

A NECESSARY AND SUFFICIENT EIGENVECTOR CONDITION FOR A CONNECTED GRAPH TO BE BIPARTITE*

SEBASTIAN M. CIOABĂ †

Abstract. We give a necessary and sufficient condition for a graph to be bipartite in terms of an eigenvector corresponding to the largest eigenvalue of the adjacency matrix of the graph.

Key words. Graph, Bipartite, Principal eigenvector, Independent set.

AMS subject classifications. 05C50, 15A18.

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[†]Department of Mathematical Sciences, University of Delaware, Newark, DE 19716-2553, USA (cioaba@math.udel.edu). Research supported by a startup grant from the Department of Mathematical Sciences of the University of Delaware.