

REPRESENTATIONS FOR THE DRAZIN INVERSE OF BOUNDED OPERATORS ON BANACH SPACE*

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Abstract. In this paper a representation is given for the Drazin inverse of a 2×2 operator matrix, extending to Banach spaces results of Hartwig, Li and Wei [SIAM J. Matrix Anal. Appl., 27 (2006) pp. 757–771]. Also, formulae are derived for the Drazin inverse of an operator matrix M under some new conditions.

Key words. Operator matrix, Drazin inverse, D-invertibility, GD-invertibility.

AMS subject classifications. 47A52, 47A62, 15A24.

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