

## FURTHER RESULTS ON THE CRAIG-SAKAMOTO EQUATION\*

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**Abstract.** In this paper, necessary and sufficient conditions are stated for the Craig-Sakamoto equation det(I-sA-tB)=det(I-sA)det(I-tB) to hold for all scalars  $s,t\in\mathbb{C}$ . Moreover, spectral properties for matrices A and B that satisfy this equation are investigated.

Key words. Determinant, Characteristic polynomial, Craig-Sakamoto equation, Bilinear form.

AMS subject classifications. 15A15, 15A18, 15A63.

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