_c)_k = N(1 - P)\alpha_{k1} \prod_{i=1}^{k-1} (1 - \alpha_{i1} - \alpha_{i2} - \alpha_{i3})$$

Figure 1: Inspection Procedure 1



Expected number of nonconforming items classified into “Accept-Sure”,

$$(AS_n)_k = NP \prod_{i=1}^k \beta_{i1}$$

Expected number of nonconforming items classified into “Accept-Not Sure”,

$$(AN_n)_k = NP\beta_{k2} \prod_{i=1}^{k-1} \beta_{i1}$$

Expected number of nonconforming items classified into “Reject-Not Sure”,

$$(RN_n)_k = NP\beta_{k3} \prod_{i=1}^{k-1} \beta_{i1}$$

Expected number of nonconforming items classified into “Reject-Sure”,

$$(RS_n)_k = NP(1 - \beta_{k1} - \beta_{k2} - \beta_{k3}) \prod_{i=1}^{k-1} \beta_{i1}$$

The expression for SAFI is:

$$\begin{aligned} (SAFI)_k &= (AFI)_1 + (AFI)_2 + (AFI)_3 \\ &\quad + \dots + (AFI)_k \\ &= 1 + (1 - P) \sum_{j=1}^{k-1} \prod_{i=1}^j (1 - \alpha_{i1} - \alpha_{i2} - \alpha_{i3}) \\ &\quad + P \sum_{j=1}^{k-1} \prod_{i=1}^j \beta_{i1} \end{aligned}$$

Expressions for AOQ, AFR, and AFI are as follows.

$$\begin{aligned} (AOQ)_k &= \frac{(AS_n)_k}{(AS_c)_k + (AS_n)_k} \\ &= \frac{P \prod_{i=1}^k \beta_{i1}}{(1 - P) \prod_{i=1}^k (1 - \alpha_{i1} - \alpha_{i2} - \alpha_{i3}) + P \prod_{i=1}^k \beta_{i1}} \\ &= \frac{1}{\frac{1-P}{P} \left[ \frac{\prod_{i=1}^k (1 - \alpha_{i1} - \alpha_{i2} - \alpha_{i3})}{\prod_{i=1}^k \beta_{i1}} \right] + 1} \\ &= \frac{1}{\frac{1-P}{P} * (A\ Constant) + 1} \end{aligned}$$

$$(AFR)_k = \frac{1}{\frac{P}{1-P}(AConstant) + 1}$$

where the constant in this formula is

$$\begin{aligned} & ((1 - \beta_{11}) + \sum_{j=2}^k \prod_{i=1}^{j-1} \beta_{i1} (1 - \beta_{j1})) / [(\alpha_{11} + \alpha_{12} + \alpha_{13}) \\ & + \sum_{j=2}^k \prod_{i=1}^{j-1} (1 - \alpha_{i1} - \alpha_{i2} - \alpha_{i3})(\alpha_{j1} + \alpha_{j2} + \alpha_{j3}) \end{aligned}$$

$$\begin{aligned} (AFI)_k &= \frac{(AS_c)_{k-1} + (AS_n)_{k-1}}{N} \\ &= (1 - P) \prod_{i=1}^{k-1} (1 - \alpha_{i1} - \alpha_{i2} - \alpha_{i3}) + P \prod_{i=1}^{k-1} \beta_{i1} \\ &= (1 - P) \star (Constant 1) + P \star (Constant 2) \end{aligned}$$

### 2.3. Procedure 2

The items in the "Reject-Sure" category are considered rejected, other items will be reinspected in the next stage. The inspection process of Procedure 2 is shown in Figure 2.

AOQ, AFR, AFI, and SAFI expressions in stage k are as follows.

$$(AS_c)_k = N(1 - P)(1 - \alpha_{k1} - \alpha_{k2} - \alpha_{k3}) \prod_{i=1}^{k-1} (1 - \alpha_{i1})$$

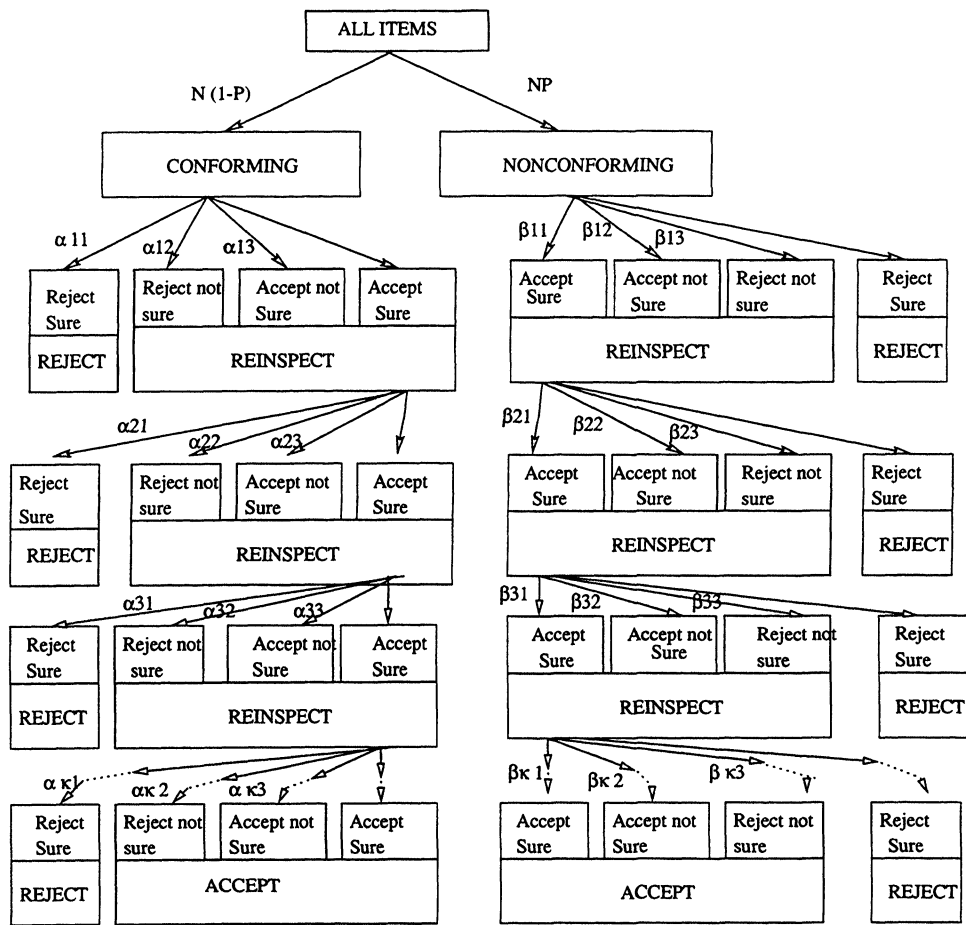
$$(AN_c)_k = N(1 - P)\alpha_{k3} \prod_{i=1}^{k-1} (1 - \alpha_{i1})$$

$$(RN_c)_k = N(1 - P)\alpha_{k2} \prod_{i=1}^{k-1} (1 - \alpha_{i1})$$

$$(RS_c)_k = N(1 - P)\alpha_{k1} \prod_{i=1}^{k-1} (1 - \alpha_{i1})$$



Figure 2: Inspection Procedure 2



$$(AS_n)_k = NP\beta_{k1} \prod_{i=1}^{k-1} (\beta_{i1} + \beta_{i2} + \beta_{i3})$$

$$(AN_n)_k = NP\beta_{k2} \prod_{i=1}^{k-1} (\beta_{i1} + \beta_{i2} + \beta_{i3})$$

$$(RN_n)_k = NP\beta_{k3} \prod_{i=1}^{k-1} (\beta_{i1} + \beta_{i2} + \beta_{i3})$$

$$(RS_n)_k = NP(1 - \beta_{k1} - \beta_{k2} - \beta_{k3}) \prod_{i=1}^{k-1} (\beta_{i1} + \beta_{i2} + \beta_{i3})$$

$$\begin{aligned} (AOQ)_k &= \frac{(AS_n)_k + (AN_n)_k + (RN_n)_k}{(AS_c)_k + (AN_c)_k + (RN_c)_k + (AS_n)_k + (AN_n)_k + (RN_n)_k} \\ &= \frac{P \prod_{i=1}^k (\beta_{i1} + \beta_{i2} + \beta_{i3})}{(1 - P) \prod_{i=1}^k (1 - \alpha_{i1}) + P \prod_{i=1}^k (\beta_{i1} + \beta_{i2} + \beta_{i3})} \\ &= \frac{1}{\frac{1-P}{P} [\prod_{i=1}^k (1 - \alpha_{i1})] / [\prod_{i=1}^k (\beta_{i1} + \beta_{i2} + \beta_{i3})] + 1} \\ &= \frac{1}{\frac{1-P}{P} \star (A\text{Constant}) + 1} \end{aligned}$$

$$(AFR)_k = \frac{1}{\frac{P}{1-P} \star (A\text{Constant}) + 1}$$

where the constant in this formula is

$$\begin{aligned} (1 - \beta_{11} - \beta_{12} - \beta_{13}) + \sum_{j=2}^k \prod_{i=1}^{j-1} (\beta_{i1} + \beta_{i2} + \beta_{i3}) + (1 - \beta_{j1} - \beta_{j2} - \beta_{j3}) / \\ [\alpha_{11} + \sum_{j=2}^k \prod_{i=1}^{j-1} (1 - \alpha_{i1}) \alpha_{j1}] \end{aligned}$$

$$\begin{aligned} (AFI)_k &= \frac{(AS_c)_{k-1} + (AN_c)_{k-1} + (RN_c)_{k-1} + (AS_n)_{k-1} + (AN_n)_{k-1} + (RN_n)_{k-1}}{N} \\ &= (1 - P) \prod_{i=1}^{k-1} (1 - \alpha_{i1}) + P \prod_{i=1}^{k-1} (\beta_{i1} + \beta_{i2} + \beta_{i3}) \\ &= (1 - P) \star (Constant1) + P \star (Constant2) \end{aligned}$$

$$\begin{aligned}
(SAFI)_k &= (AFI)_1 + (AFI)_2 + (AFI)_3 + \dots + (AFI)_k \\
&= 1 + [(1 - P)(1 - \alpha_{11}) + P(\beta_{11} + \beta_{12} + \beta_{13})] \\
&\quad + \dots + [(1 - P) \prod_{i=1}^{k-1} (1 - \alpha_{i1}) + P \prod_{i=1}^{k-1} (\beta_{i1} + \beta_{i2} + \beta_{i3})] \\
&= 1 + (1 - P) \sum_{j=1}^{k-1} \prod_{i=1}^j (1 - \alpha_{i1}) + P \sum_{j=1}^{k-1} \prod_{i=1}^j (\beta_{i1} + \beta_{i2} + \beta_{i3}) \\
&= 1 + (1 - P) \star (Constant1) + P \star (Constant2)
\end{aligned}$$

#### 2.4. Procedure 3

The items in the "Accept-Sure", and the "Accept-Not Sure" categories from preceding stage will be reinspected in the next stage, other items are considered rejected. If is equal to 1+2, and is equal to 1+ 2, then this procedure will be the same as the traditional binary decision method as previously discussed. The inspection process of Procedure 3 is shown in Figure 3.

AOQ, AFR, AFI, and SAFI expressions in stage k are given below.

$$(AS_c)_k = N(1 - P)(1 - \alpha_{k1} - \alpha_{k2} - \alpha_{k3}) \prod_{i=1}^{k-1} (1 - \alpha_{i1} - \alpha_{i2})$$

$$(AN_c)_k = N(1 - P)\alpha_{k3} \prod_{i=1}^{k-1} (1 - \alpha_{i1} - \alpha_{i2})$$

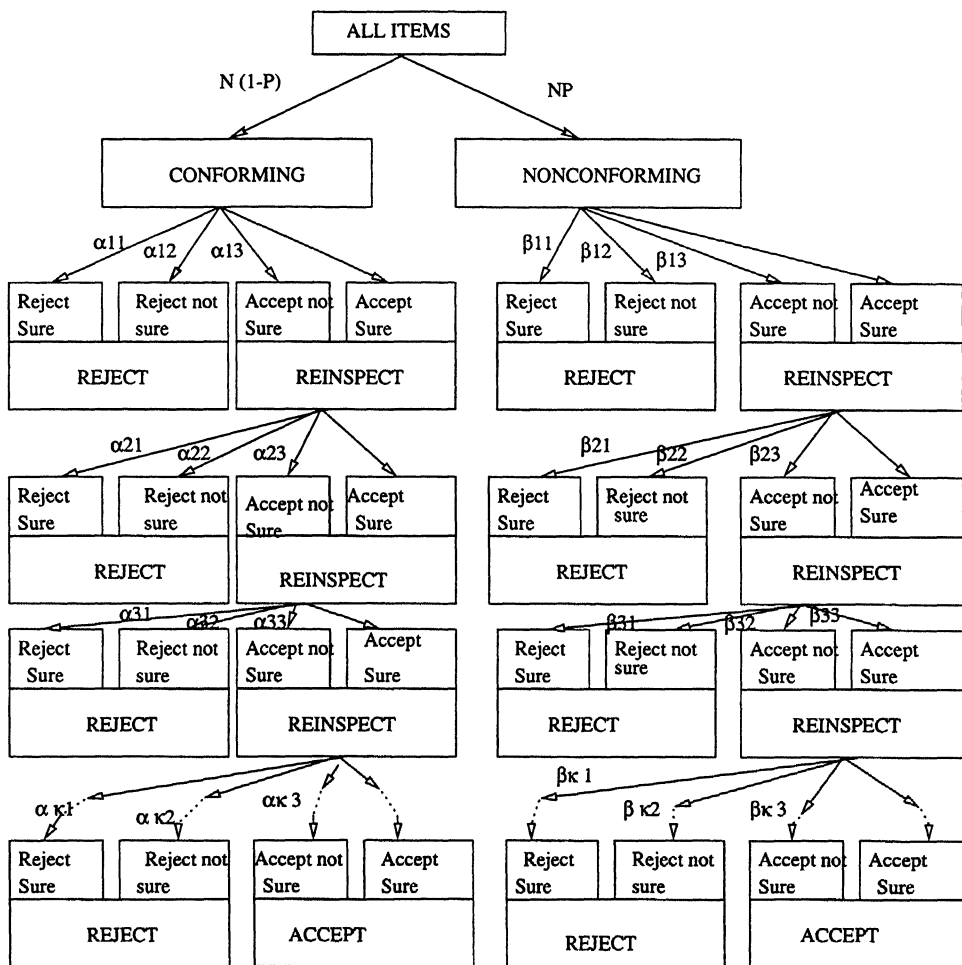
$$(RN_c)_k = N(1 - P)\alpha_{k2} \prod_{i=1}^{k-1} (1 - \alpha_{i1} - \alpha_{i2})$$

$$(RS_c)_k = N(1 - P)\alpha_{k1} \prod_{i=1}^{k-1} (1 - \alpha_{i1} - \alpha_{i2})$$

$$(AS_n)_k = NP\beta_{k1} \prod_{i=1}^{k-1} (\beta_{i1} + \beta_{i2})$$

$$(AN_n)_k = NP\beta_{k2} \prod_{i=1}^{k-1} (\beta_{i1} + \beta_{i2})$$

Figure 3: Inspection Procedure 3



$$(RN_n)_k = NP\beta_{k3} \prod_{i=1}^{k-1} (\beta_{i1} + \beta_{i2})$$

$$(RS_n)_k = NP(1 - \beta_{k1} - \beta_{k2} - \beta_{k3}) \prod_{i=1}^{k-1} (\beta_{i1} + \beta_{i2})$$

$$\begin{aligned} (AOQ)_k &= \frac{(AS_n)_k + (AN_n)_k}{(AS_c)_k + (AN_c)_k + (AS_n)_k + (AN_n)_k} \\ &= \frac{P \prod_{i=1}^k (\beta_{i1} + \beta_{i2})}{(1-P) \prod_{i=1}^k (1 - \alpha_{i1} - \alpha_{i2}) + P \prod_{i=1}^k (\beta_{i1} + \beta_{i2})} \\ &= \frac{1}{\frac{1-P}{P} [\prod_{i=1}^k (1 - \alpha_{i1} - \alpha_{i2})] / [\prod_{i=1}^k (\beta_{i1} + \beta_{i2})] + 1} \\ &= \frac{1}{\frac{1-P}{P} (A \text{ Constant}) + 1} \end{aligned}$$

$$(AFR)_k = \frac{1}{\frac{P}{1-P} (A \text{ Constant}) + 1}$$

where the constant in the formula is

$$\begin{aligned} (1 - \beta_{11} - \beta_{12}) + \sum_{j=2}^k \prod_{i=1}^{j-1} (\beta_{i1} + \beta_{i2}) (1 - \beta_{j1} - \beta_{j2}) / [(\alpha_{11} + \alpha_{12}) \\ + \sum_{j=2}^k \prod_{i=1}^{j-1} (1 - \alpha_{i1} - \alpha_{i2}) (\alpha_{j1} + \alpha_{j2}) \end{aligned}$$

$$\begin{aligned} (AFI)_k &= \frac{(AS_c)_{k-1} + (AN_c)_{k-1} + (AS_n)_{k-1} + (AN_n)_{k-1}}{N} \\ &= (1-P) \prod_{i=1}^{k-1} (1 - \alpha_{i1} - \alpha_{i2}) + P \prod_{i=1}^{k-1} (\beta_{i1} + \beta_{i2}) \\ &= (1-P) \star (\text{Constant1}) + P \star (\text{Constant2}) \end{aligned}$$

$$\begin{aligned} (SAFI)_k &= (AFI)_1 + (AFI)_2 + (AFI)_3 + \dots + (AFI)_k \\ &= 1 + (1-P) \sum_{j=1}^{k-1} \prod_{i=1}^j (1 - \alpha_{i1} - \alpha_{i2}) \end{aligned}$$

$$\begin{aligned}
& + P \sum_{j=1}^{k-1} \prod_{i=1}^j (\beta_{i1} + \beta_{i2}) \\
& = 1 + (1 - P) * (\text{Constant1}) + P * (\text{Constant2})
\end{aligned}$$

### 3. Examples

The following examples are presented to illustrate the use of the three inspection procedures described in this paper. Numerical values of AOQ, AFR, AFI, and SAFI were computed for each of these three procedures using a computer program that can be found in Tsai[9].

#### Example 1

Assume that the incoming fraction nonconforming is a constant and a three-stage inspection is needed. The probability of various responses are assumed to be the same at each stage. For  $P = 0.1$ ,  $k = 3$ , let:

$$\alpha_{i1} = 3\%, \alpha_{i2} = 6\%, \alpha_{i3} = 9\%, \beta_{i1} = 4\%, \beta_{i2} = 7\%, \beta_{i3} = 10\%.$$

The AOQ, AFR, and SAFI at the end of the third stage are shown in the Table 3.

**Example 2** This example demonstrates the effect of change in the incoming fraction nonconforming on the three indicators. Using the same assumptions as in Example 1, let  $k = 3$ , and  $\alpha_{i1} = 3\%$ ,  $\alpha_{i2} = 6\%$ ,  $\alpha_{i3} = 9\%$ ,  $\beta_{i1} = 4\%$ ,  $\beta_{i2} = 7\%$ ,  $\beta_{i3} = 10\%$ .  $P$  is changed from 5% to 25% in increments of 5%, and the results of calculations for different incoming fractions nonconforming are shown in Table 4. It can be seen that the AOQ increases when the incoming fraction nonconforming is increased. The sharpest increase rate of AOQ is in Procedure 3 and the order of the AOQ in this example is:

$$Proc.1 < Proc.3 < Proc.2$$

The AFR's decrease with an increase in the incoming fraction nonconforming. All three procedures have almost the same decreasing rate of AFR. When  $P$  is decreased from 25% to 5%, the AFR for the three procedures increases by 32%, 42%, and 40%. The order of the AFR in this example is:

$$Proc.2 < Proc.3 < Proc.1$$

When the incoming fraction nonconforming is increased, the SAFI of Procedures 1, and 2 and 3 are decreased. The effect of the increase in the incoming fraction nonconforming is significant for Procedures 1, and 2. The order of the SAFI in this example is:

$$Proc.1 < Proc.3 < Proc.2$$

**Table 3: AOQ, AFR and SAFI of Example 1**

AOQ (%)			
STAGE	PROC. 1	PROC. 2	PROC. 3
1	.5391	2.3490	1.3253
2	.0264	.5181	.1621
3	.0013	.1126	.0196
AFR (%)			
1	62.79	25.47	47.64
2	74.70	35.77	61.02
3	80.15	44.24	68.95
SAFI			
1	1	1	1
2	1.74	1.89	1.83
3	2.35	2.75	2.57

**Table4: AOQ, AFR, and SAFI of Example 1**

AOQ (%)			
P	Proc. 1	Proc. 2	Proc. 3
5 %	.006	.534	.009295
10 %	.0013	.1126	.0196
15 %	.0020	.1718	.03116
20 %	.0029	.2530	.044137
25 %	.0039	.3371	.58841
AFR (%)			
5 %	89.50	62.61	82.42
10 %	80.15	44.24	68.95
15 %	71.77	33.31	58.30
20 %	64.22	26.07	49.67
25 %	57.38	20.19	42.53
SAFI			
5 %	2.42	2.83	2.63
10 %	2.35	2.75	2.55
15 %	2.27	2.66	2.47
20 %	2.20	2.58	2.39
25 %	2.13	2.50	2.32



#### 4. CONCLUSIONS AND FUTURE DIRECTIONS OF RESEARCH

The main purpose of multi-stage inspection is to achieve a higher outgoing quality in the long-run. Obviously, the cost of additional inspection must be carefully balanced against the benefit of improved outgoing quality. Given the assumptions made in this research, it is possible to evaluate the improvement in AOQ after each stage. This gain in quality, then, must be compared to the cost of hiring an additional inspector for the extra stage. In general, AOQ must be balanced against AFR and SAFI which indicate the cost of acceptable items falsely rejected and the total inspection effort, respectively. This comparison must be made for all the six procedures addressed in this research. For instance, in Example 2 for  $P = 5\%$  after 3 stages of inspection Procedures 2 and 3 may be compared to select the one that is more cost effective. Procedure 3 achieves a much lower AOQ compared to Procedure 2. However, this improvement is accompanied with 1.31 times more in the cost of good items rejected, but the amount of inspection is roughly the same. If the 0.009% outgoing quality achieved by Procedure 3 does justify the expenditure of additional resources, then, this procedure will be chosen over Procedure 2. The future directions of the research should include allowing more categories of inspection response, and a mix of reinspection policies at selected stages as described in our earlier paper. Allowing five or more categories of inspector response for the three new procedures presented in this paper will make it possible to devise a variety of reinspection policies that may result in improved overall quality and lower costs in the long run. A mix of reinspection policies at various stages should be considered rather than assuming constant reinspection policy at every stage. This would require development of new expressions for AOQ, AFR, and SAFI.

#### References

1. E. M. Baker. Signal Detection Theory Analysis of Quality Control Inspector Performance. *Journal of Quality Technology*, 7:62-71, 1975.
2. I. Beainy and K. E. Case. A Wide Variety of AOQ and ATI Performance Measures with and without Inspection Error. *Journal of Quality Technology*, 13:1-9, 1981.
3. E. W. Deming. *Quality, Productivity, and Competitive Position*. MIT Press, Cambridge, MA., 1982.
4. D. M. Green and J. A. Swets. *Signal Detection Theory and Psychophysics*. John Wiley and Sons, New York, 1964.
5. M. Jaraiedi, R. S. Segall and Y. Tsai. Multi-Criteria Decision Procedures for the Inspection Operation. *Journal of Design and Manufacturing*, 5: 25-44, 1995.
6. P. A. Newcombe and O. B. Allen. A Three-Class Procedure for Acceptance Sampling by Variables. *Technometrics*, 30: 415-421, 1988.
7. E. R. Ott. *Process Quality Control*. McGraw-Hill Book Company, New York, 1975.
8. L. Pesotchinsky. Plans for Very Low Fraction Nonconforming. *Journal of Quality Technology*, 19:191-196, 1987.
9. Y. Tsai. Multi-Criteria Decision Procedures for the Inspection Operation. M.S. Thesis, Department of Industrial Engineering, West Virginia University, Morgantown, WV, 1993.
10. P. M. Wallack and S. K. Adams. A Comparison of Inspector Performance Measures. *AIIE Transactions*, 2:97-105, 1970.

## Special Issue on Decision Support for Intermodal Transport

### Call for Papers

Intermodal transport refers to the movement of goods in a single loading unit which uses successive various modes of transport (road, rail, water) without handling the goods during mode transfers. Intermodal transport has become an important policy issue, mainly because it is considered to be one of the means to lower the congestion caused by single-mode road transport and to be more environmentally friendly than the single-mode road transport. Both considerations have been followed by an increase in attention toward intermodal freight transportation research.

Various intermodal freight transport decision problems are in demand of mathematical models of supporting them. As the intermodal transport system is more complex than a single-mode system, this fact offers interesting and challenging opportunities to modelers in applied mathematics. This special issue aims to fill in some gaps in the research agenda of decision-making in intermodal transport.

The mathematical models may be of the optimization type or of the evaluation type to gain an insight in intermodal operations. The mathematical models aim to support decisions on the strategic, tactical, and operational levels. The decision-makers belong to the various players in the intermodal transport world, namely, drayage operators, terminal operators, network operators, or intermodal operators.

Topics of relevance to this type of decision-making both in time horizon as in terms of operators are:

- Intermodal terminal design
- Infrastructure network configuration
- Location of terminals
- Cooperation between drayage companies
- Allocation of shippers/receivers to a terminal
- Pricing strategies
- Capacity levels of equipment and labour
- Operational routines and lay-out structure
- Redistribution of load units, railcars, barges, and so forth
- Scheduling of trips or jobs
- Allocation of capacity to jobs
- Loading orders
- Selection of routing and service

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