

## ASYMPTOTIC STABILITY OF A 9-POINT MULTIGRID ALGORITHM FOR CONVECTION-DIFFUSION EQUATIONS\*

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**Abstract.** We consider the solution of the convection-diffusion equation in two dimensions by a compact high-order 9-point discretization formula combined with multigrid algorithm. We prove the  $\epsilon$ -asymptotic stability of the coarse-grid operators. Two strategies are examined. A method to compute the asymptotic convergence is described and applied to the multigrid algorithm.

**Key words.** multigrid method, high-order discretization, asymptotic stability, convection-diffusion equation.

**AMS subject classifications.** 65F10, 65N06, 65N22, 65N55, 76D07.

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