# FURTHER RESULTS ON THE CRAIG-SAKAMOTO EQUATION* 

JOHN MAROULAS ${ }^{\dagger}$


#### Abstract

In this paper, necessary and sufficient conditions are stated for the Craig-Sakamoto equation $\operatorname{det}(I-s A-t B)=\operatorname{det}(I-s A) \operatorname{det}(I-t B)$ to hold for all scalars $s, t \in \mathbb{C}$. Moreover, spectral properties for matrices $A$ and $B$ that satisfy this equation are investigated.


Key words. Determinant, Characteristic polynomial, Craig-Sakamoto equation, Bilinear form.

AMS subject classifications. 15A15, 15A18, 15A63.

* Received by the editors September 3, 2007. Accepted for publication September 11, 2008. Handling Editor: Michael Tsatsomeros.
${ }^{\dagger}$ Department of Mathematics, National Technical University, Zografou Campus, Athens 15780, Greece (maroulas@math.ntua.gr). Research supported by a grant of the EPEAEK, project Pythagoras II. The project is co-funded by the European Social Fund (75\%) and Greek National Resources (25\%).

