

## EXPLICIT SOLUTIONS OF REGULAR LINEAR DISCRETE-TIME DESCRIPTOR SYSTEMS WITH CONSTANT COEFFICIENTS\*

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**Abstract.** Explicit solution formulas are presented for systems of the form  $Ex^{k+1} = Ax^k + f^k$ with  $k \in \mathbb{K}$ , where  $\mathbb{K} \subset \mathbb{Z}$  is a discrete interval and the pencil  $\lambda E - A$  is regular. Different results are obtained when one starts with an initial condition at the point k = 0 and calculates into the future (i.e.,  $Ex^{k+1} = Ax^k + f^k$  with  $k \in \mathbb{N}$ ) and when one wants to get a complete solution (i.e.,  $Ex^{k+1} = Ax^k + f^k$  with  $k \in \mathbb{Z}$ ).

Key words. Descriptor system, Strangeness index, Linear discrete descriptor system, Explicit solution, Backward Leslie model.

AMS subject classifications. 39A05, 15A06.

<sup>\*</sup> Received by the editors January 23, 2009. Accepted for publication July 3, 2009. Handling Editor: Peter Lancaster. This research is supported by the DFG Research Center MATHEON in Berlin.

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