

## INVERSE SOURCE PROBLEM IN A 3D BALL FROM BEST MEROMORPHIC APPROXIMATION ON 2D SLICES\*

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*Dedicated to Ed Saff on the occasion of his 60th birthday*

**Abstract.** We show that the inverse monopolar or dipolar source problem in a 3D ball from overdetermined Dirichlet-Neumann data on the boundary sphere reduces to a family of 2D inverse branchpoint problems in cross sections of the sphere, at least when there are finitely many sources. We adapt from [L. Baratchart et al., *Recovery of pointwise sources or small inclusions in 2D domains and rational approximation*, Inverse Problems, 21 (2005), pp. 51–74] an approach to these 2D inverse problem which is based on meromorphic approximation, and we present numerical results.

**Key words.** inverse source problems, potential theory, meromorphic approximation

**AMS subject classifications.** 31A25, 30E10, 30E25, 35J05

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