

A NEW UPPER BOUND FOR THE EIGENVALUES OF THE CONTINUOUS ALGEBRAIC RICCATI EQUATION*

JIANZHOU LIU[†], JUAN ZHANG[‡], AND YU LIU[§]

Abstract. By using majorization inequalities, we propose a new upper bound for summations of eigenvalues (including the trace) of the solution of the continuous algebraic Riccati equation. The bound extends some of the previous results under certain conditions. Finally, we give a numerical example to illustrate the effectiveness of our results.

Key words. Eigenvalue, Majorization inequality, Trace inequality, Algebraic Riccati equation.

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[†]Department of Mathematical Science and Information Technology, Hanshan Normal University, Chaozhou, Guangdong 521041, China, and Department of Mathematics and Computational Science, Xiangtan University, Xiangtan, Hunan 411105, China (liujz@xtu.edu.cn, corresponding author). Supported in part by Natural Science Foundation of China (10971176).

 $^{^{\}ddagger}$ Department of Mathematics and Computational Science, Xiangtan University, Xiangtan, Hunan 411105, China.

 $^{^{\$}}$ Department of Mathematical Science and Information Technology, Hanshan Normal University, Chaozhou, Guangdong 521041, China.