# Mathematics Subject Classification 2000 

## Mathematics Subject Classification 2000 (MSC2000)

This is a completely revised version of the MSC, prepared collaboratively in the editorial offices of MR and Zentralblatt MATH. It replaces the 1991 MSC and is effective (in MR) with the January 2000 issue (2000a).

While in many areas in the MSC there are only very small changes, others have been expanded significantly, and in some areas there is an altogether new classification. The major changes are as follows: Section 04 has been eliminated; 03E will now be used for items previously classified in 04 . A new section, 37, has been created for Dynamical systems and ergodic theory; as a result Section 58F has been eliminated. Also in Section 58, 58 G has been completely revised and now appears as 58J. The new Section 74, Mechanics of deformable solids, is a completely revised version of Section 73, which has been eliminated. The areas covered by Sections 90 and 92 have been reorganized into Sections 90, 91 and 92. Sections 90B and 90C remain essentially unchanged. The new Section 91A replaces 90D and 91B replaces 90A. The other subsections of 91 replace the old subsections 92G, H, J and K. Sections 92B, C, D, and E remain essentially unchanged. MSC2000 contains a new section, 97, for Mathematics education. This will be used only as a secondary classification in MR. Other sections with significant additions or reorganization include $14,22,32,34,46,47,53$, and 65.

To help users of the MSC, conversion tables have been constructed and are available on the AMS web site, www.ams.org. These give, for each 1991 classification that does not appear in MSC2000, the classification(s) in MSC2000 that are most likely to be used for items that would previously have been classified using the old classification, and, for each new classification in MSC2000, the classification(s) in the 1991 MSC that are most likely to have been used earlier for items classified using the new classification.

## Instructions for using the Mathematics Subject Classification 2000

These instructions apply uniformly to all fields listed. The main purpose of the classification is to help readers find the items of present or potential interest to them as readily as possiblein MR, in Zbl, or anywhere else where this classification system
is used. A paper or book should be listed under the classification where it will receive the broadest attention from readers possibly interested in it-these include both people working in that area and people who are familiar with that area and apply its results and methods elsewhere (inside or outside mathematics). It will be extremely useful for both readers and classifiers to familiarize themselves with the entire classification system and thus to become aware of all the classifications of possible interest to them.

For every paper or book listed, MR chooses precisely one "primary" classification, which is simply the code for the section (MSC entry) in which the item will be located. This section should be the one that covers the principal contribution. When an item contains several principal contributions in different areas, the primary classification should cover the "most important" among them. A paper or book may receive one or several "secondary" classifications (or "cross-references") to cover any remaining principal contributions, ancillary results, motivation or origin of the problems discussed, intended or potential field of application, or other significant aspects worthy of notice.

The "primary" principal contribution is meant to be the one including the most important part of the work actually done in the item under consideration. For example, a paper whose main overall content is the solution of a problem in graph theory, which arose in computer science and whose solution is, say, at present only of interest to computer scientists, belongs primarily in 05 C with a cross-reference in 68; conversely, a paper whose overall content lies mainly in computer science should receive a primary classification in 68, even if it makes heavy use of graph theory and proves several new graph-theoretic results along the way.

There are two types of cross-references given after many classifications in the list. The first type is of the form " $\{$ For A, see $X\}$ "; if this appears in section Y, it means that for contributions described by A one should usually assign the classification X , not Y. The other type of cross-reference merely points out related classifications; it is of the form "[See also ...]", "[See mainly ...]", etc., and the classifications listed in the brackets may, but need not, be added to the classification of a paper, or they may be used in place of the classification where the cross-reference is given. The classifier will have to judge which classification is the most appropriate for the item at hand.

00A20
00A22
00A30
00A35
00A69

00A71
00A72
00A73
00A79 Physics (use more specific entries from Sections 70 through 86 when possible)

| 00A99 | Miscellaneous topics |
| :---: | :---: |
| 00Bxx | Conference proceedings and collections of papers |
| 00B05 | Collections of abstracts of lectures |
| 00B10 | Collections of articles of general interest |
| 00B15 | Collections of articles of miscellaneous specific content |
| 00B20 | Proceedings of conferences of general interest |
| 00B25 | Proceedings of conferences of miscellaneous specific interest |
| 00B30 | Festschriften |
| 00B50 | Volumes of selected translations |
| 00B55 | Miscellaneous volumes of translations |
| 00B60 | Collections of reprinted articles [See also 01A75] |
| 01-XX | HISTORY AND BIOGRAPHY [See also the classification number -03 in the other sections] |
| 01-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 01-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 01-02 | Research exposition (monographs, survey articles) |
| 01-06 | Proceedings, conferences, collections, etc. |
| 01-08 | Computational methods |
| 01Axx | History of mathematics and mathematicians |
| 01 A 05 | General histories, source books |
| 01 A 07 | Ethnomathematics, general |
| 01 A 10 | Paleolithic, Neolithic |
| 01A12 | Indigenous cultures of the Americas |
| 01 A 13 | Other indigenous cultures (non-European) |
| 01 A 15 | Indigenous European cultures (pre-Greek, etc.) |
| 01A16 | Egyptian |
| 01 A 17 | Babylonian |
| 01A20 | Greek, Roman |
| 01 A 25 | China |
| 01A27 | Japan |
| 01A29 | Southeast Asia |
| 01A30 | Islam (Medieval) |
| 01A32 | India |
| 01 A 35 | Medieval |
| 01A40 | 15th and 16th centuries, Renaissance |
| 01 A 45 | 17th century |
| 01 A 50 | 18th century |
| 01 A 55 | 19th century |
| 01A60 | 20th century |
| 01 A61 | Twenty-first century |
| 01 A65 | Contemporary |
| 01A67 | Future prospectives |
| 01 A 70 | Biographies, obituaries, personalia, bibliographies |
| 01A72 | Schools of mathematics |
| 01A73 | Universities |
| 01A74 | Other institutions and academies |
| 01A75 | Collected or selected works; reprintings or translations of classics [See also 00B60] |
| 01A80 | Sociology (and profession) of mathematics |
| 01A85 | Historiography |
| 01 A 90 | Bibliographic studies |
| 01A99 | Miscellaneous topics |

03-00

03-01

03-02
03-03

03-04

03-06
03A05

03Bxx
03B05
03B10
03B15
03B20

03B22

03B42
03B44
03B45

03B47

03B48
03B50
03B52

03B53

03B55
03B60
03B65

03B70
03B80
03B99
03Cxx
03C05

03C07

03 C 10

## 03-XX <br> MATHEMATICAL LOGIC AND FOUNDATIONS

03B25 Decidability of theories and sets of sentences [See also 11U05, 12L05, 20F10]
03B30 Foundations of classical theories (including reverse mathematics) [See also 03F35]
03B35 Mechanization of proofs and logical operations [See also 68T15]
03B40 Combinatory logic and lambda-calculus [See also 68N18]
Logic of knowledge and belief
General reference works (handbooks, dictionaries, bibliographies, etc.)
Instructional exposition (textbooks, tutorial papers, etc.)
Research exposition (monographs, survey articles)
Historical (must also be assigned at least one classification number from Section 01)
Explicit machine computation and programs (not the theory of computation or programming)
Proceedings, conferences, collections, etc.
Philosophical and critical \{For philosophy of mathematics, see also 00A30\}
General logic
Classical propositional logic
Classical first-order logic
Higher-order logic and type theory
Subsystems of classical logic (including intuitionistic logic)
Abstract deductive systems

Temporal logic
Modal logic \{For knowledge and belief see 03B42; for temporal logic see 03B44; for provability logic see also 03F45\}
Substructural logics (including relevance, entailment, linear logic, Lambek calculus, BCK
and BCI logics) \{For proof-theoretic aspects see 03F52\}
Probability and inductive logic [See also 60A05]
Many-valued logic
Fuzzy logic; logic of vagueness [See also 68T27, 68T37, 94D05]
Logics admitting inconsistency (paraconsistent logics, discussive logics, etc.)
Intermediate logics
Other nonclassical logic
Logic of natural languages [See also 68T50, 91F20]
Logic in computer science [See also 68-XX]
Other applications of logic
None of the above, but in this section
Model theory
Equational classes, universal algebra [See also 08Axx, 08Bxx, 18C05]
Basic properties of first-order languages and structures
Quantifier elimination, model completeness and related topics

| 03 C 13 | Finite structures [See also 68Q15, 68Q19] |
| :---: | :---: |
| 03 C 15 | Denumerable structures |
| 03C20 | Ultraproducts and related constructions |
| 03C25 | Model-theoretic forcing |
| 03C30 | Other model constructions |
| 03C35 | Categoricity and completeness of theories |
| 03C40 | Interpolation, preservation, definability |
| 03C45 | Classification theory, stability and related concepts |
| 03C50 | Models with special properties (saturated, rigid, etc.) |
| 03C52 | Properties of classes of models |
| 03C55 | Set-theoretic model theory |
| 03C57 | Effective and recursion-theoretic model theory [See also 03D45] |
| 03C60 | Model-theoretic algebra [See also 08C10, 12Lxx, 13L05] |
| 03C62 | Models of arithmetic and set theory [See also 03Hxx] |
| 03C64 | Model theory of ordered structures; o-minimality |
| 03C65 | Models of other mathematical theories |
| 03C68 | Other classical first-order model theory |
| 03 C 70 | Logic on admissible sets |
| 03 C 75 | Other infinitary logic |
| 03C80 | Logic with extra quantifiers and operators [See also 03B42, 03B44, 03B45, 03B48] |
| 03C85 | Second- and higher-order model theory |
| 03 C 90 | Nonclassical models (Boolean-valued, sheaf, etc.) |
| 03C95 | Abstract model theory |
| 03C98 | Applications of model theory [See also 03C60] |
| 03C99 | None of the above, but in this section |
| 03Dxx | Computability and recursion theory |
| 03D03 | Thue and Post systems, etc. |
| 03D05 | Automata and formal grammars in connection with logical questions [See also 68Q45, 68Q70, 68R15] |
| 03D10 | Turing machines and related notions [See also 68Q05] |
| 03D15 | Complexity of computation [See also 68Q15, 68Q17] |
| 03D20 | Recursive functions and relations, subrecursive hierarchies |
| 03D25 | Recursively (computably) enumerable sets and degrees |
| 03D28 | Other Turing degree structures |
| 03D30 | Other degrees and reducibilities |
| 03D35 | Undecidability and degrees of sets of sentences |
| 03D40 | Word problems, etc. [See also 06B25, 08A50, 20F10, 68R15] |
| 03D45 | Theory of numerations, effectively presented structures [See also 03C57; for intuitionistic and similar approaches see 03F55] |
| 03D50 | Recursive equivalence types of sets and structures, isols |
| 03D55 | Hierarchies |
| 03D60 | Computability and recursion theory on ordinals, admissible sets, etc. |
| 03D65 | Higher-type and set recursion theory |

03D70
03D75
03D80

03D99
03Exx
03E02
03E04
03 E 05
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03 E 17
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03E45
03E47
03E50
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03E65
03E70
03E72
03 E 75
03E99
03Fxx
03F03
03 F 05
03 F 07
03F10
03F15
03F20
03F25
03F30
03F35
03 F 40
03F45

03F50
03F52
03 F 55
03F60

03F65
03F99
03Gxx
03G05
03G10

Inductive definability
Abstract and axiomatic computability and recursion theory
Applications of computability and recursion theory
None of the above, but in this section
Set theory
Partition relations
Ordered sets and their cofinalities; pcf theory
Other combinatorial set theory
Ordinal and cardinal numbers
Descriptive set theory [See also 28A05, 54H05]
Cardinal characteristics of the continuum
Other classical set theory (including functions, relations, and set algebra)
Axiom of choice and related propositions
Axiomatics of classical set theory and its fragments
Consistency and independence results
Other aspects of forcing and Boolean-valued models
Inner models, including constructibility, ordinal definability, and core models
Other notions of set-theoretic definability
Continuum hypothesis and Martin's axiom
Large cardinals
Determinacy principles
Other hypotheses and axioms
Nonclassical and second-order set theories
Fuzzy set theory
Applications of set theory
None of the above, but in this section

## Proof theory and constructive mathematics

Proof theory, general
Cut-elimination and normal-form theorems
Structure of proofs
Functionals in proof theory
Recursive ordinals and ordinal notations
Complexity of proofs
Relative consistency and interpretations
First-order arithmetic and fragments
Second- and higher-order arithmetic and fragments [See also 03B30]
Gödel numberings in proof theory
Provability logics and related algebras (e.g., diagonalizable algebras) [See also 03B45, 03G25, 06E25]
Metamathematics of constructive systems
Linear logic and other substructural logics
[See also 03B47]
Intuitionistic mathematics
Constructive and recursive analysis
[See also 03B30, 03D45, 26E40, 46S30, 47S30]
Other constructive mathematics [See also 03D45]
None of the above, but in this section

## Algebraic logic

Boolean algebras [See also 06Exx]
Lattices and related structures [See also 06Bxx]

| 03G12 | Quantum logic [See also 06C15, 81P10] |
| :---: | :---: |
| 03G15 | Cylindric and polyadic algebras; relation algebras |
| 03G20 | Łukasiewicz and Post algebras [See also 06D25, 06D30] |
| 03G25 | Other algebras related to logic [See also 03F45, 06D20, 06E25, 06F35] |
| 03G30 | Categorical logic, topoi [See also 18B25, 18C05, 18C10] |
| 03G99 | None of the above, but in this section |
| 03Hxx | Nonstandard models [See also 03C62] |
| 03H05 | Nonstandard models in mathematics [See also 26E35, 28E05, 30G06, 46S20, 47S20, 54J05] |
| 03H10 | Other applications of nonstandard models (economics, physics, etc.) |
| 03H15 | Nonstandard models of arithmetic [See also 11U10, 12L15, 13L05] |
| 03H99 | None of the above, but in this section |
| 05-XX | COMBINATORICS $\{$ For finite fields, see 11Txx\} |
| 05-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 05-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 05-02 | Research exposition (monographs, survey articles) |
| 05-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 05-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 05-06 | Proceedings, conferences, collections, etc. |
| 05Axx | Enumerative combinatorics |
| 05A05 | Combinatorial choice problems (subsets, representatives, permutations) |
| 05A10 | Factorials, binomial coefficients, combinatorial functions [See also 11B65, 33Cxx] |
| 05A15 | Exact enumeration problems, generating functions [See also 33Cxx, 33Dxx] |
| 05A16 | Asymptotic enumeration |
| 05A17 | Partitions of integers [See also 11P81, 11P82, 11P83] |
| 05A18 | Partitions of sets |
| 05A19 | Combinatorial identities |
| 05A20 | Combinatorial inequalities |
| 05A30 | $q$-calculus and related topics [See also 03Dxx] |
| 05A40 | Umbral calculus |
| 05A99 | None of the above, but in this section |
| 05Bxx | Designs and configurations \{For applications of design theory, see $\mathbf{9 4 C 3 0}\}$ |
| 05B05 | Block designs [See also 51E05, 62K10] |
| 05B07 | Triple systems |
| 05B10 | Difference sets (number-theoretic, grouptheoretic, etc.) [See also 11B13] |
| 05B15 | Orthogonal arrays, Latin squares, Room squares |
| 05B20 | Matrices (incidence, Hadamard, etc.) |
| 05B25 | Finite geometries [See also 51D20, 51Exx] |
| 05B30 | Other designs, configurations [See also 51E30] |

05B35

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05B99
05Cxx

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05C38
05C40
05C45
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05C60

05C62

05C65
05C69
05 C 70
05C75
05C78
05C80
05C83
05C85
05C90
05C99
05Dxx
05D05
05D10
05D15 Transversal (matching) theory
05D40 Probabilistic methods
05D99 None of the above, but in this section
05Exx Algebraic combinatorics
05E05
05E10

05E15

05E20
05E25

05E30
Matroids, geometric lattices [See also 52B40, 90C27]
Packing and covering [See also $11 \mathrm{H} 31,52 \mathrm{C} 15$, 52C17]
Tessellation and tiling problems [See also 52C20, 52C22]
Polyominoes
None of the above, but in this section
Graph theory $\{$ For applications of graphs, see 68R10, 90C35, 94C15\}
Trees
Degree sequences
Topological graph theory, imbedding
[See also 57M15, 57M25]
Distance in graphs
Coloring of graphs and hypergraphs
Perfect graphs
Directed graphs (digraphs), tournaments
Signed, gain and biased graphs
Graphs and groups [See also 20F65]
Enumeration of graphs and maps
Extremal problems [See also 90C35]
Paths and cycles [See also 90B10]
Connectivity
Eulerian and Hamiltonian graphs
Graphs and matrices
Generalized Ramsey theory
Isomorphism problems (reconstruction conjecture, etc.)
Graph representations (geometric and intersection representations, etc.)
Hypergraphs
Dominating sets, independent sets, cliques
Factorization, matching, covering and packing
Structural characterization of types of graphs
Graph labelling (graceful graphs, bandwidth, etc.)
Random graphs
Graph minors
Graph algorithms [See also 68R10, 68W05]
Applications
None of the above, but in this section
Extremal combinatorics
Extremal set theory
Ramsey theory

Symmetric functions
Tableaux, representations of the symmetric group [See also 20C30]
Combinatorial problems concerning the classical groups [See also 22E45, 33C80]
Group actions on designs, geometries and codes
Group actions on posets and homology groups of posets [See also 06A11]
Association schemes, strongly regular graphs

| 05E35 | Orthogonal polynomials [See also 33C45, 33C50, 33D45] |
| :---: | :---: |
| 05E99 | None of the above, but in this section |
| 06-XX | ORDER, LATTICES, ORDERED |
|  | ALGEBRAIC STRUCTURES [See also 18B35] |
| 06-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 06-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 06-02 | Research exposition (monographs, survey articles) |
| 06-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 06-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 06-06 | Proceedings, conferences, collections, etc. |
| 06Axx | Ordered sets |
| 06A05 | Total order |
| 06A06 | Partial order, general |
| 06A07 | Combinatorics of partially ordered sets |
| 06A11 | Algebraic aspects of posets [See also 05E25] |
| 06A12 | Semilattices [See also 20M10; for topological semilattices see 22A26] |
| 06A15 | Galois correspondences, closure operators |
| 06A99 | None of the above, but in this section |
| 06Bxx | Lattices [See also 03G10] |
| 06B05 | Structure theory |
| 06B10 | Ideals, congruence relations |
| 06B15 | Representation theory |
| 06B20 | Varieties of lattices |
| 06B23 | Complete lattices, completions |
| 06B25 | Free lattices, projective lattices, word problems [See also 03D40, 08A50, 20F10] |
| 06B30 | Topological lattices, order topologies [See also 06F30, 22A26, 54F05, 54H12] |
| 06B35 | Continuous lattices and posets, applications [See also 06B30, 06D10, 06F30, 18B35, 22A26, 68Q55] |
| 06B99 | None of the above, but in this section |
| 06Cxx | Modular lattices, complemented lattices |
| 06 C 05 | Modular lattices, Desarguesian lattices |
| 06 C 10 | Semimodular lattices, geometric lattices |
| 06 C 15 | Complemented lattices, orthocomplemented lattices and posets [See also 03G12, 81P10] |
| 06C20 | Complemented modular lattices, continuous geometries |
| 06C99 | None of the above, but in this section |
| 06Dxx | Distributive lattices |
| 06D05 | Structure and representation theory |
| 06D10 | Complete distributivity |
| 06D15 | Pseudocomplemented lattices |
| 06D20 | Heyting algebras [See also 03G25] |
| 06D22 | Frames, locales \{For topological questions see 54-XX\} |
| 06D25 | Post algebras [See also 03G20] |
| 06D30 | De Morgan algebras, Łukasiewicz algebras [See also 03G20] |
| 06D35 | MV-algebras |

Orthogonal polynomials [See also 33C45, 33C50, 33D45]
05E99
06-XX ORDER, LATTICES, ORDERED ALGEBRAIC STRUCTURES [See also 18B35] bibliographies, etc.) papers, etc.)
06-02 Research exposition (monographs, survey articles)

06-06
06Axx
06A05
06A06 Partial order, general
06A07 Combinatorics of partially ordered sets
06A11 Algebraic aspects of posets [See also 05E25]
06A12 Semilattices [See also 20M10; for topological semilattices see 22A26]
06A15 Galois correspondences, closure operators

06B05 Structure theory
06B10 Ideals, congruence relations
06B15 Representation theory
Varieties of lattices
Complete lattices, completions
06B25 Free lattices, projective lattices, word problems [See also 03D40, 08A50, 20F10]
[See also 06F30, 22A26, 54F05, 54H12]
[See also 06B30, 06D10, 06F30, 18B35, 22A26, 68Q55]
None of the above, but in this section

06C05 Modular lattices, Desarguesian lattices
06C10 Semimodular lattices, geometric lattices
06C15 Complemented lattices, orthocomplemented lattices and posets [See also 03G12, 81P10]
06C20 Complemented modular lattices, continuous geometries
None of the above, but in this section

06D05 Structure and representation theory
06D10 Complete distributivity
06D15 Pseudocomplemented lattices
06D20 Heyting algebras [See also 03G25]
06D22 Frames, locales \{For topological questions see 54-XX\}
06D25 Post algebras [See also 03G20]
06D30 De Morgan algebras, Łukasiewicz algebras
[See also 03G20]
06D35 MV-algebras

06D50 Lattices and duality
06D72 Fuzzy lattices (soft algebras) and related topics
06D99 None of the above, but in this section
06Exx Boolean algebras (Boolean rings)
[See also 03G05]
06E05
06E10
06E15
06E20

06E25

06E30
06E99
06Fxx
06F05

06F07
06F10
06F15
06F20

06F25

06F30

06F35
06F99
08-XX
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08-02
08-03
08-04

08-06
08Axx
08A02
08A05
08A30
08A35
08A40
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08A50
08A55
08A60
08A62
08A65
08A68
08A70

08A72

Structure theory
Chain conditions, complete algebras
Stone space and related constructions
Ring-theoretic properties [See also 16E50, 16G30]
Boolean algebras with additional operations (diagonalizable algebras, etc.) [See also 03G25, 03F45]
Boolean functions [See also 94C10]
None of the above, but in this section
Ordered structures
Ordered semigroups and monoids
[See also 20Mxx]
Quantales
Noether lattices
Ordered groups [See also 20F60]
Ordered abelian groups, Riesz groups, ordered linear spaces [See also 46A40]
Ordered rings, algebras, modules \{For ordered
fields, see 12J15; see also 13J25, 16W80\}
Topological lattices, order topologies
[See also 06B30, 22A26, 54F05, 54H12]
BCK-algebras, BCI-algebras [See also 03G25]
None of the above, but in this section
GENERAL ALGEBRAIC SYSTEMS
General reference works (handbooks, dictionaries, bibliographies, etc.)
Instructional exposition (textbooks, tutorial papers, etc.)
Research exposition (monographs, survey articles)
Historical (must also be assigned at least one classification number from Section 01)
Explicit machine computation and programs (not the theory of computation or programming)
Proceedings, conferences, collections, etc.
Algebraic structures [See also 03C05]
Relational systems, laws of composition
Structure theory
Subalgebras, congruence relations
Automorphisms, endomorphisms
Operations, polynomials, primal algebras
Equational compactness
Word problems [See also 03D40, 06B25, 20F10, 68R15]
Partial algebras
Unary algebras
Finitary algebras
Infinitary algebras
Heterogeneous algebras
Applications of universal algebra in computer science
Fuzzy algebraic structures

| 08A99 | None of the above, but in this section |
| :--- | :--- |
| 08Bxx | Varieties [See also 03C05] |
| 08B05 | Equational logic, Mal'cev (Maltsev) conditions |
| 08B10 | Congruence modularity, congruence distributivity |
| 08B15 | Lattices of varieties |
| 08B20 | Free algebras |
| 08B25 | Products, amalgamated products, and other kinds <br> of limits and colimits [See also 18A30] |
| 08B26 | Subdirect products and subdirect irreducibility |
| 08B30 | Injectives, projectives |
| 08B99 | None of the above, but in this section |
| 08Cxx | Other classes of algebras |
| 08C05 | Categories of algebras [See also 18C05] |
| 08C10 | Axiomatic model classes [See also 03Cxx, in |
| particular 03C60] |  |

11B68
11B73
11B75
11B83
11B85
11B99
11 Cxx
11C08
11 C 20
11C99
11Dxx

11D04
11D09
11D25
11D41
11D45
11D57
11D59
11D61
11D68
11D72
11D75
11D79
11D85
11D88
11D99
11Exx

11E04
11E08
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11E12
11E16
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11E25

11E39
11E41
11E45

11E57
11E70
11E72

11E76
11E81

11 E 88

11E95
11E99

Bernoulli and Euler numbers and polynomials
Bell and Stirling numbers
Other combinatorial number theory
Special sequences and polynomials
Automata sequences
None of the above, but in this section
Polynomials and matrices
Polynomials [See also 13F20]
Matrices, determinants [See also 15A36]
None of the above, but in this section
Diophantine equations [See also 11Gxx, 14Gxx]
Linear equations
Quadratic and bilinear equations
Cubic and quartic equations
Higher degree equations; Fermat's equation
Counting solutions of Diophantine equations
Multiplicative and norm form equations
Thue-Mahler equations
Exponential equations
Rational numbers as sums of fractions
Equations in many variables [See also 11P55]
Diophantine inequalities [See also 11J25]
Congruences in many variables
Representation problems [See also 11P55]
$p$-adic and power series fields
None of the above, but in this section
Forms and linear algebraic groups [See also 19Gxx] \{For quadratic forms in linear algebra, see 15 A 63$\}$
Quadratic forms over general fields
Quadratic forms over local rings and fields
Forms over real fields
Quadratic forms over global rings and fields
General binary quadratic forms
General ternary and quaternary quadratic forms;
forms of more than two variables
Sums of squares and representations by other particular quadratic forms
Bilinear and Hermitian forms
Class numbers of quadratic and Hermitian forms
Analytic theory (Epstein zeta functions; relations with automorphic forms and functions)
Classical groups [See also 14Lxx, 20Gxx]
$K$-theory of quadratic and Hermitian forms
Galois cohomology of linear algebraic groups [See also 20G10]
Forms of degree higher than two
Algebraic theory of quadratic forms; Witt groups
and rings [See also 19G12, 19G24]
Quadratic spaces; Clifford algebras
[See also 15A63, 15A66]
$p$-adic theory
None of the above, but in this section

| 11Fxx | Discontinuous groups and automorphic forms <br> [See also 11R39, 11S37, 14Gxx, 14Kxx, 22E50, |
| :--- | :--- |
|  | 22E55, 30F35, 32Nxx] \{For relations with <br> quadratic forms, see 11E45\} |
| 11F03 | Modular and automorphic functions |
| 11F06 | Structure of modular groups and generalizations; <br> arithmetic groups [See also 20H05, 20H10, <br> 22E40] |
| 11F11 | Modular forms, one variable |
| 11F12 | Automorphic forms, one variable |
| 11F20 | Dedekind eta function, Dedekind sums <br> Relationship to Lie algebras and finite simple <br> groups |
| 11F22 | Relations with algebraic geometry and topology |
| 11F23 | Hecke-Petersson operators, differential operators <br> (one variable) |
| 11F25 |  |

11G16
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11H06
11H16
11H31

11H46
11H50

11H56
11H60
11H71
11H99
11Jxx

11J04
11 J06
11J13

11 J 17
11J20
11J25
11J54
11J61
11 J68
11 J 70

11J71
11 J72
11J81
11 J 82
11 J83
11 J85
11 J 86
11 J 89
11J91
11 J 93

11G55 Polylogarithms and relations with $K$-theory
11G99 None of the above, but in this section
11Hxx Geometry of numbers \{For applications in coding theory, see 94B75\}

11H55 Quadratic forms (reduction theory, extreme forms, etc.)
Elliptic and modular units [See also 11R27]
Arithmetic aspects of modular and Shimura varieties [See also 14G35]
Curves over finite and local fields
[See also 14H25]
Varieties over finite and local fields [See also 14G15, 14G20]
Curves of arbitrary genus or genus $\neq 1$ over global fields [See also 14H25]
Varieties over global fields [See also 14G25]
$L$-functions of varieties over global fields; Birch-
Swinnerton-Dyer conjecture [See also 14G10]
Geometric class field theory [See also 11R37,
14C35, 19F05]
Heights [See also 14G40]

Lattices and convex bodies [See also 11P21, 52C05, 52C07]
Nonconvex bodies
Lattice packing and covering [See also 05B40,
52C15, 52C17]
Products of linear forms
Minima of forms

Automorphism groups of lattices
Mean value and transfer theorems
Relations with coding theory
None of the above, but in this section
Diophantine approximation, transcendental number theory [See also 11K60]
Homogeneous approximation to one number Markov and Lagrange spectra and generalizations Simultaneous homogeneous approximation, linear forms
Approximation by numbers from a fixed field Inhomogeneous linear forms
Diophantine inequalities [See also 11D75]
Small fractional parts of polynomials and generalizations
Approximation in non-Archimedean valuations
Approximation to algebraic numbers
Continued fractions and generalizations
[See also 11A55, 11K50]
Distribution modulo one [See also 11K06]
Irrationality; linear independence over a field Transcendence (general theory)
Measures of irrationality and of transcendence Metric theory
Algebraic independence; Gel'fond's method
Linear forms in logarithms; Baker's method
Transcendence theory of elliptic and abelian functions
Transcendence theory of other special functions
Transcendence theory of Drinfel'd and $t$-modules

| 11J95 | Results involving abelian varieties <br> Analogues of methods in Nevanlinna theory <br> (work of Vojta et al.) |
| :--- | :--- |
| 11J97 | None of the above, but in this section |
| 11J99 | Nrobabilistic theory: distribution modulo 1; <br> 11Kxx <br> Protric theory of algorithms |
| 11K06 | General theory of distribution modulo 1 <br> [See also 11J71] |
| 11K16 | Normal numbers, radix expansions, etc. <br> [See also 11A63] |
| 11K31 | Special sequences |
| 11K36 | Well-distributed sequences and other variations |
| 11K38 | Irregularities of distribution, discrepancy |
| [See also 11Nxx] |  |

11 N 25

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11 N 32

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11N45

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11N60

11N64

11N69
11N75

11N80
11N99
11Pxx
11P05
11P21
11P32

11P55
11 P70
11P81
11P82
11P83

11P99
11Rxx

11R04
11R06

11R09
11R11
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11R18
11R20
11R21
11R23
11R27
11R29
11R32
11R33

11R34 Galois cohomology [See also 12Gxx, 16H05, 19A31]
11R37
11R39 Langlands-Weil conjectures, nonabelian class field theory [See also 11Fxx, 22E55]
11R42 Zeta functions and $L$-functions of number fields [See also 11M41, 19F27]

| 11R44 | Distribution of prime ideals [See also 11N05] |
| :---: | :---: |
| 11R45 | Density theorems |
| 11R47 | Other analytic theory [See also 11Nxx] |
| 11R52 | Quaternion and other division algebras: arithmetic, zeta functions |
| 11R54 | Other algebras and orders, and their zeta and $L$ functions [See also $11 \mathrm{~S} 45,16 \mathrm{H} 05,16 \mathrm{Kxx}$ ] |
| 11R56 | Adèle rings and groups |
| 11R58 | Arithmetic theory of algebraic function fields [See also 14-XX] |
| 11R60 | Cyclotomic function fields (class groups, Bernoulli objects, etc.) |
| 11R65 | Class groups and Picard groups of orders |
| 11R70 | $K$-theory of global fields [See also 19Fxx] |
| 11R80 | Totally real and totally positive fields [See also 12J15] |
| 11R99 | None of the above, but in this section |
| 11Sxx | Algebraic number theory: local and $p$-adic fields |
| 11S05 | Polynomials |
| 11S15 | Ramification and extension theory |
| 11S20 | Galois theory |
| 11S23 | Integral representations |
| 11S25 | Galois cohomology [See also 12Gxx, 16H05] |
| 11S31 | Class field theory; $p$-adic formal groups [See also 14L05] |
| 11S37 | Langlands-Weil conjectures, nonabelian class field theory [See also 11Fxx, 22E50] |
| 11S40 | Zeta functions and $L$-functions [See also 11 M 41 , 19F27] |
| 11S45 | Algebras and orders, and their zeta functions [See also 11R52, 11R54, 16H05, 16Kxx] |
| 11S70 | $K$-theory of local fields [See also 19Fxx] |
| 11S80 | Other analytic theory (analogues of beta and gamma functions, $p$-adic integration, etc.) |
| 11S85 | Other nonanalytic theory |
| 11S90 | Prehomogeneous vector spaces |
| 11S99 | None of the above, but in this section |
| 11Txx | Finite fields and commutative rings (numbertheoretic aspects) |
| 11 T 06 | Polynomials |
| 11 T 22 | Cyclotomy |
| 11 T 23 | Exponential sums |
| 11 T 24 | Other character sums and Gauss sums |
| 11 T 30 | Structure theory |
| 11 T 55 | Arithmetic theory of polynomial rings over finite fields |
| 11 T 60 | Finite upper half-planes |
| 11 T 71 | Algebraic coding theory; cryptography |
| 11 T 99 | None of the above, but in this section |
| 11Uxx | Connections with logic |
| 11U05 | Decidability [See also 03B25] |
| 11U07 | Ultraproducts [See also 03C20] |
| 11U09 | Model theory [See also 03Cxx] |
| 11 U 10 | Nonstandard arithmetic [See also 03H15] |
| 11U99 | None of the above, but in this section |

11Yxx

11 Y 05
11 Y 11
11 Y 16
11 Y 35
11 Y 40
11 Y50
11 Y55
11 Y60
11 Y 65
11 Y 70
11 Y99
$11 Z 05$
12-XX
12-00

12-01

12-02
12-03

12-04

12-06
12Dxx
12D05
12D10

12D15

12D99
12Exx
12E05
12E10
12E12
12E15

12E20
12E25
12E30
12E99
12Fxx
12F05
12 F 10
12 F 12
12F15
12F20
12F99
12Gxx
12G05

12G10
12G99

## Computational number theory [See also 11-

 04]Factorization
Primality
Algorithms; complexity [See also 68Q25]
Analytic computations
Algebraic number theory computations
Computer solution of Diophantine equations
Calculation of integer sequences
Evaluation of constants
Continued fraction calculations
Values of arithmetic functions; tables
None of the above, but in this section
Miscellaneous applications of number theory
FIELD THEORY AND POLYNOMIALS
General reference works (handbooks, dictionaries, bibliographies, etc.)
Instructional exposition (textbooks, tutorial papers, etc.)
Research exposition (monographs, survey articles)
Historical (must also be assigned at least one classification number from Section 01)
Explicit machine computation and programs (not the theory of computation or programming)
Proceedings, conferences, collections, etc.
Real and complex fields
Polynomials: factorization
Polynomials: location of zeros (algebraic theorems) \{For the analytic theory, see 26C10, 30C15\}
Fields related with sums of squares (formally real
fields, Pythagorean fields, etc.) [See also 11Exx]
None of the above, but in this section
General field theory
Polynomials (irreducibility, etc.)
Special polynomials
Equations
Skew fields, division rings [See also 11R52, 11R54, 11S45, 16Kxx]
Finite fields (field-theoretic aspects)
Hilbertian fields; Hilbert's irreducibility theorem
Field arithmetic
None of the above, but in this section
Field extensions
Algebraic extensions
Separable extensions, Galois theory
Inverse Galois theory
Inseparable extensions
Transcendental extensions
None of the above, but in this section
Homological methods (field theory)
Galois cohomology [See also 14F22, 16H05, 16K50]
Cohomological dimension
None of the above, but in this section

| 12Hxx | Differential and difference algebra |
| :---: | :---: |
| 12H05 | Differential algebra [See also 13Nxx] |
| 12H10 | Difference algebra [See also 39Axx] |
| 12H20 | Abstract differential equations [See also 34Mxx] |
| 12H25 | $p$-adic differential equations [See also 11S80, 14G20] |
| 12H99 | None of the above, but in this section |
| 12Jxx | Topological fields |
| 12 J 05 | Normed fields |
| 12 J 10 | Valued fields |
| 12J12 | Formally $p$-adic fields |
| 12J15 | Ordered fields |
| 12J17 | Topological semifields |
| 12 J 20 | General valuation theory [See also 13A18] |
| 12 J 25 | Non-Archimedean valued fields [See also 30G06, 32P05, 46S10, 47S10] |
| 12J27 | Krasner-Tate algebras [See mainly 32P05; see also 46S10, 47S10] |
| 12 J 99 | None of the above, but in this section |
| 12Kxx | Generalizations of fields |
| 12K05 | Near-fields [See also 16Y30] |
| 12K10 | Semifields [See also 16Y60] |
| 12K99 | None of the above, but in this section |
| 12Lxx | Connections with logic |
| 12L05 | Decidability [See also 03B25] |
| 12L10 | Ultraproducts [See also 03C20] |
| 12L12 | Model theory [See also 03C60] |
| 12L15 | Nonstandard arithmetic [See also 03H15] |
| 12L99 | None of the above, but in this section |
| 12Y05 | Computational aspects of field theory and polynomials |
| 13-XX | COMMUTATIVE RINGS AND ALGEBRAS |
| 13-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 13-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 13-02 | Research exposition (monographs, survey articles) |
| 13-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 13-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 13-06 | Proceedings, conferences, collections, etc. |
| 13Axx | General commutative ring theory |
| 13A02 | Graded rings [See also 16W50] |
| 13A05 | Divisibility |
| 13A10 | Radical theory |
| 13A15 | Ideals; multiplicative ideal theory |
| 13A18 | Valuations and their generalizations [See also 12J20] |
| 13A30 | Associated graded rings of ideals (Rees ring, form ring), analytic spread and related topics |
| 13A35 | Characteristic $p$ methods (Frobenius endomorphism) and reduction to characteristic $p$; tight closure [See also 13B22] |
| 13A50 | Actions of groups on commutative rings; invariant theory [See also 14L24] |
| 13A99 | None of the above, but in this section |

13Bxx
13B02
13B05
13B10
13B21
13B22

13B24
13B25

13B30
13B35
13B40

13B99
13Cxx
13C05
13 C 10

13C11
13 C 12
13 C 13
13 C 14
13 C 15

13 C 20
13 C 40

13C99
13Dxx

13D02
13D03

13D05
13D07
13D10

13D15

13D22
13D25
13D30
13D40

13D45
13D99
13Exx
13E05
13E10

13E15

13E99

Ring extensions and related topics
Extension theory
Galois theory
Morphisms
Integral dependence
Integral closure of rings and ideals
[See also 13A35]; integrally closed rings, related
rings (Japanese, etc.)
Going up; going down; going between
Polynomials over commutative rings
[See also 11C08, 13F20, 13M10]
Quotients and localization
Completion [See also 13J10]
Étale and flat extensions; Henselization; Artin
approximation [See also 13J15, 14B12, 14B25]
None of the above, but in this section
Theory of modules and ideals
Structure, classification theorems
Projective and free modules and ideals [See also 19A13]
Injective and flat modules and ideals
Torsion modules and ideals
Other special types
Cohen-Macaulay modules [See also 13 H 10 ]
Dimension theory, depth, related rings (catenary, etc.)
Class groups [See also 11R29]
Linkage, complete intersections and determinantal ideals [See also 14M06, 14M10, 14M12]
None of the above, but in this section
Homological methods \{For noncommutative
rings, see 16Exx; for general categories, see 18Gxx\}
Syzygies and resolutions
(Co)homology of commutative rings and algebras
(e.g., Hochschild, André-Quillen, cyclic, dihedral, etc.)
Homological dimension
Homological functors on modules (Tor, Ext, etc.)
Deformations and infinitesimal methods
[See also 14B10, 14B12, 14D15, 32Gxx]
Grothendieck groups, $K$-theory [See also 14C35,
18F30, 19Axx, 19D50]
Homological conjectures (intersection theorems)
Complexes
Torsion theory [See also 13C12, 18E40]
Hilbert-Samuel and Hilbert-Kunz functions;
Poincaré series
Local cohomology [See also 14B15]
None of the above, but in this section
Chain conditions, finiteness conditions
Noetherian rings and modules
Artinian rings and modules, finite-dimensional algebras
Rings and modules of finite generation or presentation; number of generators
None of the above, but in this section

| 13Fxx | Arithmetic rings and other special rings |
| :---: | :---: |
| 13F05 | Dedekind, Prüfer and Krull rings and their generalizations |
| 13F07 | Euclidean rings and generalizations |
| 13 F 10 | Principal ideal rings |
| 13F15 | Factorial rings, unique factorization domains [See also 14M05] |
| 13F20 | Polynomial rings and ideals; rings of integervalued polynomials [See also 11C08, 13B25] |
| 13F25 | Formal power series rings [See also 13J05] |
| 13F30 | Valuation rings [See also 13A18] |
| 13 F 40 | Excellent rings |
| 13F45 | Seminormal rings |
| 13 F 50 | Rings with straightening laws, Hodge algebras |
| 13 F 55 | Face and Stanley-Reisner rings; simplicial complexes [See also 55U10] |
| 13F99 | None of the above, but in this section |
| 13G05 | Integral domains |
| 13Hxx | Local rings and semilocal rings |
| 13H05 | Regular local rings |
| 13H10 | Special types (Cohen-Macaulay, Gorenstein, Buchsbaum, etc.) [See also 14M05] |
| 13H15 | Multiplicity theory and related topics [See also 14C17] |
| 13H99 | None of the above, but in this section |
| 13Jxx | Topological rings and modules [See also 16W60, 16W80] |
| 13J05 | Power series rings [See also 13F25] |
| 13J07 | Analytical algebras and rings [See also 32B05] |
| 13 J 10 | Complete rings, completion [See also 13B35] |
| 13J15 | Henselian rings [See also 13B40] |
| 13J20 | Global topological rings |
| 13J25 | Ordered rings [See also 06F25] |
| 13 J 30 | Real algebra [See also 12D15, 14Pxx] |
| 13 J 99 | None of the above, but in this section |
| $13 \mathrm{K05}$ | Witt vectors and related rings |
| 13L05 | Applications of logic to commutative algebra [See also 03Cxx, 03Hxx] |
| 13Mxx | Finite commutative rings $\{$ For numbertheoretic aspects, see 11Txx\} |
| 13M05 | Structure |
| 13M10 | Polynomials |
| 13M99 | None of the above, but in this section |
| 13Nxx | Differential algebra [See also 12H05, 14F10] |
| 13N05 | Modules of differentials |
| 13N10 | Rings of differential operators and their modules [See also 16S32, 32C38] |
| 13N15 | Derivations |
| 13N99 | None of the above, but in this section |
| 13Pxx | Computational aspects of commutative algebra [See also 68W30] |
| 13 P 05 | Polynomials, factorization [See also 12Y05] |
| 13 P 10 | Polynomial ideals, Gröbner bases [See also 13F20] |
| 13P99 | None of the above, but in this section |


| 14-XX | ALGEBRAIC GEOMETRY |
| :---: | :---: |
| 14-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 14-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 14-02 | Research exposition (monographs, survey articles) |
| 14-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 14-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 14-06 | Proceedings, conferences, collections, etc. |
| 14Axx | Foundations |
| 14 A 05 | Relevant commutative algebra [See also 13-XX] |
| 14A10 | Varieties and morphisms |
| 14A15 | Schemes and morphisms |
| 14 A 20 | Generalizations (algebraic spaces, stacks) |
| 14A22 | Noncommutative algebraic geometry |
| 14 A 25 | Elementary questions |
| 14A99 | None of the above, but in this section |
| 14Bxx | Local theory |
| 14B05 | Singularities [See also 14E15, 14H20, 14J17, 32Sxx, 58Kxx] |
| 14B07 | Deformations of singularities [See also 14D15, 32S30] |
| 14B10 | Infinitesimal methods [See also 13D10] |
| 14B12 | Local deformation theory, Artin approximation, etc. [See also 13B40, 13D10] |
| 14B15 | Local cohomology [See also 13D45, 32C36] |
| 14B20 | Formal neighborhoods |
| 14B25 | Local structure of morphisms: étale, flat, etc. [See also 13B40] |
| 14B99 | None of the above, but in this section |
| 14Cxx | Cycles and subschemes |
| 14 C 05 | Parametrization (Chow and Hilbert schemes) |
| 14 C 15 | Chow groups and rings |
| 14 C 17 | Intersection theory, characteristic classes, intersection multiplicities [See also 13H15] |
| 14C20 | Divisors, linear systems, invertible sheaves |
| 14 C 21 | Pencils, nets, webs [See also 53A60] |
| 14 C 22 | Picard groups |
| 14 C 25 | Algebraic cycles |
| 14C30 | Transcendental methods, Hodge theory [See also 14D07, 32G20, 32J25, 32S35], Hodge conjecture |
| 14C34 | Torelli problem [See also 32G20] |
| 14C35 | Applications of methods of algebraic $K$-theory [See also 19Exx] |
| 14C40 | Riemann-Roch theorems [See also 19E20, 19L10] |
| 14C99 | None of the above, but in this section |
| 14Dxx | Families, fibrations |
| 14D05 | Structure of families (Picard-Lefschetz, monodromy, etc.) |
| 14D06 | Fibrations, degenerations |
| 14D07 | Variation of Hodge structures [See also 32G20] |
| 14D10 | Arithmetic ground fields (finite, local, global) |
| 14D15 | Formal methods; deformations [See also 13D10, 14B07, 32Gxx] |

ALGEBRAIC GEOMETRY
General reference works (handbooks, dictionaries, bibliographies, etc.) papers, etc.)
Research exposition (monographs, survey articles) classification number from Section 01)
Explicit machine computation and programs (not or programming)
14-06
14Axx
14A05
14A10
14A15
14A20
14A22
14A25
14A99

14B05

14B07

14B10
14B12

14B15
14B20
14B25

14B99
14Cxx
-
14 C 17

14C20
14 C 21
14C22
14C25
14C30 Transcendental methods, Hodge theory
[See also 14D07, 32G20, 32J25, 32S35], Hodge conjecture
14C34 Torelli problem [See also 32G20] [See also 19Exx]
14C40 Riemann-Roch theorems [See also 19E20, 19L10]
14C99 None of the above, but in this section
14Dxx Families, fibrations
14D05 Structure of families (Picard-Lefschetz, monodromy, etc.)
Fibrations, degenerations
Variation of Hodge structures [See also 32G20]

Formal methods; deformations [See also 13D10, 14B07, 32Gxx]

| 14D20 | Algebraic moduli problems, moduli of vector <br> bundles \{For analytic moduli problems, see <br> 32G13\} |
| :--- | :--- |
| 14D21 |  |


| 14G35 | Modular and Shimura varieties [See also 11F41, 11F46, 11G18] |
| :---: | :---: |
| 14G40 | Arithmetic varieties and schemes; Arakelov theory; heights [See also 11G50] |
| 14G50 | Applications to coding theory and cryptography [See also 94A60, 94B27, 94B40] |
| 14G99 | None of the above, but in this section |
| 14Hxx | Curves |
| 14H05 | Algebraic functions; function fields [See also 11R58] |
| 14H10 | Families, moduli (algebraic) |
| 14H15 | Families, moduli (analytic) [See also 30F10, 32Gxx] |
| 14H20 | Singularities, local rings [See also 13Hxx, 14B05] |
| 14H25 | Arithmetic ground fields [See also 11Dxx, 11G05, 14Gxx] |
| 14H30 | Coverings, fundamental group [See also 14E20, 14F35] |
| 14H37 | Automorphisms |
| 14H40 | Jacobians, Prym varieties [See also 32G20] |
| 14H42 | Theta functions; Schottky problem [See also 14K25, 32G20] |
| 14H45 | Special curves and curves of low genus |
| 14H50 | Plane and space curves |
| 14H51 | Special divisors (gonality, Brill-Noether theory) |
| 14H52 | Elliptic curves [See also 11G05, 11G07, 14Kxx] |
| 14H55 | Riemann surfaces; Weierstrass points; gap sequences [See also 30Fxx] |
| 14H60 | Vector bundles on curves and their moduli [See also 14D20, 14F05] |
| 14H70 | Relationships with integrable systems |
| 14H81 | Relationships with physics |
| 14H99 | None of the above, but in this section |
| 14Jxx | Surfaces and higher-dimensional varieties \{For analytic theory, see 32Jxx\} |
| 14J10 | Families, moduli, classification: algebraic theory |
| 14J15 | Moduli, classification: analytic theory; relations with modular forms [See also 32G13] |
| 14J17 | Singularities [See also 14B05, 14E15] |
| 14J20 | Arithmetic ground fields [See also 11Dxx, 11G25, 11G35, 14Gxx] |
| 14J25 | Special surfaces \{For Hilbert modular surfaces, see 14G35\} |
| 14J26 | Rational and ruled surfaces |
| 14 J 27 | Elliptic surfaces |
| 14 J 28 | K3 surfaces and Enriques surfaces |
| 14 J 29 | Surfaces of general type |
| 14 J 30 | 3-folds |
| 14 J 32 | Calabi-Yau manifolds, mirror symmetry |
| 14 J 35 | 4-folds |
| 14 J 40 | $n$-folds ( $n>4$ ) |
| 14 J 45 | Fano varieties |
| 14 J 50 | Automorphisms of surfaces and higherdimensional varieties |
| 14J60 | Vector bundles on surfaces and higherdimensional varieties, and their moduli [See also 14D20, 14F05, 32Lxx] |


| 14 J 70 | Hypersurfaces |
| :---: | :---: |
| 14J80 | Topology of surfaces (Donaldson polynomials, Seiberg-Witten invariants) |
| 14J81 | Relationships with physics |
| 14J99 | None of the above, but in this section |
| 14Kxx | Abelian varieties and schemes |
| 14K02 | Isogeny |
| 14K05 | Algebraic theory |
| 14K10 | Algebraic moduli, classification [See also 11G15] |
| 14K12 | Subvarieties |
| 14K15 | Arithmetic ground fields [See also 11Dxx, 11Fxx, 11Gxx, 14Gxx] |
| 14K20 | Analytic theory; abelian integrals and differentials |
| 14K22 | Complex multiplication [See also 11G15] |
| 14K25 | Theta functions [See also 14H42] |
| 14K30 | Picard schemes, higher Jacobians [See also 14H40, 32G20] |
| 14K99 | None of the above, but in this section |
| 14Lxx | Algebraic groups \{For linear algebraic groups, see 20Gxx; for Lie algebras, see 17B45\} |
| 14L05 | Formal groups, $p$-divisible groups [See also 55N22] |
| 14L10 | Group varieties |
| 14L15 | Group schemes |
| 14L17 | Affine algebraic groups, hyperalgebra constructions [See also 17B45, 18D35] |
| 14L24 | Geometric invariant theory [See also 13A50] |
| 14L30 | Group actions on varieties or schemes (quotients) [See also 13A50, 14L24] |
| 14L35 | Classical groups (geometric aspects) [See also 20Gxx, 51N30] |
| 14L40 | Other algebraic groups (geometric aspects) |
| 14L99 | None of the above, but in this section |
| 14Mxx | Special varieties |
| 14M05 | Varieties defined by ring conditions (factorial, Cohen-Macaulay, seminormal) [See also 13F45, 13H10] |
| 14M06 | Linkage [See also 13C40] |
| 14M07 | Low codimension problems |
| 14M10 | Complete intersections [See also 13C40] |
| 14M12 | Determinantal varieties [See also 13C40] |
| 14M15 | Grassmannians, Schubert varieties, flag manifolds [See also 32M10, 51M35] |
| 14M17 | Homogeneous spaces and generalizations [See also 32M10, 53C30, 57T15] |
| 14M20 | Rational and unirational varieties |
| 14M25 | Toric varieties, Newton polyhedra [See also 52B20] |
| 14M30 | Supervarieties [See also 32C11, 58A50] |
| 14M99 | None of the above, but in this section |
| 14Nxx | Projective and enumerative geometry [See also 51-XX] |
| 14N05 | Projective techniques [See also 51N35] |
| 14N10 | Enumerative problems (combinatorial problems) |
| 14N15 | Classical problems, Schubert calculus |
| 14N20 | Configurations of linear subspaces |
| 14N25 | Varieties of low degree |
| 14N30 | Adjunction problems |


| 14N35 | Gromov-Witten invariants, quantum cohomology |
| :--- | :--- |
|  | [See also 53D45] |
| 14N99 | None of the above, but in this section |
| 14Pxx | Real algebraic and real analytic geometry |
| 14P05 | Real algebraic sets [See also 12Dxx] |
| 14P10 | Semialgebraic sets and related spaces |
| 14P15 | Real analytic and semianalytic sets <br> [See also 32B20, 32C05] |
| 14P20 | Nash functions and manifolds [See also 32C07, |
|  | 58A07] |
| 14P25 | Topology of real algebraic varieties |
| 14P99 | None of the above, but in this section |
| 14Qxx | Computational aspects in algebraic geometry |
|  | [See also 12Y05, 13Pxx, 68W30] |


| 15A33 | Matrices over special rings (quaternions, finite fields, etc.) | 16D70 | Structure and classification (except as in 16Gxx), direct sum decomposition, cancellation |
| :---: | :---: | :---: | :---: |
| 15A36 | Matrices of integers [See also 11C20] | 16D80 | Other classes of modules and ideals |
| 15A39 | Linear inequalities |  | [See also 16G50] |
| 15A42 | Inequalities involving eigenvalues and eigenvectors | 16D90 | Module categories [See also 16Gxx, 16S90]; module theory in a category-theoretic context; |
| 15A45 | Miscellaneous inequalities involving matrices |  | Morita equivalence and duality |
| 15A48 | Positive matrices and their generalizations; cones of matrices | $\begin{aligned} & \text { 16D99 } \\ & \text { 16Exx } \end{aligned}$ | None of the above, but in this section Homological methods \{For commutative rings, |
| 15A51 | Stochastic matrices |  | see 13Dxx; for general categories, see 18Gxx $\}$ |
| 15A52 | Random matrices | 16E05 | Syzygies, resolutions, complexes |
| 15A54 | Matrices over function rings in one or more variables | $\begin{aligned} & \text { 16E10 } \\ & \text { 16E20 } \end{aligned}$ | Homological dimension Grothendieck groups, $K$-theory, etc. |
| 15A57 | Other types of matrices (Hermitian, skewHermitian, etc.) | 16E30 | [See also 18F30, 19Axx, 19D50] <br> Homological functors on modules (Tor, Ext, etc.) |
| 15A60 | Norms of matrices, numerical range, applications of functional analysis to matrix theory [See also 65F35, 65J05] | 16 E 40 16 E 45 | (Co)homology of rings and algebras (e.g. Hochschild, cyclic, dihedral, etc.) Differential graded algebras and applications |
| 15A63 | Quadratic and bilinear forms, inner products [See mainly 11Exx] | $\begin{aligned} & 16 \mathrm{E} 50 \\ & \text { 16E60 } \end{aligned}$ | von Neumann regular rings and generalizations Semihereditary and hereditary rings, free ideal |
| 15A66 | Clifford algebras, spinors |  | rings, Sylvester rings, etc. |
| 15A69 | Multilinear algebra, tensor products | 16E65 | Homological conditions on rings (generalizations |
| 15A72 | Vector and tensor algebra, theory of invariants [See also 13A50, 14L24] |  | of regular, Gorenstein, Cohen-Macaulay rings, etc.) |
| 15A75 | Exterior algebra, Grassmann algebras | 16E99 | None of the above, but in this section |
| 15A78 | Other algebras built from modules | 16Gxx | Representation theory of rings and algebras |
| 15A90 | Applications of matrix theory to physics | 16G10 | Representations of Artinian rings |
| 15A99 | Miscellaneous topics | 16G20 | Representations of quivers and partially ordered sets |
| 16-XX | ASSOCIATIVE RINGS AND ALGEBRAS \{For the commutative case, see 13-XX\} | 16G30 | Representations of orders, lattices, algebras over commutative rings [See also 16 H 05 ] |
| 16-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) | $\begin{aligned} & \text { 16G50 } \\ & \text { 16G60 } \end{aligned}$ | Cohen-Macaulay modules <br> Representation type (finite, tame, wild, etc.) |
| 16-01 | Instructional exposition (textbooks, tutorial papers, etc.) | 16G70 | Auslander-Reiten sequences (almost split sequences) and Auslander-Reiten quivers |
| 16-02 | Research exposition (monographs, survey articles) | 16G99 | None of the above, but in this section |
| 16-03 | Historical (must also be assigned at least one classification number from Section 01) | 16H05 | Orders and arithmetic, separable algebras, Azumaya algebras [See also 11R52, 11R54, |
| 16-04 | Explicit machine computation and programs (not the theory of computation or programming) | 16Kxx | 11S45] Division rings and semisimple Artin rings |
| 16-06 | Proceedings, conferences, collections, etc. |  | [See also 12E15, 15A30] |
| 16Bxx | General and miscellaneous | 16K20 | Finite-dimensional \{For crossed products, see |
| 16B50 | Category-theoretic methods and results (except as in 16D90) [See also 18-XX] | 16K40 | 16S35\} Infinite-dimensional and general |
| 16B70 | Applications of logic [See also 03Cxx] | 16K50 | Brauer groups [See also 12G05, 14F22] |
| 16B99 | None of the above, but in this section | 16K99 | None of the above, but in this section |
| 16Dxx | Modules, bimodules and ideals | 16Lxx | Local rings and generalizations |
| 16D10 | General module theory | 16L30 | Noncommutative local and semilocal rings, |
| 16D20 | Bimodules |  | perfect rings |
| 16D25 | Ideals | 16L60 | Quasi-Frobenius rings [See also 16D50] |
| 16D30 | Infinite-dimensional simple rings (except as in 16 Kxx ) | $\begin{aligned} & \text { 16L99 } \\ & \text { 16Nxx } \end{aligned}$ | None of the above, but in this section Radicals and radical properties of rings |
| 16D40 | Free, projective, and flat modules and ideals | 16N20 | Jacobson radical, quasimultiplication |
|  | [See also 19A13] | 16N40 | Nil and nilpotent radicals, sets, ideals, rings |
| 16D50 | Injective modules, self-injective rings [See also 16L60] | 16N60 | Prime and semiprime rings [See also 16D60, 16U10] |
| 16D60 | Simple and semisimple modules, primitive rings and ideals | 16N80 | General radicals and rings $\{$ For radicals in module categories, see 16 S 90$\}$ |

$\left.\left.\begin{array}{ll}\text { 16N99 } & \begin{array}{l}\text { None of the above, but in this section } \\ \text { Chain conditions, growth conditions, and other } \\ \text { forms of finiteness }\end{array} \\ \text { 16Pxx }\end{array}\right\} \begin{array}{l}\text { Finite rings and finite-dimensional algebras \{For } \\ \text { semisimple, see 16K20; for commutative, see }\end{array}\right\}$

| 16Uxx | Conditions on elements |
| :---: | :---: |
| 16U10 | Integral domains |
| 16U20 | Ore rings, multiplicative sets, Ore localization |
| 16U30 | Divisibility, noncommutative UFDs |
| 16 U 60 | Units, groups of units |
| 16U70 | Center, normalizer (invariant elements) |
| 16 U 80 | Generalizations of commutativity |
| 16U99 | None of the above, but in this section |
| 16Wxx | Rings and algebras with additional structure |
| 16W10 | Rings with involution; Lie, Jordan and other nonassociative structures [See also 17B60, $17 \mathrm{C} 50,46 \mathrm{Kxx}]$ |
| 16W20 | Automorphisms and endomorphisms |
| 16W22 | Actions of groups and semigroups; invariant theory |
| 16W25 | Derivations, actions of Lie algebras |
| 16W30 | Coalgebras, bialgebras, Hopf algebras [See also 16S40, 57T05]; rings, modules, etc. on which these act |
| 16W35 | Ring-theoretic aspects of quantum groups [See also 17B37, 20G42, 81R50] |
| 16W50 | Graded rings and modules |
| 16W55 | "Super" (or "skew") structure [See also 17A70, 17Bxx, 17C70] \{For exterior algebras, see 15A75; for Clifford algebras, see 11E88, 15A66\} |
| 16W60 | Valuations, completions, formal power series and related constructions [See also 13Jxx] |
| 16W70 | Filtered rings; filtrational and graded techniques |
| 16W80 | Topological and ordered rings and modules [See also 06F25, 13Jxx] |
| 16W99 | None of the above, but in this section |
| 16Yxx | Generalizations \{For nonassociative rings, see 17-XX $\}$ |
| 16Y30 | Near-rings [See also 12K05] |
| 16 Y 60 | Semirings [See also 12K10] |
| 16Y99 | None of the above, but in this section |
| 16Z05 | Computational aspects of associative rings [See also 68W30] |
| 17-XX | NONASSOCIATIVE RINGS AND ALGEBRAS |
| 17-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 17-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 17-02 | Research exposition (monographs, survey articles) |
| 17-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 17-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 17-06 | Proceedings, conferences, collections, etc. |
| 17-08 | Computational methods |
| 17Axx | General nonassociative rings |
| 17A01 | General theory |
| 17A05 | Power-associative rings |
| 17A15 | Noncommutative Jordan algebras |
| 17A20 | Flexible algebras |
| 17A30 | Algebras satisfying other identities |


| 17A32 | Leibniz algebras |
| :---: | :---: |
| 17A35 | Division algebras |
| 17A36 | Automorphisms, derivations, other operators |
| 17A40 | Ternary compositions |
| 17A42 | Other $n$-ary compositions ( $n \geq 3$ ) |
| 17A45 | Quadratic algebras (but not quadratic Jordan algebras) |
| 17A50 | Free algebras |
| 17A60 | Structure theory |
| 17A65 | Radical theory |
| 17A70 | Superalgebras |
| 17A75 | Composition algebras |
| 17A80 | Valued algebras |
| 17A99 | None of the above, but in this section |
| 17Bxx | Lie algebras and Lie superalgebras \{For Lie groups, see 22Exx $\}$ |
| 17B01 | Identities, free Lie (super)algebras |
| 17B05 | Structure theory |
| 17B10 | Representations, algebraic theory (weights) |
| 17B15 | Representations, analytic theory |
| 17B20 | Simple, semisimple, reductive (super)algebras (roots) |
| 17B25 | Exceptional (super)algebras |
| 17B30 | Solvable, nilpotent (super)algebras |
| 17B35 | Universal enveloping (super)algebras [See also 16S30] |
| 17B37 | Quantum groups (quantized enveloping algebras) and related deformations [See also 16W35, 20G42, 81R50, 82B23] |
| 17B40 | Automorphisms, derivations, other operators |
| 17B45 | Lie algebras of linear algebraic groups [See also 14Lxx and 20Gxx] |
| 17B50 | Modular Lie (super)algebras |
| 17B55 | Homological methods in Lie (super)algebras |
| 17B56 | Cohomology of Lie (super)algebras |
| 17B60 | Lie (super)algebras associated with other structures (associative, Jordan, etc.) [See also 16W10, 17C40, 17C50] |
| 17B62 | Lie bialgebras |
| 17B63 | Poisson algebras |
| 17B65 | Infinite-dimensional Lie (super)algebras [See also 22E65] |
| 17B66 | Lie algebras of vector fields and related (super) algebras |
| 17B67 | Kac-Moody (super)algebras (structure and representation theory) |
| 17B68 | Virasoro and related algebras |
| 17B69 | Vertex operators; vertex operator algebras and related structures |
| 17B70 | Graded Lie (super)algebras |
| 17B75 | Color Lie (super)algebras |
| 17B80 | Applications to integrable systems |
| 17B81 | Applications to physics |
| 17B99 | None of the above, but in this section |
| 17Cxx | Jordan algebras (algebras, triples and pairs) |
| 17C05 | Identities and free Jordan structures |
| 17 C 10 | Structure theory |
| 17 C 17 | Radicals |

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17C30
17C36
17C37
17 C 40
17 C 50

17C55
17C60
17C65

17C70
17C90
17C99
17Dxx
17D05
17D10
17D15
17D20
17D25
17D92
17D99
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18Axx
18A05
18A10

18A15

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CATEGORY THEORY; HOMOLOGICAL ALGEBRA \{For commutative rings see 13Dxx, for associative rings 16Exx, for groups 20Jxx, for topological groups and related structures 57Txx; see also 55 Nxx and 55Uxx for algebraic topology
18-00 General reference works (handbooks, dictionaries, bibliographies, etc.)
18-01 Instructional exposition (textbooks, tutorial papers, etc.)
18-02 Research exposition (monographs, survey articles)
18-03 Historical (must also be assigned at least one classification number from Section 01)
18-04 Explicit machine computation and programs (not the theory of computation or programming)
Simple, semisimple algebras
Idempotents, Peirce decompositions
Associated groups, automorphisms
Associated manifolds
Associated geometries
Exceptional Jordan structures
Jordan structures associated with other structures [See also 16W10]
Finite-dimensional structures
Division algebras
Jordan structures on Banach spaces and algebras
[See also 46H70, 46L70]
Super structures
Applications to physics
None of the above, but in this section
Other nonassociative rings and algebras
Alternative rings
Mal'cev (Mal'tsev) rings and algebras
Right alternative rings
$(\gamma, \delta)$-rings, including $(1,-1)$-rings
Lie-admissible algebras
Genetic algebras
None of the above, but in this section

## Proceedings, conferences, collections, etc.

General theory of categories and functors
Definitions, generalizations
Graphs, diagram schemes, precategories [See especially 20L05]
Foundations, relations to logic and deductive systems [See also 03-XX]
Epimorphisms, monomorphisms, special classes of morphisms, null morphisms
Special properties of functors (faithful, full, etc.)
Natural morphisms, dinatural morphisms
Functor categories, comma categories
Limits and colimits (products, sums, directed
limits, pushouts, fiber products, equalizers, kernels, ends and coends, etc.)
Factorization of morphisms, substructures, quotient structures, congruences, amalgams Categories admitting limits (complete categories), functors preserving limits, completions
\(\left.$$
\begin{array}{ll}\text { 18A40 } & \begin{array}{l}\text { Adjoint functors (universal constructions, } \\
\text { reflective subcategories, Kan extensions, etc.) }\end{array} \\
\text { 18A99 } & \begin{array}{l}\text { None of the above, but in this section } \\
\text { 18Bxx }\end{array}
$$ <br>

18pecial categories\end{array}\right]\)| Category of sets, characterizations [See also 03- |
| :--- |
| XX] |

18E40

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18G60

18G99
19-XX
19-00

19-01
19-02
19-03

19-04

19-06
19Axx

19A13
19A15
19A22

19A31
19A49
19A99

18G15 Ext and Tor, generalizations, Künneth formula [See also 55U25]
Torsion theories, radicals [See also 13D30, 16S90]
None of the above, but in this section

## Categories and geometry

Local categories and functors
Grothendieck topologies [See also 14F20]
Abstract manifolds and fiber bundles
[See also 55Rxx, 57Pxx]
Presheaves and sheaves [See also 14F05, 32C35, $32 \mathrm{~L} 10,54 \mathrm{~B} 40,55 \mathrm{~N} 30]$
Algebraic $K$-theory and $L$-theory
[See also 11Exx, 11R70, 11S70, 12-XX, 13D15, 14Cxx, 16E20, 19-XX, 46L80, 57R65, 57R67]
Grothendieck groups [See also 13D15, 16E20, 19Axx]
None of the above, but in this section
Homological algebra [See also 13Dxx, 16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx]
Projectives and injectives [See also 13C10, 13C11, 16D40, 16D50]
Resolutions; derived functors [See also 13D02, 16E05, 18E25]

Homological dimension [See also 13D05, 16E10]
Relative homological algebra, projective classes
Simplicial sets, simplicial objects (in a category) [See also 55U10]
Chain complexes [See also 18E30, 55U15]
Spectral sequences, hypercohomology
[See also 55Txx]
Nonabelian homological algebra
Homotopical algebra
Other (co)homology theories [See also 19D55, 46L80, 58J20, 58J22]
None of the above, but in this section
$K$-THEORY [See also 16E20, 18F25]
General reference works (handbooks, dictionaries, bibliographies, etc.)
Instructional exposition (textbooks, tutorial papers, etc.)
Research exposition (monographs, survey articles)
Historical (must also be assigned at least one classification number from Section 01)
Explicit machine computation and programs (not the theory of computation or programming)
Proceedings, conferences, collections, etc.
Grothendieck groups and $K_{0}$ [See also 13D15, 18F30]
Stability for projective modules [See also 13C10]
Efficient generation
Frobenius induction, Burnside and representation rings
$K_{0}$ of group rings and orders
$K_{0}$ of other rings
None of the above, but in this section

| 19Bxx | Whitehead groups and $K_{1}$ | 19K99 | None of the above, but in this section |
| :---: | :---: | :---: | :---: |
| 19B10 | Stable range conditions | 19Lxx | Topological $K$-theory [See also 55N15, 55R50, |
| 19B14 | Stability for linear groups |  | 55S25] |
| 19B28 | $K_{1}$ of group rings and orders [See also 57Q10] | 19L10 | Riemann-Roch theorems, Chern characters |
| 19B37 | Congruence subgroup problems [See also 20H05] | 19L20 | $J$-homomorphism, Adams operations |
| 19B99 | None of the above, but in this section |  | [See also 55Q50] |
| 19Cxx | Steinberg groups and $K_{2}$ | 19L41 | Connective $K$-theory, cobordism |
| 19C09 | Central extensions and Schur multipliers |  | [See also 55N22] |
| 19 C 20 | Symbols, presentations and stability of $K_{2}$ | 19L47 | Equivariant $K$-theory [See also 55N91, 55P91, |
| 19C30 | $K_{2}$ and the Brauer group |  | 55Q91, 55R91, 55S91] |
| 19 C 40 | Excision for $K_{2}$ | 19L64 | Computations, geometric applications |
| 19C99 | None of the above, but in this section | 19L99 | None of the above, but in this section |
| 19Dxx | Higher algebraic $K$-theory | 19M05 | Miscellaneous applications of $K$-theory |
| 19D06 | $Q$ - and plus-constructions | 20-XX | GROUP THEORY AN |
| 19D10 | Algebraic $K$-theory of spaces |  | GENERALIZATIONS |
| 19D23 | Symmetric monoidal categories [See also 18D10] | 20-00 |  |
| 19D25 | Karoubi-Villamayor-Gersten $K$-theory | 20-00 | bibliographies, etc.) |
| 19D35 | Negative $K$-theory, NK and Nil | 20-01 |  |
| 19D45 | Higher symbols, Milnor $K$-theory |  | papers, etc.) |
| 19D50 | Computations of higher $K$-theory of rings [See also 13D15, 16E20] | 20-02 | Research exposition (monographs, survey articles) |
| 19D55 | $K$-theory and homology; cyclic homology and cohomology [See also 18G60] | 20-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 19D99 | None of the above, but in this section | 20-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 19Exx | $K$-theory in geometry |  |  |
| 19E08 | $K$-theory of schemes [See also 14C35] |  | Proceedings, conferences, collections, etc. |
| 19E15 | Algebraic cycles and motivic cohomology [See also 14C25, 14C35] | 20Ax ${ }^{\text {20A }}$ | Axiomatics and elementary properties |
| 19E20 | Relations with cohomology theories [See also 14 Fxx ] | 20A10 | Metamathematical considerations \{For word problems, see 20F10\} |
| 19E99 | None of the above, but in this section | 20A15 | Applications of logic to group theory |
| 19Fxx | $K$-theory in number theory [See also 11R70, | 20A99 | None of the above, but in this section |
|  | 11S70] | 20Bxx | Permutation groups |
| 19F05 | Generalized class field theory [See also 11G45] | 20B05 | General theory for finite groups |
| 19F15 | Symbols and arithmetic [See also 11R37] | 20B07 | General theory for infinite groups |
| 19F27 | Étale cohomology, higher regulators, zeta and | 20B10 | Characterization theorems |
|  | $L$-functions [See also 11G40, 11R42, 11S40, | 20B15 | Primitive groups |
|  | 14F20, 14G10] | 20B20 | Multiply transitive finite groups |
| 19F99 | None of the above, but in this section | 20B22 | Multiply transitive infinite groups |
| 19Gxx | $K$-theory of forms [See also 11Exx] | 20B25 | Finite automorphism groups of algebraic, |
| 19G05 | Stability for quadratic modules |  | geometric, or combinatorial structures |
| $19 \mathrm{G12}$ | Witt groups of rings [See also 11E81] |  | [See also 05Bxx, 12F10, 20G40, 20H30, 51-XX] |
| 19G24 | $L$-theory of group rings [See also 11E81] | 20B27 | Infinite automorphism groups [See also 12F10] |
| 19G38 | Hermitian $K$-theory, relations with $K$-theory of | 20B30 | Symmetric groups |
|  | rings | 20B35 | Subgroups of symmetric groups |
| 19G99 | None of the above, but in this section | 20B40 | Computational methods |
| 19Jxx | Obstructions from topology | 20B99 | None of the above, but in this section |
| 19 J 05 | Finiteness and other obstructions in $K_{0}$ | 20Cxx | Representation theory of groups |
| 19 J 10 | Whitehead (and related) torsion |  | [See also 19A22 (for representation rings and |
| 19 J 25 | Surgery obstructions [See also 57R67] |  | Burnside rings)] |
| 19 J 35 | Obstructions to group actions | 20C05 | Group rings of finite groups and their modules |
| 19 J 99 | None of the above, but in this section |  | [See also 16S34] |
| 19Kxx | $K$-theory and operator algebras [See mainly 46L80, and also 46M20] | 20C07 | Group rings of infinite groups and their modules [See also 16S34] |
| 19K14 | $K_{0}$ as an ordered group, traces | 20C08 | Hecke algebras and their representations |
| 19K33 | EXT and $K$-homology [See also 55N22] | 20C10 | Integral representations of finite groups |
| 19K35 | Kasparov theory ( $K K$-theory) [See also 58J22] | 20C11 | $p$-adic representations of finite groups |
| 19K56 | Index theory [See also 58J20, 58J22] | 20C12 | Integral representations of infinite groups |


| 20C15 | Ordinary representations and characters |
| :--- | :--- |
| 20C20 | Modular representations and characters |
| 20C25 | Projective representations and multipliers |
| 20C30 | Representations of finite symmetric groups |
| 20C32 | Representations of infinite symmetric groups |
| 20C33 | Representations of finite groups of Lie type |
| 20C34 | Representations of sporadic groups |
| 20C35 | Applications of group representations to physics |
| 20C40 | Computational methods |
| 20C99 | None of the above, but in this section |
| 20Dxx | Abstract finite groups |
| 20D05 | Classification of simple and nonsolvable groups <br> 20D06 |
|  | Simple groups: alternating groups and groups of <br> Lie type [See also 20Gxx] |
| 20D08 | Simple groups: sporadic groups |
| 20D10 | Solvable groups, theory of formations, Schunck <br> classes, Fitting classes, $\pi$-length, ranks |
| [See also 20F17] |  |

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20C99
20Dxx
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20D08
20D10

20D15
20D20 Sylow subgroups, Sylow properties, $\pi$-groups, $\pi$ -
20D25 Special subgroups (Frattini, Fitting, etc.)
20D30 Series and lattices of subgroups
20D35 Subnormal subgroups
20D40 Products of subgroups
20D45 Automorphisms
20D60 Arithmetic and combinatorial problems
20D99 None of the above, but in this section
20Exx Structure and classification of infinite or finite groups
$\begin{array}{ll}20 \mathrm{E} 05 & \text { Free nonabelian groups } \\ 20 \mathrm{E} 06 & \text { Free products, free products with amalgamation, }\end{array}$ Higman-Neumann-Neumann extensions, and generalizations
20E07 Subgroup theorems; subgroup growth
Groups acting on trees [See also 20F65]
20E15 Chains and lattices of subgroups, subnormal subgroups [See also 20F22]
20E18 Limits, profinite groups
20E22 Extensions, wreath products, and other

20E25 Local properties
20E26 Residual properties and generalizations
20E28 Maximal subgroups
20E32 Simple groups [See also 20D05]
General structure theorems
20E36 General theorems concerning automorphisms of groups
Groups with a $B N$-pair; buildings
[See also 51E24]
20E99 None of the above, but in this section
20Fxx Special aspects of infinite or finite groups
20F05 Generators, relations, and presentations
20F06 Cancellation theory; application of van Kampen diagrams [See also 57M05]

20F10

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20G45
20G99

20G30 Linear algebraic groups over global fields and their integers
20G35 Linear algebraic groups over adèles and other rings and schemes
Word problems, other decision problems, connections with logic and automata
[See also 03B25, 03D05, 03D40, 06B25, 08A50, 68Q70]
Commutator calculus
Derived series, central series, and generalizations
Solvable groups, supersolvable groups
[See also 20D10]
Formations of groups, Fitting classes
[See also 20D10]
Nilpotent groups [See also 20D15]
Generalizations of solvable and nilpotent groups
Other classes of groups defined by subgroup chains
FC-groups and their generalizations
Automorphism groups of groups
[See also 20E36]
Representations of groups as automorphism
groups of algebraic systems
Fundamental groups and their automorphisms
[See also 57M05, 57Sxx]
Braid groups; Artin groups
Other groups related to topology or analysis
Associated Lie structures
Engel conditions
Periodic groups; locally finite groups
Reflection and Coxeter groups [See also 22E40, 51F15]
Ordered groups [See mainly 06F15]
Geometric group theory [See also 05C25, 20E08, 57Mxx]
Hyperbolic groups and nonpositively curved groups
Asymptotic properties of groups
None of the above, but in this section
Linear algebraic groups (classical groups)
\{For arithmetic theory, see 11E57, 11H56; for geometric theory, see 14Lxx, 22Exx; for other methods in representation theory, see 15A30, 22E45, 22E46, 22E47, 22E50, 22E55\}
Representation theory
Cohomology theory
Linear algebraic groups over arbitrary fields
Linear algebraic groups over the reals, the complexes, the quaternions
Linear algebraic groups over local fields and their integers

Linear algebraic groups over finite fields
Quantum groups (quantized function algebras) and their representations [See also 16 W 35 , 17B37, 81R50]
Applications to physics
None of the above, but in this section

| 20 Hxx | Other groups of matrices [See also 15A30] | 20M50 | Connections of semigroups with homological |
| :---: | :---: | :---: | :---: |
| 20H05 | Unimodular groups, congruence subgroups |  | algebra and category theory |
|  | [See also 11F06, 19B37, 22E40, 51F20] | 20M99 | None of the above, but in this section |
| 20H10 | Fuchsian groups and their generalizations | 20 Nxx | Other generalizations of groups |
|  | [See also 11F06, 22E40, 30F35, 32Nxx] | 20N02 | Sets with a single binary operation (groupoids) |
| 20H15 | Other geometric groups, including | 20N05 | Loops, quasigroups [See also 05Bxx] |
|  | crystallographic groups [See also 51-XX, especially 51 F 15 , and 82 D 25 ] | 20N10 | Ternary systems (heaps, semiheaps, heapoids, etc.) |
| 20H20 | Other matrix groups over fields | 20N15 | $n$-ary systems ( $n \geq 3$ ) |
| 20H25 | Other matrix groups over rings | 20N20 | Hypergroups |
| 20H30 | Other matrix groups over finite fields | 20N25 | Fuzzy groups [See also 03E72] |
| 20H99 | None of the above, but in this section | 20N99 | None of the above, but in this section |
| 20Jxx | Connections with homological algebra and category theory | 20P05 | Probabilistic methods in group theory [See also 60Bxx] |
| 20 J 05 | Homological methods in group theory |  |  |
| 20 J06 | Cohomology of groups | 22-XX | TOPOLOGICAL GROUPS, LIE GROUPS |
| 20J15 | Category of groups |  | \{For transformation groups, see 54H15, 57Sxx, |
| 20 J 99 | None of the above, but in this section |  | 58-XX. For abstract harmonic analysis, see 43-XX $\}$ |
| 20Kxx | Abelian groups |  | $\text { 43-XX }\}$ |
| 20K01 | Finite abelian groups | 22-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 20K10 | Torsion groups, primary groups and generalized primary groups | 22-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 20K15 | Torsion-free groups, finite rank Torsion-free groups, infinite rank | 22-02 | Research exposition (monographs, survey articles) |
| 20K20 | Torsion-free groups, infinite rank Mixed groups | 22-03 | Historical (must also be assigned at least one |
| 20K25 | Direct sums, direct products, etc. |  | classificatio |
| 20K27 | Subgroups | 22-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 20K30 | Automorphisms, homomorphisms, endomorphisms, etc. | 22-06 | the theory of computation or programming) Proceedings, conferences, collections, etc. |
| 20K35 | Extensions | 22 Axx | Topological and differentiable algebraic |
| 20K40 | Homological and categorical methods |  | systems $\{$ For topological rings and fields, see 12Jxx, 13Jxx, 16W80\} |
| 20K45 | Topological methods [See also 22A05, 22B05] | 22A05 | 12Jxx, ${ }^{\text {S }}$ Structure of general topological groups |
| 20K99 | None of the above, but in this section | 22 A 05 | Structure of general topological groups Analysis on general topological groups |
| 20L05 | Groupoids (i.e. small categories in which all morphisms are isomorphisms) \{For sets with | 22A10 | Analysis on general topological groups Structure of topological semigroups |
|  | a single binary operation, see 20N02; for | 22A20 | Analysis on topological semigroups |
|  | topological groupoids, see $22 \mathrm{~A} 22,58 \mathrm{H05}\}$ | 22A22 | Topological groupoids (including differentiable |
| 20 Mxx | Semigroups |  | and Lie groupoids) [See also 58 |
| 20M05 | Free semigroups, generators and relations, word problems | 22A25 | Representations of general topological groups and semigroups |
| 20M07 | Varieties of semigroups | 22A26 | Topological semilattices, lattices and applications |
| 20M10 | General structure theory |  | [See also 06B30, 06B35, 06F30] . |
| 20M11 | Radical theory | 22A30 | Other topological algebraic systems and their |
| 20M12 | Ideal theory |  | representations |
| 20M14 | Commutative semigroups | 22A99 | None of the above, but in this section |
| 20M15 | Mappings of semigroups | 22Bxx | Locally compact abelian groups (LCA groups) |
| 20M17 | Regular semigroups | 22B05 | General properties and structure of LCA groups |
| 20M18 | Inverse semigroups | 22B10 | Structure of group algebras of LCA groups |
| 20M19 | Orthodox semigroups | 22B99 | None of the above, but in this section |
| 20M20 | Semigroups of transformations, etc. | $22 \mathrm{C05}$ | Compact groups |
|  | [See also 47D03, 47H20, 54H15] | 22Dxx | Locally compact groups and their algebras |
| 20M25 | Semigroup rings, multiplicative semigroups of rings [See also 16S36, 16Y60] | 22D05 | General properties and structure of locally compact groups |
| 20M30 | Representation of semigroups; actions of | 22D10 | Unitary representations of locally compact groups |
|  | semigroups on sets | 22D12 | Other representations of locally compact groups |
| 20M35 | Semigroups in automata theory, linguistics, etc. | 22D15 | Group algebras of locally compact groups |
|  | [See also 03D05, 68Q70, 68T50] | 22D20 | Representations of group algebras |

$\left.\begin{array}{ll}\text { 22D25 } & \begin{array}{l}C^{*} \text {-algebras and } W^{*} \text {-algebras in relation to group } \\ \text { representations [See also 46Lxx] }\end{array} \\ \text { 22D30 } & \text { Induced representations } \\ \text { 22D35 } & \text { Duality theorems } \\ \text { 22D40 } & \begin{array}{l}\text { Ergodic theory on groups [See also 28Dxx] }\end{array} \\ \text { 22D45 } & \text { Automorphism groups of locally compact groups } \\ \text { 22D99 } & \begin{array}{l}\text { None of the above, but in this section } \\ \text { Lie groups \{For the topology of Lie groups } \\ \text { and homogeneous spaces, see 57Sxx, 57Txx; }\end{array} \\ \text { 22Exx } \\ \text { for analysis thereon, see 43A80, 43A85, 43A90\} }\end{array}\right\}$

22F30

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26A16
26A18 Iteration [See also 37Bxx, 37Cxx, 37Exx, 39B12, 47H10, 54H25]
26A21 Classification of real functions; Baire classification of sets and functions
[See also 03E15, 28A05, 54C50]
26A24 Differentiation (functions of one variable): general theory, generalized derivatives, meanvalue theorems [See also 28A15]
26A27 Nondifferentiability (nondifferentiable functions, points of nondifferentiability), discontinuous derivatives
26A30 Singular functions, Cantor functions, functions with other special properties
26A33 Fractional derivatives and integrals
26A36 Antidifferentiation
26A39 Denjoy and Perron integrals, other special integrals
26A42 Integrals of Riemann, Stieltjes and Lebesgue type [See also 28-XX]
26A45 Functions of bounded variation, generalizations
26A46 Absolutely continuous functions
26A48 Monotonic functions, generalizations
26A51 Convexity, generalizations
26A99 None of the above, but in this section
26Bxx Functions of several variables
26B05
26B10
Homogeneous spaces \{For general actions on manifolds or preserving geometrical structures, see 57M60, 57Sxx; for discrete subgroups of Lie groups see especially 22 E 40$\}$
Groups as automorphisms of other structures
REAL FUNCTIONS [See also 54C30]
General reference works (handbooks, dictionaries, bibliographies, etc.)
Instructional exposition (textbooks, tutorial papers, etc.)
Research exposition (monographs, survey articles)
Historical (must also be assigned at least one classification number from Section 01)
Explicit machine computation and programs (not the theory of computation or programming)
Proceedings, conferences, collections, etc.
Functions of one variable
Foundations: limits and generalizations, elementary topology of the line
One-variable calculus
Elementary functions
Rate of growth of functions, orders of infinity, slowly varying functions [See also 26A48]
Continuity and related questions (modulus of continuity, semicontinuity, discontinuities, etc.) \{For properties determined by Fourier coefficients, see 42A16; for those determined by approximation properties, see 41A25, 41A27\}
Lipschitz (Hölder) classes
26A21

26A36

Continuity and differentiation questions
Implicit function theorems, Jacobians,
transformations with several variables

| 26B12 | Calculus of vector functions | 28-03 |
| :---: | :---: | :---: |
| 26B15 | Integration: length, area, volume [See also 28A75, 51M25] | 28-04 |
| 26B20 | Integral formulas (Stokes, Gauss, Green, etc.) |  |
| 26B25 | Convexity, generalizations | 28-06 |
| 26B30 | Absolutely continuous functions, functions of bounded variation | $\begin{aligned} & \mathbf{2 8 A x x} \\ & 28 \mathrm{~A} 05 \end{aligned}$ |
| 26B35 | Special properties of functions of several variables, Hölder conditions, etc. |  |
| 26B40 | Representation and superposition of functions | 28A10 |
| 26B99 | None of the above, but in this section | 28A12 |
| 26Cxx | Polynomials, rational functions | 28A15 |
| 26C05 | Polynomials: analytic properties, etc. [See also 12Dxx, 12Exx] | 28A20 |
| 26C10 | Polynomials: location of zeros [See also 12D10, 30C15, 65H05] | 28 |
| 26 C 15 | Rational functions [See also 14Pxx] | 28 A |
| 26C99 | None of the above, but in this section | 28A33 |
| 26Dxx | Inequalities \{For maximal function inequalities, see 42B25; for functional inequalities, see 39B72; for probabilistic inequalities, see 60 E 15$\}$ | 28A33 28A35 28A50 28A51 |
| 26D05 | Inequalities for trigonometric functions and polynomials | 28A60 |
| 26D07 | Inequalities involving other types of functions | 28A75 |
| 26D10 | Inequalities involving derivatives and differential and integral operators | 28A78 |
| 26D15 | Inequalities for sums, series and integrals | 28A80 |
| 26D20 | Other analytical inequalities | 28A99 |
| 26D99 | None of the above, but in this section | 28Bxx |
| 26Exx | Miscellaneous topics [See also 58Cxx] |  |
| 26E05 | Real-analytic functions [See also 32B05, 32C05] | 28B05 |
| 26E10 | $C^{\infty}$-functions, quasi-analytic functions [See also 58C25] | 28B10 |
| 26E15 | Calculus of functions on infinite-dimensional spaces [See also 46G05, 58Cxx] | 28B15 |
| 26E20 | Calculus of functions taking values in infinitedimensional spaces [See also 46E40, 46G10, 58Cxx] | 28B20 |
| 26E25 | Set-valued functions [See also 28B20, 54C60] \{For nonsmooth analysis, see 49J52, 58Cxx, 90Cxx $\}$ | $\begin{aligned} & \text { 28B99 } \\ & \mathbf{2 8 C x} \end{aligned}$ |
| 26E30 | Non-Archimedean analysis [See also 12J25] |  |
| 26E35 | Nonstandard analysis [See also 03H05, 28E05, 54J05] | 28C05 |
| 26E40 | Constructive real analysis [See also 03F60] |  |
| 26E50 | Fuzzy real analysis [See also 03E72, 28E10] | $28 \mathrm{C10}$ |
| 26E60 | Means [See also 47A64] | 28 C 10 |
| 26E99 | None of the above, but in this section |  |
| 28-XX | MEASURE AND INTEGRATION \{For analysis on manifolds, see 58-XX $\}$ | 28C15 |
| 28-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) | 28C20 |
| 28-01 | Instructional exposition (textbooks, tutorial papers, etc.) |  |
| 28-02 | Research exposition (monographs, survey articles) | 28C99 |

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26C99
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26D05

26D07
26D10

26D15
26D20
26D99
26Exx
26E05
26E10

26E15

26E20

26E25

26E30
26E35 Nonstandard analysis [See also 03H05, 28E05, 54J05]
26E40 Constructive real analysis [See also 03F60]
Fuzzy real analysis [See also 03E72, 28E10]
26E99

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28-XX MEASURE AND INTEGRATION \{For analysis on manifolds, see 58-XX \(\}\) bibliographies, etc.) papers, etc.)
Research exposition (monographs, survey articles)
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28A75

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28A80
28A99
28Bxx

28B05
28B10

28B15

28 C 15

28C20

28C99

28B20 Set-valued set functions and measures; integration of set-valued functions; measurable selections
[See also 26E25, 54C60, 54C65, 91B14]
None of the above, but in this section
Set functions and measures on spaces with additional structure [See also 46G12, 58C35, 58D20]
Integration theory via linear functionals (Radon measures, Daniell integrals, etc.), representing set functions and measures
Set functions and measures on topological groups, Haar measures, invariant measures [See also 22Axx, 43A05]
Historical (must also be assigned at least one classification number from Section 01)
Explicit machine computation and programs (not the theory of computation or programming)
Proceedings, conferences, collections, etc.
Classical measure theory
Classes of sets (Borel fields, $\sigma$-rings, etc.), measurable sets, Suslin sets, analytic sets
[See also 03E15, 26A21, 54H05]
Real- or complex-valued set functions
Contents, measures, outer measures, capacities
Abstract differentiation theory, differentiation of set functions [See also 26A24]
Measurable and nonmeasurable functions, sequences of measurable functions, modes of convergence
Integration with respect to measures and other set functions
Spaces of measures, convergence of measures [See also 46E27, 60Bxx]
Measures and integrals in product spaces
Integration and disintegration of measures
Lifting theory [See also 46G15]
Measures on Boolean rings, measure algebras [See also 54H10]
Length, area, volume, other geometric measure theory [See also 26B15, 49Q15]
Hausdorff and packing measures
Fractals [See also 37Fxx]
None of the above, but in this section
Set functions, measures and integrals with values in abstract spaces
Vector-valued set functions, measures and integrals [See also 46G10]
Group- or semigroup-valued set functions, measures and integrals
Set functions, measures and integrals with values in ordered spaces

Set functions and measures on topological spaces (regularity of measures, etc.)
Set functions and measures and integrals in infinite-dimensional spaces (Wiener measure, Gaussian measure, etc.) [See also 46G12, 58C35, 58D20, 60B11]
None of the above, but in this section

| 28Dxx | Measure-theoretic ergodic theory [See also 11K50, 11K55, 22D40, 37Axx, 47A35, 54H20, 60Fxx, 60G10] |
| :---: | :---: |
| 28D05 | Measure-preserving transformations |
| 28D10 | One-parameter continuous families of measurepreserving transformations |
| 28D15 | General groups of measure-preserving transformations |
| 28D20 | Entropy and other invariants |
| 28D99 | None of the above, but in this section |
| 28Exx | Miscellaneous topics in measure theory |
| 28E05 | Nonstandard measure theory [See also 03H05, 26E35] |
| 28E10 | Fuzzy measure theory [See also 03E72, 26E50, 94D05] |
| 28E15 | Other connections with logic and set theory |
| 28E99 | None of the above, but in this section |
| 30-XX | FUNCTIONS OF A COMPLEX VARIABLE \{For analysis on manifolds, see 58-XX\} |
| 30-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 30-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 30-02 | Research exposition (monographs, survey articles) |
| 30-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 30-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 30-06 | Proceedings, conferences, collections, etc. |
| 30Axx | General properties |
| 30A05 | Monogenic properties of complex functions (including polygenic and areolar monogenic functions) |
| 30A10 | Inequalities in the complex domain |
| 30A99 | None of the above, but in this section |
| 30Bxx | Series expansions |
| 30B10 | Power series (including lacunary series) |
| 30B20 | Random power series |
| 30B30 | Boundary behavior of power series, overconvergence |
| 30B40 | Analytic continuation |
| 30B50 | Dirichlet series and other series expansions, exponential series [See also $11 \mathrm{M} 41,42-\mathrm{XX}$ ] |
| 30B60 | Completeness problems, closure of a system of functions |
| 30B70 | Continued fractions [See also 11A55, 40A15] |
| 30B99 | None of the above, but in this section |
| 30Cxx | Geometric function theory |
| 30C10 | Polynomials |
| 30C15 | Zeros of polynomials, rational functions, and other analytic functions (e.g. zeros of functions with bounded Dirichlet integral) \{For algebraic theory, see 12D10; for real methods, see 26 C 10$\}$ |
| 30C20 | Conformal mappings of special domains |
| 30C25 | Covering theorems in conformal mapping theory |
| 30C30 | Numerical methods in conformal mapping theory [See also 65E05] |

30C35
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30C75
30C80

30C85

30C99
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30D45
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30D55
30D60
30D99
30Exx

30E05
30E10
30E15

30E20

30E25
30E99
30Fxx
30F10

30F15
30F20

30D15 Special classes of entire functions and growth
estimates
General theory of conformal mappings
Kernel functions and applications
Special classes of univalent and multivalent functions (starlike, convex, bounded rotation, etc.)
Coefficient problems for univalent and multivalent functions
General theory of univalent and multivalent functions
Quasiconformal mappings in the plane
Quasiconformal mappings in $\mathbf{R}^{n}$, other generalizations
Extremal problems for conformal and quasiconformal mappings, variational methods
Extremal problems for conformal and quasiconformal mappings, other methods Maximum principle; Schwarz's lemma, Lindelöf principle, analogues and generalizations; subordination
Capacity and harmonic measure in the complex plane [See also 31A15]
None of the above, but in this section
Entire and meromorphic functions, and related topics
Functional equations in the complex domain, iteration and composition of analytic functions
[See also 34Mxx, 37Fxx, 39-XX]
Representations of entire functions by series and integrals

Entire functions, general theory
Meromorphic functions, general theory
Distribution of values, Nevanlinna theory
Cluster sets, prime ends, boundary behavior
Bloch functions, normal functions, normal families
Blaschke products, bounded mean oscillation, bounded characteristic, bounded functions, functions with positive real part
$H^{p}$-classes
Quasi-analytic and other classes of functions
None of the above, but in this section
Miscellaneous topics of analysis in the complex domain
Moment problems, interpolation problems
Approximation in the complex domain
Asymptotic representations in the complex domain
Integration, integrals of Cauchy type, integral representations of analytic functions
[See also 45Exx]
Boundary value problems [See also 45Exx]
None of the above, but in this section
Riemann surfaces
Compact Riemann surfaces and uniformization [See also 14H15, 32G15]
Harmonic functions on Riemann surfaces
Classification theory of Riemann surfaces

| 30F25 | Ideal boundary theory |
| :---: | :---: |
| 30F30 | Differentials on Riemann surfaces |
| 30F35 | Fuchsian groups and automorphic functions [See also 11Fxx, 20H10, 22E40, 32Gxx, 32Nxx] |
| 30F40 | Kleinian groups [See also 20H10] |
| 30F45 | Conformal metrics (hyperbolic, Poincaré, distance functions) |
| 30F50 | Klein surfaces |
| 30F60 | Teichmüller theory [See also 32G15] |
| 30 F 99 | None of the above, but in this section |
| 30Gxx | Generalized function theory |
| 30G06 | Non-Archimedean function theory [See also 12J25]; nonstandard function theory [See also 03H05] |
| 30G12 | Finely holomorphic functions and topological function theory |
| 30G20 | Generalizations of Bers or Vekua type (pseudoanalytic, $p$-analytic, etc.) |
| 30G25 | Discrete analytic functions |
| 30G30 | Other generalizations of analytic functions (including abstract-valued functions) |
| 30G35 | Functions of hypercomplex variables and generalized variables |
| 30G99 | None of the above, but in this section |
| 30H05 | Spaces and algebras of analytic functions [See also 32A38, 46Exx, 46J15] |
| 31-XX | POTENTIAL THEORY \{For probabilistic potential theory, see $\mathbf{6 0 J 4 5}\}$ |
| 31-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 31-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 31-02 | Research exposition (monographs, survey articles) |
| 31-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 31-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 31-06 | Proceedings, conferences, collections, etc. |
| 31Axx | Two-dimensional theory |
| 31 A 05 | Harmonic, subharmonic, superharmonic functions |
| 31 A 10 | Integral representations, integral operators, integral equations methods |
| 31 A 15 | Potentials and capacity, harmonic measure, extremal length [See also 30C85] |
| 31 A 20 | Boundary behavior (theorems of Fatou type, etc.) |
| 31 A 25 | Boundary value and inverse problems |
| 31 A 30 | Biharmonic, polyharmonic functions and equations, Poisson's equation |
| 31 A35 | Connections with differential equations |
| 31A99 | None of the above, but in this section |
| 31Bxx | Higher-dimensional theory |
| 31B05 | Harmonic, subharmonic, superharmonic functions |
| 31B10 | Integral representations, integral operators, integral equations methods |
| 31B15 | Potentials and capacities, extremal length |
| 31B20 | Boundary value and inverse problems |
| 31B25 | Boundary behavior |

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31B99
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31 C 10
31 C 12

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31 C 20
31 C 25
31C35
31C40
31C45

31C99
31D05
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32-01

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32-03

32-04

32-06
32Axx

32A05
32A07

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32A22 Nevanlinna theory (local); growth estimates; other inequalities \{For geometric theory, see 32H25, 32H30 \}
32A25 Integral representations; canonical kernels (Szegő, Bergman, etc.)
32A26 Integral representations, constructed kernels (e.g. Cauchy, Fantappiè-type kernels)
32A27 Local theory of residues [See also 32C30]
32A30 Other generalizations of function theory of one complex variable (should also be assigned at least one classification number from Section 30) \{For functions of several hypercomplex variables, see 30G35\}

| 32A35 | $H^{p}$-spaces, Nevanlinna spaces [See also 32M15, | 32D20 | Removable singularities |
| :---: | :---: | :---: | :---: |
|  | 42B30, 43A85, 46J15] | 32D26 | Riemann domains |
| 32A36 | Bergman spaces | 32D99 | None of the above, but in this section |
| 32A37 | Other spaces of holomorphic functions (e.g. | 32Exx | Holomorphic convexity |
|  | bounded mean oscillation (BMOA), vanishing mean oscillation (VMOA)) [See also 46Exx] | 32E05 | Holomorphically convex complex spaces, reduction theory |
| 32A38 | Algebras of holomorphic functions | 32E10 | Stein spaces, Stein manifolds |
|  | [See also 30H05, 46J10, 46J15] | 32E20 | Polynomial convexity |
| 32A40 | Boundary behavior of holomorphic functions | 32E30 | Holomorphic and polynomial approximation, |
| 32A45 | Hyperfunctions [See also 46F15] |  | Runge pairs, interpolation |
| 32A50 | Harmonic analysis of several complex variables [See mainly 43-XX] | 32E35 | Global boundary behavior of holomorphic functions |
| 32A55 | Singular integrals | 32E40 | The Levi problem |
| 32A60 | Zero sets of holomorphic functions | 32E99 | None of the above, but in this section |
| 32A65 | Banach algebra techniques [See mainly 46Jxx] | 32Fxx | Geometric convexity |
| 32A70 | Functional analysis techniques | 32F10 | $q$-convexity, $q$-concavity |
|  | [See mainly 46Exx] | 32F17 | Other notions of convexity |
| 32A99 | None of the above, but in this section | 32F18 | Finite-type conditions |
| 32Bxx | Local analytic geometry [See also 13-XX and | 32F27 | Topological consequences of geometric convexity |
|  | 14-XX] | 32F32 | Analytical consequences of geometric convexity |
| 32B05 | Analytic algebras and generalizations, preparation theorems | 32F45 | (vanishing theorems, etc.) <br> Invariant metrics and pseudodistances |
| 32B10 | Germs of analytic sets, local parametrization | 32F99 | None of the above, but in this section |
| 32B15 | Analytic subsets of affine space | 32Gxx | Deformations of analytic structures |
| 32B20 | Semi-analytic sets and subanalytic sets [See also 14P15] | 32G05 | Deformations of complex structures [See also 13D10, 16S80, 58H10, 58H15] |
| 32B25 | Triangulation and related questions | 32G07 | Deformations of special (e.g. CR) structures |
| 32B99 | None of the above, but in this section | 32G08 | Deformations of fiber bundles |
| 32 Cxx | Analytic spaces | 32G10 | Deformations of submanifolds and subspaces |
| 32C05 | Real-analytic manifolds, real-analytic spaces [See also 14Pxx, 58A07] | 32G13 | Analytic moduli problems \{For algebraic moduli problems, see 14D20, 14D22, 14H10, 14J10 \} |
| 32C07 | Real-analytic sets, complex Nash functions |  | [See also 14H15, 14J15] |
|  | [See also 14P15, 14P20] | 32G15 | Moduli of Riemann surfaces, Teichmüller theory |
| 32C09 | Embedding of real analytic manifolds |  | [See also 14H15, 30Fxx] |
| 32 C 11 | Complex supergeometry [See also 14A22, 14M30, 58A50] | 32G20 | Period matrices, variation of Hodge structure; degenerations [See also 14D05, 14D07, 14K30] |
| 32 C 15 | Complex spaces | 32G34 | Moduli and deformations for ordinary differential |
| 32 C 18 | Topology of analytic spaces |  | equations (e.g. Khnizhnik-Zamolodchikov |
| 32 C 20 | Normal analytic spaces |  | equation) [See also 34Mxx] |
| 32 C 22 | Embedding of analytic spaces | 32G81 | Applications to physics |
| 32 C 25 | Analytic subsets and submanifolds | 32G99 | None of the above, but in this section |
| 32C30 | Integration on analytic sets and spaces, currents | 32Hxx | Holomorphic mappings and correspondences |
|  | \{For local theory, see 32A25 or 32A27\} | 32H02 | Holomorphic mappings, (holomorphic) |
| 32C35 | Analytic sheaves and cohomology groups |  | embeddings and related questions |
|  | [See also 14Fxx, 18F20, 55N30] | 32H04 | Meromorphic mappings |
| 32C36 | Local cohomology of analytic spaces | 32 H 12 | Boundary uniqueness of mappings |
| 32 C 37 | Duality theorems | 32 H 25 | Picard-type theorems and generalizations \{For |
| 32C38 | Sheaves of differential operators and their modules, $D$-modules [See also $14 \mathrm{~F} 10,16 \mathrm{~S} 32$, 35A27, 58J15] | 32H30 | function-theoretic properties, see 32A22\} <br> Value distribution theory in higher dimensions <br> \{For function-theoretic properties, see 32A22\} |
| 32C55 | The Levi problem in complex spaces; generalizations | $\begin{aligned} & 32 \mathrm{H} 35 \\ & 32 \mathrm{H} 40 \end{aligned}$ | Proper mappings, finiteness theorems Boundary regularity of mappings |
| 32 C 81 | Applications to physics | 32H50 | Iteration problems |
| 32C99 | None of the above, but in this section | 32H99 | None of the above, but in this section |
| 32Dxx | Analytic continuation | 32Jxx | Compact analytic spaces \{For Riemann |
| 32D05 | Domains of holomorphy |  | surfaces, see 14Hxx, 30Fxx; for algebraic |
| 32D10 | Envelopes of holomorphy |  | theory, see 14Jxx |
| 32D15 | Continuation of analytic objects | 32J05 | Compactification of analytic spaces |


| 32J10 | Algebraic dependence theorems |
| :---: | :---: |
| 32J15 | Compact surfaces |
| 32J17 | Compact 3-folds |
| 32J18 | Compact $n$-folds |
| 32J25 | Transcendental methods of algebraic geometry [See also 14C30] |
| 32J27 | Compact Kähler manifolds: generalizations, classification |
| 32J81 | Applications to physics |
| 32J99 | None of the above, but in this section |
| 32Kxx | Generalizations of analytic spaces (should also be assigned at least one other classification number from Section 32 describing the type of problem) |
| 32 K 05 | Banach analytic spaces [See also 58Bxx] |
| 32K07 | Formal and graded complex spaces [See also 58C50] |
| 32K15 | Differentiable functions on analytic spaces, differentiable spaces [See also 58C25] |
| 32K99 | None of the above, but in this section |
| 32Lxx | Holomorphic fiber spaces [See also 55Rxx] |
| 32L05 | Holomorphic bundles and generalizations |
| 32L10 | Sheaves and cohomology of sections of holomorphic vector bundles, general results [See also 14F05, 18F20, 55N30] |
| 32L15 | Bundle convexity [See also 32F10] |
| 32L20 | Vanishing theorems |
| 32L25 | Twistor theory, double fibrations [See also 53C28] |
| 32L81 | Applications to physics |
| 32L99 | None of the above, but in this section |
| 32Mxx | Complex spaces with a group of automorphisms |
| 32 M 05 | Complex Lie groups, automorphism groups acting on complex spaces [See also 22E10] |
| 32M10 | Homogeneous complex manifolds [See also 14M17, 57T15] |
| 32M12 | Almost homogeneous manifolds and spaces [See also 14M17] |
| 32M15 | Hermitian symmetric spaces, bounded symmetric domains, Jordan algebras [See also 22E10, 22E40, 53C35, 57T15] |
| 32M17 | Automorphism groups of $\mathbf{C}^{n}$ and affine manifolds |
| 32M25 | Complex vector fields |
| 32M99 | None of the above, but in this section |
| 32Nxx | Automorphic functions [See also 11Fxx, 20H10, 22E40, 30F35] |
| 32N05 | General theory of automorphic functions of several complex variables |
| 32N10 | Automorphic forms |
| 32N15 | Automorphic functions in symmetric domains |
| 32N99 | None of the above, but in this section |
| 32P05 | Non-Archimedean complex analysis (should also be assigned at least one other classification number from Section 32 describing the type of problem) |

32Qxx
32Q05
32Q10
32Q15
32Q20
32Q25
32Q28
32Q30
32Q35
32Q40
32Q45
32Q55
32Q57
32Q60
32Q65
32Q99
32Sxx
32S05
32S10
32S15
32S20
32S22
32S25
32S30

32S35

32 S 40

32S45
32S50
32S55
32S60
32S65

32S70
32S99
32Txx
32 T 05
32 T 15
32 T 20
32 T 25
32 T 27

32 T 35
32 T 40
32 T 99

## Complex manifolds

Negative curvature manifolds
Positive curvature manifolds
Kähler manifolds
Kähler-Einstein manifolds [See also 53Cxx]
Calabi-Yau theory
Stein manifolds
Uniformization
Complex manifolds as subdomains of Euclidean space
Embedding theorems
Hyperbolic and Kobayashi hyperbolic manifolds
Topological aspects of complex manifolds
Classification theorems
Almost complex manifolds
Pseudoholomorphic curves
None of the above, but in this section
Singularities [See also 58Kxx]
Local singularities [See also 14J17]
Invariants of analytic local rings
Equisingularity (topological and analytic)
[See also 14E15]
Global theory of singularities; cohomological properties [See also 14E15]
Relations with arrangements of hyperplanes [See also 52C35]
Surface and hypersurface singularities [See also 14J17]
Deformations of singularities; vanishing cycles [See also 14B07]
Mixed Hodge theory of singular varieties [See also 14C30, 14D07]
Monodromy; relations with differential equations and $D$-modules
Modifications; resolution of singularities [See also 14E15]
Topological aspects: Lefschetz theorems, topological classification, invariants
Milnor fibration; relations with knot theory [See also 57M25, 57Q45]
Stratifications; constructible sheaves; intersection cohomology [See also 58Kxx]
Singularities of holomorphic vector fields and foliations
Other operations on singularities
None of the above, but in this section
Pseudoconvex domains
Domains of holomorphy
Strongly pseudoconvex domains
Worm domains
Finite type domains
Geometric and analytic invariants on weakly
pseudoconvex boundaries
Exhaustion functions
Peak functions
None of the above, but in this section

| 32Uxx | Pluripotential theory |
| :---: | :---: |
| 32U05 | Plurisubharmonic functions and generalizations [See also 31C10] |
| 32U10 | Plurisubharmonic exhaustion functions |
| 32U15 | General pluripotential theory |
| 32U20 | Capacity theory and generalizations |
| 32U25 | Lelong numbers |
| 32U30 | Removable sets |
| 32U35 | Pluricomplex Green functions |
| 32U40 | Currents |
| 32U99 | None of the above, but in this section |
| 32Vxx | CR manifolds |
| 32 V 05 | CR structures, CR operators, and generalizations |
| 32 V 10 | CR functions |
| 32 V 15 | CR manifolds as boundaries of domains |
| 32 V 20 | Analysis on CR manifolds |
| 32 V 25 | Extension of functions and other analytic objects from CR manifolds |
| 32 V 30 | Embeddings of CR manifolds |
| 32 V 35 | Finite type conditions on CR manifolds |
| 32V40 | Real submanifolds in complex manifolds |
| 32 V 99 | None of the above, but in this section |
| 32Wxx | Differential operators in several variables |
| 32W05 | $\bar{\partial}$ and $\bar{\partial}$-Neumann operators |
| 32 W 10 | $\bar{\partial}_{b}$ and $\bar{\partial}_{b}$-Neumann operators |
| 32W20 | Complex Monge-Ampère operators |
| 32W25 | Pseudodifferential operators in several complex variables |
| 32W30 | Heat kernels in several complex variables |
| 32W50 | Other partial differential equations of complex analysis |
| 32W99 | None of the above, but in this section |
| 33-XX | SPECIAL FUNCTIONS (33-XX deals with the properties of functions as functions) $\{$ For orthogonal functions, see 42 Cxx ; for aspects of combinatorics see 05 Axx ; for number-theoretic aspects see $11-X X$; for representation theory see 22Exx $\}$ |
| 33-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 33-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 33-02 | Research exposition (monographs, survey articles) |
| 33-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 33-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 33-06 | Proceedings, conferences, collections, etc. |
| 33Bxx | Elementary classical functions |
| 33B10 | Exponential and trigonometric functions |
| 33B15 | Gamma, beta and polygamma functions |
| 33B20 | Incomplete beta and gamma functions (error functions, probability integral, Fresnel integrals) |
| 33B30 | Higher logarithm functions |
| 33B99 | None of the above, but in this section |
| 33Cxx | Hypergeometric functions |
| 33 C 05 | Classical hypergeometric functions, ${ }_{2} F_{1}$ |

33 C 10
33 C 15
33 C 20
33C45

33 C 47

33 C 50

33C52

33C55
33C60

33C65
33C67

33C70
33C75
33C80

33C90
33C99
33Dxx
33D05
33D15
33D45

33D50

33D52

33D60
33D65

33D70
33D80

33D90
33D99
33Exx
33E05
33E10
33 E 12
33E15
33 E 17

33D67 Basic hypergeometric functions associated with root systems
Bessel and Airy functions, cylinder functions, ${ }_{0} F_{1}$
Confluent hypergeometric functions, Whittaker functions, ${ }_{1} F_{1}$
Generalized hypergeometric series, ${ }_{p} F_{q}$
Orthogonal polynomials and functions of hypergeometric type (Jacobi, Laguerre, Hermite, Askey scheme, etc.) [See also 42C05 for general orthogonal polynomials and functions]
Other special orthogonal polynomials and functions
Orthogonal polynomials and functions in several variables expressible in terms of special functions in one variable
Orthogonal polynomials and functions associated with root systems
Spherical harmonics
Hypergeometric integrals and functions defined by them ( $E, G$ and $H$ functions)
Appell, Horn and Lauricella functions
Hypergeometric functions associated with root systems
Other hypergeometric functions and integrals in several variables
Elliptic integrals as hypergeometric functions
Connections with groups and algebras, and related topics
Applications
None of the above, but in this section
Basic hypergeometric functions
$q$-gamma functions, $q$-beta functions and integrals
Basic hypergeometric functions in one variable,
${ }_{r} \varphi_{s}$
Basic orthogonal polynomials and functions
(Askey-Wilson polynomials, etc.)
Orthogonal polynomials and functions in several variables expressible in terms of basic hypergeometric functions in one variable
Basic orthogonal polynomials and functions associated with root systems (Macdonald polynomials, etc.)
Basic hypergeometric integrals and functions defined by them
Bibasic functions and multiple bases

Other basic hypergeometric functions and integrals in several variables
Connections with quantum groups, Chevalley
groups, $p$-adic groups, Hecke algebras, and
related topics
Applications
None of the above, but in this section
Other special functions
Elliptic functions and integrals
Lamé, Mathieu, and spheroidal wave functions
Mittag-Leffler functions and generalizations
Other wave functions
Painlevé-type functions
\(\left.$$
\begin{array}{ll}\text { 33E20 } & \text { Other functions defined by series and integrals } \\
\text { 33E30 } & \begin{array}{l}\text { Other functions coming from differential, } \\
\text { difference and integral equations }\end{array} \\
\text { 33E50 } & \begin{array}{l}\text { Special functions in characteristic } p \text { (gamma } \\
\text { functions, etc.) }\end{array} \\
\text { 33E99 } & \text { None of the above, but in this section } \\
\text { 33Fxx } & \text { Computational aspects } \\
\text { 33F05 } & \text { Numerical approximation [See also 65D20] } \\
\text { 33F10 } & \begin{array}{l}\text { Symbolic computation (Gosper and Zeilberger } \\
\text { algorithms, etc.) [See also 68W30] }\end{array}
$$ <br>

33F99 \& None of the above, but in this section\end{array}\right\}\)| 34-XX | ORDINARY DIFFERENTIAL EQUATIONS |
| :--- | :--- |
| 34-00 | General reference works (handbooks, dictionaries, <br> bibliographies, etc.) |
| 34-01 | Instructional exposition (textbooks, tutorial |
| papers, etc.) |  |

33 E 30

33E50

33E99
33Fxx
33F05
33F10
33F99

- $\mathbf{X X}$

34-01

34-02
34-03
34-04

34-06
34Axx
34A05
Explicit solutions and reductions [See also 65L80] continuous dependence and continuation of solutions
transforms, operational calculus, etc.
[See also 44-XX]
34A26
34A30
34A34
34A36
34A37
34A40
34A45

34A55 Inverse problems
34A60 Differential inclusions [See also 49J24, 49K24]
34A99 None of the above, but in this section
34Bxx Boundary value problems \{For ordinary differential operators, see 34Lxx\}
34B05 Linear boundary value problems
Linear boundary value problems with nonlinear dependence on the spectral parameter
34B08 Multi-parameter boundary value problems
34B09 Boundary value problems with an indefinite weight
34B10 Multipoint boundary value problems
34B15 Nonlinear boundary value problems
34B16 Singular nonlinear boundary value problems problems

34B20
34B24
34B27
34B30
34B37
34B40
34B45
34B60
34B99
34Cxx
34C05
34C07

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34C10

34C11
34 C 12
34C14
34 C 15
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34C23
34C25
34C26
34 C 27
34C28

34C29
34C30
34C37
34 C 40
34C41
34C45
34C55
34C60
34C99
34Dxx
34D05
34D08
34D09
34D10
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34D30
34D35
34D40
34D45
34D99
34Exx
34E05
34E10

Weyl theory and its generalizations
Sturm-Liouville theory [See also 34Lxx] Green functions
Special equations (Mathieu, Hill, Bessel, etc.)
Boundary value problems with impulses
Boundary value problems on infinite intervals
Boundary value problems on graphs and networks
Applications
None of the above, but in this section
Qualitative theory [See also 37-XX]
Location of integral curves, singular points, limit cycles
Theory of limit cycles of polynomial and analytic vector fields (existence, uniqueness, bounds, Hilbert's 16th problem and ramifications)
Connections with real algebraic geometry (fewnomials, desingularization, zeros of Abelian integrals, etc.)
Oscillation theory, zeros, disconjugacy and comparison theory
Growth, boundedness, comparison of solutions
Monotone systems
Symmetries, invariants
Nonlinear oscillations, coupled oscillators
Transformation and reduction of equations and systems, normal forms
Bifurcation [See mainly 37Gxx]
Periodic solutions
Relaxation oscillations
Almost periodic solutions
Complex behavior, chaotic systems
[See mainly 37Dxx]
Averaging method
Manifolds of solutions
Homoclinic and heteroclinic solutions
Equations and systems on manifolds
Equivalence, asymptotic equivalence
Method of integral manifolds
Hysteresis
Applications
None of the above, but in this section
Stability theory [See also 37C75, 93Dxx]
Asymptotic properties
Characteristic and Lyapunov exponents
Dichotomy, trichotomy
Perturbations
Singular perturbations
Lyapunov stability
Global stability
Structural stability and analogous concepts
[See also 37C20]
Stability of manifolds of solutions
Ultimate boundedness
Attractors [See also 37C70, 37D45]
None of the above, but in this section
Asymptotic theory
Asymptotic expansions
Perturbations, asymptotics

\begin{tabular}{|c|c|c|c|}
\hline 34E13 \& Multiple scale methods \& 34L20 \& Asymptotic distribution of eigenvalues, \\
\hline 34E15 \& Singular perturbations, general theory \& \& asymptotic theory of eigenfunctions \\
\hline 34E18 \& Methods of nonstandard analysis \& 34L25 \& Scattering theory \\
\hline 34E20 \& Singular perturbations, turning point theory, \& 34L30 \& Nonlinear ordinary differential operators \\
\hline \& WKB methods \& 34L40 \& Particular operators (Dirac, one-dimensional \\
\hline 34E99 \& None of the above, but in this section \& \& Schrödinger, etc.) \\
\hline 34F05 \& Equations and systems with randomness \& 34L99 \& None of the above, but in this section \\
\hline 34Gxx \& \begin{tabular}{l}
[See also 34K50, 60H10, 93E03] \\
Differential equations in abstract spaces
\end{tabular} \& 34Mxx \& Differential equations in the complex domain [See also 30Dxx, 32G34] \\
\hline \& [See also 34Lxx, 37Kxx, 47Dxx, 47Hxx, 47Jxx, \& 34M05 \& Entire and meromorphic solutions \\
\hline \& 58D25] \& 34M10 \& Oscillation, growth of solutions \\
\hline 34G10 \& Linear equations [See also 47D06, 47D09] \& 34M15 \& Algebraic aspects (differential-algebraic, \\
\hline 34G20 \& Nonlinear equations [See also 47Hxx, 47Jxx] \& 34M15 \& hypertranscendence, group-theoretical) \\
\hline 34G25 \& Evolution inclusions \& 34M20 \& Nonanalytic aspects \\
\hline 34G99 \& None of the above, but in this section \& 34M25 \& Formal solutions, transform techniques \\
\hline 34H05 \& Control problems [See also 49J25, 49K25,
93C15] \& 34M30 \& Asymptotics, summation methods \\
\hline 34Kxx \& Functional-differential and differentialdifference equations, with or without deviating arguments [See also 37-XX] \& 34 M 35
34 M 37 \& Singularities, monodromy, local behavior of solutions, normal forms Resurgence phenomena \\
\hline 34K05 \& General theory \& 34M40 \& Stokes phenomena and connection problems \\
\hline 34K06 \& Linear functional-differential equations \& \& \\
\hline 34K07 \& Theoretical approximation of solutions \& 34M45 \& Differential equations on complex manifolds \\
\hline 34K10 \& Boundary value problems \& 34M50 \& Inverse problems (Riemann-Hilbert, inverse \\
\hline 34K11 \& Oscillation theory \& \& differential Galois, etc.) \\
\hline 34K12 \& Growth, boundedness, comparison of solutions \& 34M55 \& Painlevé and other special equations; \\
\hline 34K13 \& Periodic solutions \& \& classification, hierarchies; isomonodromic \\
\hline 34K14 \& Almost periodic solutions \& \& deformations \\
\hline 34 K 17

34 K 18 \& Transformation and reduction of equations and systems, normal forms \& 34M60 \& Singular perturbation problems in the complex domain (complex WKB, turning points, steepest descent) [See also 34E20] <br>
\hline 34K18 \& Bifurcation theory \& \& <br>
\hline 34K19 \& Invariant manifolds \& 34M99 \& None of the above, but in this section <br>
\hline 34K20 \& Stability theory \& 35-XX \& PARTIAL DIFFERENTIAL EQUATIONS <br>
\hline 34K23 \& Complex (chaotic) behavior of solutions \& 35-00 \& General reference works (handbooks, dictionaries, <br>
\hline 34K25 \& Asymptotic theory \& \& bibliographies, etc.) <br>
\hline 34K26 \& Singular perturbations \& 35-01 \& Instructional exposition (textbooks, tutorial <br>
\hline 34K28 \& Numerical approximation of solutions \& \& papers, etc.) <br>
\hline 34K29 \& Inverse problems \& 35-02 \& Research exposition (monographs, survey articles) <br>
\hline 34K30 \& Equations in abstract spaces [See also 34Gxx, 47Dxx, 47Jxx] \& 35-03 \& Historical (must also be assigned at least one classification number from Section 01) <br>
\hline 34K35 \& Control problems [See also 49J25, 49K25, 93C15] \& 35-04 \& Explicit machine computation and programs (not the theory of computation or programming) <br>
\hline 34K40 \& Neutral equations \& 35-06 \& Proceedings, conferences, collections, etc. <br>
\hline 34K45 \& Equations with impulses \& 35Axx \& General theory <br>
\hline 34K50 \& Stochastic delay equations [See also 34F05, $60 \mathrm{Hxx}]$ \& 35A05 \& General existence and uniqueness theorems <br>
\hline 34K60 \& Applications \& 35A07 \& Local existence and uniqueness theorems [See also 35Hxx, 35Sxx] <br>
\hline 34K99 \& None of the above, but in this section \& \& Fundamental solutions <br>
\hline 34Lxx \& Ordinary differential operators [See also 47E05] \& 35A10 \& Cauchy-Kovalevskaya theorems <br>
\hline 34L05 \& General spectral theory \& 35A15 \& Variational methods <br>

\hline 34L10 \& Eigenfunction expansions, completeness of eigenfunctions \& 35A17 \& | Parametrices |
| :--- |
| Wave front sets | <br>

\hline 34L15 \& Estimation of eigenvalues, upper and lower bounds \& $$
\begin{aligned}
& 35 \mathrm{~A} 20 \\
& 35 \mathrm{~A} 21
\end{aligned}
$$ \& Analytic methods, singularities Propagation of singularities <br>

\hline 34L16 \& Numerical approximation of eigenvalues and of other parts of the spectrum \& $$
\begin{aligned}
& 35 \mathrm{~A} 22 \\
& 35 \mathrm{~A} 25
\end{aligned}
$$ \& Transform methods (e.g. integral transforms) Other special methods <br>

\hline
\end{tabular}

| 35A27 | Microlocal methods; methods of sheaf theory and <br> homological algebra in PDE [See also 32C38, | 35F10 | Initial value problems for linear first-order PDE, |
| :--- | :--- | :--- | :--- |
|  | 58J15] <br> Geometric theory, characteristics, transformations | 35F15 | linear evolution equations |
| Boundary value problems for linear first-order |  |  |  |
| 35A30 | PDE |  |  |
| [See also 58J70, 58J72] | 35F20 | General theory of nonlinear first-order PDE |  |


| 35Kxx | Parabolic equations and systems [See also 35Bxx, 35Dxx, 35R30, 35R35, 58J35] |
| :---: | :---: |
| 35K05 | Heat equation |
| 35K10 | General theory of second-order, parabolic equations |
| 35K15 | Initial value problems for second-order, parabolic equations |
| 35K20 | Boundary value problems for second-order, parabolic equations |
| 35K25 | General theory of higher-order, parabolic equations |
| 35K30 | Initial value problems for higher-order, parabolic equations |
| 35K35 | Boundary value problems for higher-order, parabolic equations |
| 35K40 | General theory of parabolic systems of PDE |
| 35K45 | Initial value problems for parabolic systems |
| 35K50 | Boundary value problems for parabolic systems |
| 35K55 | Nonlinear PDE of parabolic type |
| 35K57 | Reaction-diffusion equations |
| 35K60 | Nonlinear boundary value problems for linear parabolic PDE; boundary value problems for nonlinear parabolic PDE |
| 35K65 | Parabolic partial differential equations of degenerate type |
| 35K70 | Ultraparabolic, pseudoparabolic PDE, etc. |
| 35K85 | Unilateral problems and variational inequalities for parabolic PDE [See also 35R35, 49J40] |
| 35K90 | Abstract parabolic evolution equations |
| 35K99 | None of the above, but in this section |
| 35Lxx | Partial differential equations of hyperbolic type [See also 58J45] |
| 35L05 | Wave equation |
| 35 L 10 | General theory of second-order, hyperbolic equations |
| 35L15 | Initial value problems for second-order, hyperbolic equations |
| 35L20 | Boundary value problems for second-order, hyperbolic equations |
| 35L25 | General theory of higher-order, hyperbolic equations |
| 35L30 | Initial value problems for higher-order, hyperbolic equations |
| 35L35 | Boundary value problems for higher-order, hyperbolic equations |
| 35L40 | General theory of hyperbolic systems of firstorder PDE |
| 35L45 | Initial value problems for hyperbolic systems of first-order PDE |
| 35L50 | Boundary value problems for hyperbolic systems of first-order PDE |
| 35L55 | Hyperbolic systems of higher-order PDE |
| 35L60 | Nonlinear first-order PDE of hyperbolic type |
| 35L65 | Conservation laws |
| 35L67 | Shocks and singularities [See also 58Kxx, 76L05] |
| 35L70 | Nonlinear second-order PDE of hyperbolic type |
| 35L75 | Nonlinear hyperbolic PDE of higher ( $>2$ ) order |
| 35L80 | Hyperbolic PDE of degenerate type |

35L82
35L85

35L90
35L99
35Mxx

35M10
35M20
35M99
35Nxx

35N05

35N10

35N15 $\quad \partial$-Neumann problem and generalizations; formal complexes [See also $32 \mathrm{~W} 05,32 \mathrm{~W} 10,58 \mathrm{~J} 10$ ]
35N99 None of the above, but in this section
35Pxx Spectral theory and eigenvalue problems for partial differential operators [See also 47Axx, 47Bxx, 47F05]
General spectral theory of PDE
Completeness of eigenfunctions, eigenfunction expansions for PDO
35P15 Estimation of eigenvalues, upper and lower bounds
35P20 Asymptotic distribution of eigenvalues and eigenfunctions for PDO
35P25
35P30

35P99
35Qxx

35Q05

35Q15 Riemann-Hilbert problems [See also 30E25, 31A25, 31B20]
35Q30 Stokes and Navier-Stokes equations
[See also 76D05, 76D07, 76N10]
35Q35
35Q40
35Q51
35Q53

35Q55

35Q58

35Q60
35Q72
35Q75
35Q80 Applications of PDE in areas other than physics
35Q99 None of the above, but in this section

| 35Rxx | Miscellaneous topics involving partial <br> differential equations \{For equations on |
| :--- | :--- |
|  | manifolds, see 58Jxx; for manifolds of <br> solutions, see 58Bxx; for stochastic PDEs, see |
|  | also 60H15\} |
| 35R05 | PDE with discontinuous coefficients or data |
| 35R10 | Partial functional-differential or differential- <br> difference equations, with or without deviating |
|  | arguments |
|  | Impulsive partial differential equations |
|  | Partial differential equations on infinite- <br> dimensional (e.g. function) spaces (= PDE in |
| 35R12 |  |

37A15

37 A 17
37A20

37A25
37A30

37A35

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37A50

37A55

37A60

37A99
37Bxx
37B05

37B10
37B15
37B20
37B25

37B30
37B35

37B40
37B45
37B50

37B55
37B99
37Cxx

37C05
37C10

37C15

37C20
37C25

37C27
37C29
37C30

37C35
37C40

37C45

General groups of measure-preserving transformations [See mainly 22Fxx]
Homogeneous flows [See also 22Fxx]
Orbit equivalence, cocycles, ergodic equivalence relations
Ergodicity, mixing, rates of mixing
Ergodic theorems, spectral theory, Markov operators \{For operator ergodic theory, see mainly 47A35\}
Entropy and other invariants, isomorphism, classification
Nonsingular (and infinite-measure preserving) transformations
Relations with number theory and harmonic analysis [See also 11 Kxx ]
Relations with probability theory and stochastic processes [See also 60Fxx and 60G10]
Relations with the theory of $C^{*}$-algebras [See mainly 46L55]
Dynamical systems in statistical mechanics
[See also 82Cxx]
None of the above, but in this section
Topological dynamics [See also 54H20]
Transformations and group actions with special properties (minimality, distality, proximality, etc.)
Symbolic dynamics [See also 37Cxx, 37Dxx]
Cellular automata
Notions of recurrence
Lyapunov functions and stability; attractors, repellers
Index theory, Morse-Conley indices
Gradient-like and recurrent behavior; isolated (locally-maximal) invariant sets
Topological entropy
Continua theory in dynamics
Multi-dimensional shifts of finite type, tiling dynamics
Nonautonomous dynamical systems
None of the above, but in this section
Smooth dynamical systems: general theory [See also 34Cxx, 34Dxx]
Smooth mappings and diffeomorphisms
Vector fields, flows, ordinary differential equations
Topological and differentiable equivalence, conjugacy, invariants, moduli, classification
Generic properties, structural stability
Fixed points, periodic points, fixed-point index theory
Periodic orbits of vector fields and flows
Homoclinic and heteroclinic orbits
Zeta functions, (Ruelle-Frobenius) transfer
operators, and other functional analytic
techniques in dynamical systems
Orbit growth
Smooth ergodic theory, invariant measures [See also 37Dxx]
Dimension theory of dynamical systems

| 37C50 | Approximate trajectories (pseudotrajectories, shadowing, etc.) | $\begin{aligned} & 37 \mathrm{~F} 35 \\ & 37 \mathrm{~F} 40 \end{aligned}$ |
| :---: | :---: | :---: |
| 37C55 | Periodic and quasiperiodic flows and diffeomorphisms | 37F45 |
| 37C60 | Nonautonomous smooth dynamical systems [See also 37B55] | 37F50 |
| 37C65 | Monotone flows | 37F75 |
| 37 C 70 | Attractors and repellers, topological structure |  |
| 37 C 75 | Stability theory | 37F99 |
| 37 C 80 | Symmetries, equivariant dynamical systems | 37Gxx |
| 37 C 85 | Dynamics of group actions other than $\mathbf{Z}$ and |  |
|  | $\mathbf{R}$, and foliations [See mainly 22Fxx, and also | 37G05 |
|  | 57R30, 57Sxx] | 37G10 |
| 37C99 | None of the above, but in this section | 37G15 |
| 37Dxx | Dynamical systems with hyperbolic behavior | 37G20 |
| 37D05 | Hyperbolic orbits and sets | 37 G 20 |
| 37 D 10 | Invariant manifold theory | 37G25 |
| 37D15 | Morse-Smale systems |  |
| 37D20 | Uniformly hyperbolic systems (expanding, | 37G30 |
|  | Anosov, Axiom A, etc.) | 37G35 |
| 37D25 | Nonuniformly hyperbolic systems (Lyapunov exponents, Pesin theory, etc.) | 37 G 40 37 G 99 |
| 37D30 | Partially hyperbolic systems and dominated splittings | $\mathbf{3 7 H x}$ |
| 37D35 | Thermodynamic formalism, variational principles, equilibrium states | 37H05 |
| 37D40 | Dynamical systems of geometric origin and hyperbolicity (geodesic and horocycle flows, etc.) | 37H10 |
| 37D45 | Strange attractors, chaotic dynamics |  |
| 37D50 | Hyperbolic systems with singularities (billiards, etc.) | 37H15 |
| 37D99 | None of the above, but in this section |  |
| 37Exx | Low-dimensional dynamical systems |  |
| 37E05 | Maps of the interval (piecewise continuous, continuous, smooth) | $\begin{aligned} & 37 \mathrm{H} 20 \\ & 37 \mathrm{H} 99 \end{aligned}$ |
| 37E10 | Maps of the circle | 37Jxx |
| 37E15 | Combinatorial dynamics (types of periodic orbits) |  |
| 37 E 20 | Universality, renormalization [See also 37F25] |  |
| 37E25 | Maps of trees and graphs | 37J05 |
| 37E30 | Homeomorphisms and diffeomorphisms of planes and surfaces | 37J10 |
| 37E35 | Flows on surfaces | 37J15 |
| 37 E 40 | Twist maps |  |
| 37E45 | Rotation numbers and vectors | 37J20 |
| 37E99 | None of the above, but in this section | 37J25 |
| 37Fxx | Complex dynamical systems [See also 30D05, 32H50] | 37J30 |
| 37F05 | Relations and correspondences | 37J35 |
| 37F10 | Polynomials; rational maps; entire and meromorphic functions [See also 32A10, 32A20, $32 \mathrm{H} 02,32 \mathrm{H} 04]$ | 37J40 |
| 37F15 | Expanding maps; hyperbolicity; structural stability | 37J45 |
| 37F20 | Combinatorics and topology | 37 J 50 |
| 37 F 25 | Renormalization | 37 J 55 |
| 37F30 | Quasiconformal methods and Teichmüller theory; | 37J60 |
|  | Fuchsian and Kleinian groups as dynamical systems | 37 J 99 |

Conformal densities and Hausdorff dimension Geometric limits
Holomorphic families of dynamical systems; the Mandelbrot set; bifurcations
Small divisors, rotation domains and linearization; Fatou and Julia sets
Holomorphic foliations and vector fields [See also 32M25, 32S65, 34Mxx]
None of the above, but in this section
Local and nonlocal bifurcation theory [See also 34C23, 34K18]
37G05 Normal forms
37G10 Bifurcations of singular points
37G15 Bifurcations of limit cycles and periodic orbits
Hyperbolic singular points with homoclinic trajectories
Bifurcations connected with nontransversal intersection
37G30 Infinite nonwandering sets arising in bifurcations
Attractors and their bifurcations
37G40 Symmetries, equivariant bifurcation theory
37 None of the above, but in this section
Random dynamical systems [See also 15A52, 34D08, 34F05, 47B80, 70L05, 82C05, 93Exx]
37H05 Foundations, general theory of cocycles, algebraic ergodic theory [See also 37Axx]
Generation, random and stochastic difference and differential equations [See also 34F05, 34K50, 60H10, 60H15]
Multiplicative ergodic theory, Lyapunov exponents [See also 34D08, 37Axx, 37Cxx, 37Dxx]
Bifurcation theory [See also 37Gxx]
None of the above, but in this section
Finite-dimensional Hamiltonian, Lagrangian, contact, and nonholonomic systems
[See also 53Dxx, 70Fxx, 70Hxx]
General theory, relations with symplectic geometry and topology
Symplectic mappings, fixed points Symmetries, invariants, invariant manifolds, momentum maps, reduction [See also 53D20] Bifurcation problems
Stability problems
Obstructions to integrability (nonintegrability criteria)
Completely integrable systems, topological structure of phase space, integration methods
Perturbations, normal forms, small divisors, KAM theory, Arnol'd diffusion
Periodic, homoclinic and heteroclinic orbits; variational methods, degree-theoretic methods
Action-minimizing orbits and measures
Contact systems [See also 53D10]
Nonholonomic dynamical systems
[See also 70F25]
None of the above, but in this section

| 37Kxx | Infinite-dimensional Hamiltonian systems [See also 35Axx, 35Qxx] |
| :---: | :---: |
| 37K05 | Hamiltonian structures, symmetries, variational principles, conservation laws |
| 37K10 | Completely integrable systems, integrability tests, bi-Hamiltonian structures, hierarchies (KdV, KP, Toda, etc.) |
| 37K15 | Integration of completely integrable systems by inverse spectral and scattering methods |
| 37K20 | Relations with algebraic geometry, complex analysis, special functions [See also 14H70] |
| 37K25 | Relations with differential geometry |
| 37K30 | Relations with infinite-dimensional Lie algebras and other algebraic structures |
| 37K35 | Lie-Bäcklund and other transformations |
| 37K40 | Soliton theory, asymptotic behavior of solutions |
| 37K45 | Stability problems |
| 37K50 | Bifurcation problems |
| 37K55 | Perturbations, KAM for infinite-dimensional systems |
| 37K60 | Lattice dynamics [See also 37L60] |
| 37K65 | Hamiltonian systems on groups of diffeomorphisms and on manifolds of mappings and metrics |
| 37K99 | None of the above, but in this section |
| 37Lxx | Infinite-dimensional dissipative dynamical systems [See also 35Bxx, 35Qxx] |
| 37L05 | General theory, nonlinear semigroups, evolution equations |
| 37L10 | Normal forms, center manifold theory, bifurcation theory |
| 37L15 | Stability problems |
| 37L20 | Symmetries |
| 37L25 | Inertial manifolds and other invariant attracting sets |
| 37L30 | Attractors and their dimensions, Lyapunov exponents |
| 37L40 | Invariant measures |
| 37L45 | Hyperbolicity; Lyapunov functions |
| 37L50 | Noncompact semigroups; dispersive equations; perturbations of Hamiltonian systems |
| 37L55 | Infinite-dimensional random dynamical systems; stochastic equations [See also 35R60, 60H10, 60H15] |
| 37L60 | Lattice dynamics [See also 37K60] |
| 37L65 | Special approximation methods (nonlinear Galerkin, etc.) |
| 37L99 | None of the above, but in this section |
| 37Mxx | Approximation methods and numerical treatment of dynamical systems [See also 65Pxx] |
| 37M05 | Simulation |
| 37M10 | Time series analysis |
| 37M15 | Symplectic integrators |
| 37M20 | Computational methods for bifurcation problems |
| 37M25 | Computational methods for ergodic theory (approximation of invariant measures, computation of Lyapunov exponents, entropy) |

37M99 None of the above, but in this section
37Nxx
37N05

37N10

37N1
37N20 Dynamical systems in other branches of physics (quantum mechanics, general relativity, laser physics)
37N25 Dynamical systems in biology [See mainly 92XX, but also 91-XX]
37N30 Dynamical systems in numerical analysis
37N35 Dynamical systems in control
37N40 Dynamical systems in optimization and economics
37N99 None of the above, but in this section
39-XX DIFFERENCE AND FUNCTIONAL EQUATIONS
39-00 General reference works (handbooks, dictionaries, bibliographies, etc.)
39-01 Instructional exposition (textbooks, tutorial papers, etc.)
39-02 Research exposition (monographs, survey articles)
39-03 Historical (must also be assigned at least one classification number from Section 01)
39-04 Explicit machine computation and programs (not the theory of computation or programming)
39-06 Proceedings, conferences, collections, etc.
39Axx Difference equations \{For dynamical systems, see $37-\mathbf{X X}\}$
39A05 General
39A10 Difference equations, additive
39A11 Stability and asymptotics of difference equations; oscillatory and periodic solutions, etc.
39A12 Discrete version of topics in analysis
39A13 Difference equations, scaling ( $q$-differences) [See also 33Dxx]
39A20 Multiplicative and other generalized difference equations, e.g. of Lyness type
39A70 Difference operators [See also 47B39]
39A99 None of the above, but in this section
39Bxx Functional equations and inequalities [See also 30D05]
39B05 General
39B12 Iteration theory, iterative and composite equations [See also 26A18, 30D05, 37-XX]
39B22 Equations for real functions [See also 26A51, 26B25]
39B32 Equations for complex functions
[See also 30D05]
39B42 Matrix and operator equations [See also 47Jxx]
39B52 Equations for functions with more general domains and/or ranges

| 39B55 | Orthogonal additivity and other conditional <br> equations |
| :--- | :--- |
| 39B62 | Functional inequalities, including subadditivity, <br> convexity, etc. [See also 26A51, 26B25, 26Dxx] |
| 39B72 | Systems of functional equations and inequalities |
| 39B82 | Stability, separation, extension, and related topics <br> [See also 46A22] |
| 39B99 | None of the above, but in this section |
| 40-XX | SEQUENCES, SERIES, SUMMABILITY |
| 40-00 | General reference works (handbooks, dictionaries, <br> bibliographies, etc.) |
| 40-01 | Instructional exposition (textbooks, tutorial <br> papers, etc.) |
| 40-02 | Research exposition (monographs, survey articles) |
| 40-03 | Historical (must also be assigned at least one <br> classification number from Section 01) |
| 40-04 | Explicit machine computation and programs (not <br> the theory of computation or programming) |
| 40-06 | Proceedings, conferences, collections, etc. |
| 40Axx | Convergence and divergence of infinite limiting <br> processes |
| 40E05 |  |

Orthogonal additivity and other conditional equations convexity, etc. [See also 26A51, 26B25, 26Dxx]
39B72
39B82 Stability, separation, extension, and related topics [See also 46A22]

## 40-XX

40-00

40-01 Instructional exposition (textbooks, tutorial papers, etc.)
Research exposition (monographs, survey articles)
Historical (must also be assigned at least one classification number from Section 01) the theory of computation or programming)
40-06 Proceedings, conferences, collections, etc.
40Axx Convergence and divergence of infinite limiting processes
40A05 Convergence and divergence of series and sequences
40A10 Convergence and divergence of integrals

40A20 $\begin{aligned} & \text { fractions [See also 30B70] } \\ & \text { Convergence and divergence of infinite products }\end{aligned}$
40A25 Approximation to limiting values (summation of series, etc.) \{For the Euler-Maclaurin summation formula, see 65B15\}
40A30 Convergence and divergence of series and sequences of functions
40A99 None of the above, but in this section
40B05 Multiple sequences and series (should also be assigned at least one other classification number in this section)
40Cxx General summability methods
40C05 Matrix methods
40C10 Integral methods
40C15 Function-theoretic methods (including power series methods and semicontinuous methods)
40C99 None of the above, but in this section
40Dxx Direct theorems on summability
General theorems
Structure of summability fields
Tauberian constants and oscillation limits
Convergence factors and summability factors
40D25 Inclusion and equivalence theorems
40D99 None of the above, but in this section
40Exx Inversion theorems
40E05 Tauberian theorems, general
40E10
40E15 Lacunary inversion theorems
40E20 Tauberian constants

40F05 Absolute and strong summability

| 40Gxx | Special methods of summability |
| :---: | :---: |
| 40G05 | Cesàro, Euler, Nörlund and Hausdorff methods |
| 40G10 | Abel, Borel and power series methods |
| 40G99 | None of the above, but in this section |
| $40 \mathrm{H05}$ | Functional analytic methods in summability |
| $40 \mathrm{J05}$ | Summability in abstract structures [See also 43A55, 46A35, 46B15] |
| 41-XX | APPROXIMATIONS AND EXPANSIONS <br> \{For all approximation theory in the complex domain, see 30 E 05 and 30 E 10 ; for all trigonometric approximation and interpolation, see 42A10 and 42A15; for numerical approximation, see 65Dxx\} |
| 41-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 41-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 41-02 | Research exposition (monographs, survey articles) |
| 41-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 41-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 41-06 | Proceedings, conferences, collections, etc. |
| 41A05 | Interpolation [See also 42A15 and 65D05] |
| 41A10 | Approximation by polynomials \{For approximation by trigonometric polynomials, see 42A10\} |
| 41A15 | Spline approximation |
| 41 A 17 | Inequalities in approximation (Bernstein, Jackson, Nikol'skiĭ-type inequalities) |
| 41A20 | Approximation by rational functions |
| 41A21 | Padé approximation |
| 41A25 | Rate of convergence, degree of approximation |
| 41A27 | Inverse theorems |
| 41A28 | Simultaneous approximation |
| 41A29 | Approximation with constraints |
| 41A30 | Approximation by other special function classes |
| 41A35 | Approximation by operators (in particular, by integral operators) |
| 41A36 | Approximation by positive operators |
| 41A40 | Saturation |
| 41A44 | Best constants |
| 41A45 | Approximation by arbitrary linear expressions |
| 41A46 | Approximation by arbitrary nonlinear expressions; widths and entropy |
| 41A50 | Best approximation, Chebyshev systems |
| 41A52 | Uniqueness of best approximation |
| 41A55 | Approximate quadratures |
| 41A58 | Series expansions (e.g. Taylor, Lidstone series, but not Fourier series) |
| 41A60 | Asymptotic approximations, asymptotic expansions (steepest descent, etc.) [See also 30E15] |
| 41A63 | Multidimensional problems (should also be assigned at least one other classification number in this section) |

40Gxx
40G05
40G10
40G99
40 H 05
$40 J 05$

41-XX

41-00

41-01

41-02
41-03

41-04

41-06
41A05
41A10

41A15
41A17

41A20
41A21
41 A25
41A27
41A28
41A29
41A30
41A35

41A36
41A40

41A45
41A46

41A50
41A52
41A55
Series expansions (e.g. Taylor, Lidstone series, but not Fourier series)
Asymptotic approximations, asymptotic expansions (steepest descent, etc.)
[See also 30E15]
assigned at least one other classification number in this section)
\(\left.$$
\begin{array}{cl}\text { 41A65 } & \begin{array}{l}\text { Abstract approximation theory (approximation in } \\
\text { normed linear spaces and other abstract spaces) }\end{array}
$$ <br>
41A80 \& Remainders in approximation formulas <br>

41A99 \& Miscellaneous topics\end{array}\right\}\)| 42-XX | FOURIER ANALYSIS |
| :--- | :--- |
| 42-00 | General reference works (handbooks, dictionaries, <br> bibliographies, etc.) |
| 42-01 | Instructional exposition (textbooks, tutorial <br> papers, etc.) |
| 42-02 | Research exposition (monographs, survey articles) |
| 42-03 | Historical (must also be assigned at least one <br> classification number from Section 01) |
| 42-04 | Explicit machine computation and programs (not <br> the theory of computation or programming) |
| 42-06 | Proceedings, conferences, collections, etc. |
| 42Axx | Fourier analysis in one variable |
| 42A05 | Trigonometric polynomials, inequalities, extremal <br> problems |
| 42A10 | Trigonometric approximation |
| 42A15 | Trigonometric interpolation |
| 42A16 | Fourier coefficients, Fourier series of functions <br> with special properties, special Fourier series |
| 42B15 |  |

42B35 Function spaces arising in harmonic analysis
42B99 None of the above, but in this section
42Cxx Nontrigonometric Fourier analysis
42C05 Orthogonal functions and polynomials, general theory [See also 33C45, 33C50, 33D45]
42C10 Fourier series in special orthogonal functions (Legendre polynomials, Walsh functions, etc.)
42C15 Series of general orthogonal functions, generalized Fourier expansions, nonorthogonal expansions
42C20 Rearrangements and other transformations of Fourier and other orthogonal series
42C25 Uniqueness and localization for orthogonal series
42C30 Completeness of sets of functions
42C40 Wavelets
42C99 None of the above, but in this section
43-XX ABSTRACT HARMONIC ANALYSIS \{For other analysis on topological and Lie groups, see 22Exx $\}$
43-00 General reference works (handbooks, dictionaries, bibliographies, etc.)
43-01 Instructional exposition (textbooks, tutorial papers, etc.)
43-02 Research exposition (monographs, survey articles)
43-03 Historical (must also be assigned at least one classification number from Section 01)
43-04 Explicit machine computation and programs (not the theory of computation or programming)
43-06 Proceedings, conferences, collections, etc.
43A05 Measures on groups and semigroups, etc.
43A07 Means on groups, semigroups, etc.; amenable groups
43A10 Measure algebras on groups, semigroups, etc.
43A15 $\quad L^{p}$-spaces and other function spaces on groups, semigroups, etc.
43A17 Analysis on ordered groups, $H^{p}$-theory
43A20 $\quad L^{1}$-algebras on groups, semigroups, etc.
43A22 Homomorphisms and multipliers of function spaces on groups, semigroups, etc.
43A25 Fourier and Fourier-Stieltjes transforms on locally compact abelian groups
43A30 Fourier and Fourier-Stieltjes transforms on nonabelian groups and on semigroups, etc.
43A32 Other transforms and operators of Fourier type
43A35 Positive definite functions on groups, semigroups, etc.
43A40 Character groups and dual objects
43A45 Spectral synthesis on groups, semigroups, etc.
43A46 Special sets (thin sets, Kronecker sets, Helson sets, Ditkin sets, Sidon sets, etc.)
43A50 Convergence of Fourier series and of inverse transforms
43A55 Summability methods on groups, semigroups, etc. [See also 40J05]

| 43A60 | Almost periodic functions on groups and semigroups and their generalizations (recurrent functions, distal functions, etc.); almost automorphic functions |
| :---: | :---: |
| 43A62 | Hypergroups |
| 43A65 | Representations of groups, semigroups, etc. [See also 22A10, 22A20, 22Dxx, 22E45] |
| 43A70 | Analysis on specific locally compact abelian groups [See also 11R56, 22B05] |
| 43A75 | Analysis on specific compact groups |
| 43A77 | Analysis on general compact groups |
| 43A80 | Analysis on other specific Lie groups [See also 22Exx] |
| 43 A85 | Analysis on homogeneous spaces |
| 43A90 | Spherical functions [See also 22E45, 22E46, 33C65] |
| 43A95 | Categorical methods [See also 46Mxx] |
| 43A99 | Miscellaneous topics |
| 44-XX | INTEGRAL TRANSFORMS, OPERATIONAL CALCULUS \{For fractional derivatives and integrals, see 26A33. For Fourier transforms, see 42A38, 42B10. For integral transforms in distribution spaces, see 46F12. For numerical methods, see 65R10\} |
| 44-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 44-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 44-02 | Research exposition (monographs, survey articles) |
| 44-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 44-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 44-06 | Proceedings, conferences, collections, etc. |
| 44A05 | General transforms [See also 42A38] |
| 44A10 | Laplace transform |
| 44A12 | Radon transform [See also 92C55] |
| 44A15 | Special transforms (Legendre, Hilbert, etc.) |
| 44A20 | Transforms of special functions |
| 44A30 | Multiple transforms |
| 44A35 | Convolution |
| 44A40 | Calculus of Mikusiński and other operational calculi |
| 44A45 | Classical operational calculus |
| 44A55 | Discrete operational calculus |
| 44A60 | Moment problems |
| 44A99 | Miscellaneous topics |
| 45-XX | INTEGRAL EQUATIONS |
| 45-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 45-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 45-02 | Research exposition (monographs, survey articles) |
| 45-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 45-04 | Explicit machine computation and programs (not the theory of computation or programming) |


| 45-06 | Proceedings, conferences, collections, etc. |
| :---: | :---: |
| 45A05 | Linear integral equations |
| 45B05 | Fredholm integral equations |
| $45 \mathrm{C05}$ | Eigenvalue problems [See also 34Lxx, 35Pxx, 45P05, 47A75] |
| 45D05 | Volterra integral equations [See also 34A12] |
| 45Exx | Singular integral equations [See also 30E20, 30E25, 44A15, 44A35] |
| 45E05 | Integral equations with kernels of Cauchy type [See also 35J15] |
| 45E10 | Integral equations of the convolution type (Abel, Picard, Toeplitz and Wiener-Hopf type) [See also 47B35] |
| 45E99 | None of the above, but in this section |
| 45Fxx | Systems of linear integral equations |
| 45F05 | Systems of nonsingular linear integral equations |
| 45 F 10 | Dual, triple, etc., integral and series equations |
| 45F15 | Systems of singular linear integral equations |
| 45F99 | None of the above, but in this section |
| 45Gxx | Nonlinear integral equations [See also 47H30, 47Jxx] |
| 45G05 | Singular nonlinear integral equations |
| 45G10 | Other nonlinear integral equations |
| 45G15 | Systems of nonlinear integral equations |
| 45 H 05 | Miscellaneous special kernels [See also 44A15] |
| 45J05 | Integro-ordinary differential equations [See also 34K05, 34K30, 47G20] |
| 45 K 05 | Integro-partial differential equations [See also 34K30, 35R10, 47G20] |
| 45L05 | Theoretical approximation of solutions \{For numerical analysis, see 65Rxx\} |
| 45Mxx | Qualitative behavior |
| 45M05 | Asymptotics |
| 45M10 | Stability theory |
| 45M15 | Periodic solutions |
| 45M20 | Positive solutions |
| 45M99 | None of the above, but in this section |
| 45N05 | Abstract integral equations, integral equations in abstract spaces |
| 45P05 | Integral operators [See also 47B38, 47G10] |
| 45Q05 | Inverse problems |
| 45R05 | Random integral equations [See also 60H20] |
| 46-XX | FUNCTIONAL ANALYSIS \{For manifolds modeled on topological linear spaces, see 57Nxx, 58Bxx $\}$ |
| 46-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 46-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 46-02 | Research exposition (monographs, survey articles) |
| 46-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 46-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 46-06 | Proceedings, conferences, collections, etc. |


| 46Axx | Topological linear spaces and related <br> structures \{For function spaces, see 46Exx |
| :--- | :--- |
| 46A03 | General theory of locally convex spaces <br> Locally convex Fréchet spaces and (DF)-spaces |
| 46A04 |  |
| 46A08 | Barrelled spaces, bornological spaces |
| 46A11 | Spaces determined by compactness or <br> summability properties (nuclear spaces, Schwartz <br> spaces, Montel spaces, etc.) |
| 46A13 | Spaces defined by inductive or projective limits <br> (LB, LF, etc.) [See also 46M40] |
| 46A16 | Not locally convex spaces (metrizable topological <br> linear spaces, locally bounded spaces, quasi- |
| Banach spaces, etc.) |  |

46C07 Hilbert subspaces (= operator ranges);

46B20
46B22

46B25
46B26
46B28

46B40
46B42
46B45
46B50
46B70
46B99
46 Cxx

46C05

46C15
46C20

46C50

46C99
46Exx

46E05

46E10

46E15

46E20
46E22

46E25

46E27
46E30

46E35

46E39
46E40

Geometry and structure of normed linear spaces
Radon-Nikodým, Kreĭn-Milman and related properties [See also 46G10]
Classical Banach spaces in the general theory
Nonseparable Banach spaces
Spaces of operators; tensor products; approximation properties [See also 46A32, 46M05, 47L05, 47L20]
Ordered normed spaces [See also 46A40, 46B42]
Banach lattices [See also 46A40, 46B40]
Banach sequence spaces [See also 46A45]
Compactness in Banach (or normed) spaces
Interpolation between normed linear spaces
[See also 46M35]
None of the above, but in this section
Inner product spaces and their generalizations,
Hilbert spaces \{For function spaces, see 46Exx $\}$
Hilbert and pre-Hilbert spaces: geometry and topology (including spaces with semidefinite inner product)
complementation (Aronszajn, de Branges, etc.) [See also 46B70, 46M35]
Characterizations of Hilbert spaces
Spaces with indefinite inner product (Kreĭn spaces, Pontryagin spaces, etc.) [See also 47B50] Generalizations of inner products (semi-inner products, partial inner products, etc.)
None of the above, but in this section
Linear function spaces and their duals
[See also 30H05, 32A38, 46F05] \{For function algebras, see 46J10\}
Lattices of continuous, differentiable or analytic functions
Topological linear spaces of continuous, differentiable or analytic functions
Banach spaces of continuous, differentiable or analytic functions
Hilbert spaces of continuous, differentiable or analytic functions
Hilbert spaces with reproducing kernels (= [proper] functional Hilbert spaces, including de Branges-Rovnyak and other structured spaces) [See also 47B32]
Rings and algebras of continuous, differentiable or analytic functions \{For Banach function algebras, see 46J10, 46J15\}
Spaces of measures [See also 28A33, 46Gxx] Spaces of measurable functions ( $L^{p}$-spaces, Orlicz spaces, Köthe function spaces, Lorentz spaces, rearrangement invariant spaces, ideal spaces, etc.)
Sobolev spaces and other spaces of "smooth" functions, embedding theorems, trace theorems
Sobolev (and similar kinds of) spaces of functions of discrete variables
Spaces of vector- and operator-valued functions

| 46E50 | Spaces of differentiable or holomorphic functions on infinite-dimensional spaces [See also 46G20, 46G25, 47H60] | 46Jxx | Commutative Banach algebras and commutative topological algebras [See also 46E25] |
| :---: | :---: | :---: | :---: |
| 46E99 | None of the above, but in this section | 46J05 | General theory of commutative topological |
| 46Fxx | Distributions, generalized functions, distribution spaces [See also 46T30] | 46J10 | algebras <br> Banach algebras of continuous functions, function |
| 46F05 | Topological linear spaces of test functions, distributions and ultradistributions [See also 46E10, 46E35] | 46J15 | algebras [See also 46E25] <br> Banach algebras of differentiable or analytic functions, $H^{p}$-spaces [See also 30D55, 30H05, |
| 46F10 | Operations with distributions |  | $32 \mathrm{~A} 35,32 \mathrm{~A} 37,32 \mathrm{~A} 38,42 \mathrm{~B} 30]$ |
| 46 F 12 | Integral transforms in distribution spaces [See also 42-XX, 44-XX] | $\begin{aligned} & 46 \mathrm{~J} 20 \\ & 46 \mathrm{~J} 25 \end{aligned}$ | Ideals, maximal ideals, boundaries Representations of commutative topological |
| 46F15 | Hyperfunctions, analytic functionals [See also 32A25, 32A45, 32C35, 58J15] | 46J30 | algebras Subalgebras |
| 46F20 | Distributions and ultradistributions as boundary values of analytic functions [See also 30D40, 30E25, 32A40] | $46 J 40$ $46 J 45$ | Structure, classification of commutative topological algebras Radical Banach algebras |
| 46F25 | Distributions on infinite-dimensional spaces [See also 58C35] | $\begin{aligned} & \text { 46J99 } \\ & \text { 46Kxx } \end{aligned}$ | None of the above, but in this section Topological (rings and) algebras with an |
| 46F30 | Generalized functions for nonlinear analysis (Rosinger, Colombeau, nonstandard, etc.) | 46K05 | involution [See also 16W10] <br> General theory of topological algebras with involution |
| 46F99 | None of the above, but in this section | 46K10 |  |
| 46Gxx | Measures, integration, derivative, holomorphy (all involving infinite-dimensional spaces) [See also 28-XX, 46Txx] | 46 K 10 46 K 15 | Representations of topological algebras with involution <br> Hilbert algebras |
| 46G05 | Derivatives [See also 46T20, 58C20, 58C25] | 46K50 | Nonselfadjoint (sub)algebras in algebras with involution |
| 46G10 | Vector-valued measures and integration [See also 28Bxx, 46B22] | 46K70 | Nonassociative topological algebras with an involution [See also 46H70, 46L70] |
| 46G12 | Measures and integration on abstract linear spaces [See also 28C20, 46T12] | 46K99 | None of the above, but in this section |
| 46G15 | Functional analytic lifting theory [See also 28A51] | 46Lxx | von Neumann ( $W^{*_{-}}$) algebras, etc.) <br> [See also 22D25, 47Lxx] |
| 46G20 | Infinite-dimensional holomorphy [See also 32XX, 46E50, 46T25, 58B12, 58C10] | 46L05 46L06 | General theory of $C^{*}$-algebras <br> Tensor products of $C^{*}$-algebras |
| 46G25 | (Spaces of) multilinear mappings, polynomials [See also 46E50, 46G20, 47H60] | 46L07 | Operator spaces and completely bounded maps [See also 47L25] |
| 46G99 | None of the above, but in this section | 46L08 | $C^{*}$-modules |
| 46Hxx | Topological algebras, normed rings and algebras, Banach algebras \{For group algebras, convolution algebras and measure algebras, see 43A10, 43A20\} | $\begin{aligned} & \text { 46L09 } \\ & \text { 46L10 } \\ & \text { 46L30 } \\ & \text { 46L35 } \end{aligned}$ | Free products of $C^{*}$-algebras <br> General theory of von Neumann algebras <br> States <br> Classifications of $C^{*}$-algebras, factors |
| 46H05 | General theory of topological algebras | 46L37 | Subfactors and their classification |
| 46H10 | Ideals and subalgebras | 46L40 | Automorphisms |
| 46H15 | Representations of topological algebras | 46L45 | Decomposition theory for $C^{*}$-algebras |
| 46 H 20 | Structure, classification of topological algebras | 46L51 | Noncommutative measure and integration |
| 46H25 | Normed modules and Banach modules, topological modules (if not placed in 13-XX or 16-XX) | 46L52 46L53 46L54 | Noncommutative function spaces Noncommutative probability and statistics Free probability and free operator algebras |
| 46H30 | Functional calculus in topological algebras [See also 47A60] | 46L55 | Noncommutative dynamical systems [See also 28Dxx, 37Kxx, 37Lxx, 54H20] |
| 46H35 | Topological algebras of operators [See mainly 47Lxx] | 46L57 | Derivations, dissipations and positive semigroups in $C^{*}$-algebras |
| 46H40 | Automatic continuity | 46L60 | Applications of selfadjoint operator algebras to |
| 46H70 | Nonassociative topological algebras [See also 46K70, 46L70] |  | physics [See also 46N50, 46N55, 47L90, 81T05, 82B10, 82C10] |
| 46H99 | None of the above, but in this section | 46L65 | Quantizations, deformations |


| 46L70 | Nonassociative selfadjoint operator algebras [See also 46H70, 46K70] | 46Txx | Nonlinear functional analysis [See also 47Hxx, 47Jxx, 58Cxx, 58Dxx] |
| :---: | :---: | :---: | :---: |
| 46L80 | $K$-theory and operator algebras (including cyclic theory) [See also 18 F 25 , 19Kxx, 46M20, 55Rxx, 58J22] | 46 T 05 46 T 10 | Infinite-dimensional manifolds [See also 53Axx, 57N20, 58Bxx, 58Dxx] <br> Manifolds of mappings |
| 46L85 | Noncommutative topology [See also 58B32, 58B34, 58J22] | 46 T 12 | Measure (Gaussian, cylindrical, etc.) and integrals (Feynman, path, Fresnel, etc.) on manifolds |
| 46L87 | Noncommutative differential geometry [See also 58B32, 58B34, 58J22] | 46 T 20 | [See also 28Cxx, 46G12, 60-XX] Continuous and differentiable maps |
| 46L89 | Other "noncommutative" mathematics based on $C^{*}$-algebra theory [See also 58B32, 58B34, 58J22] | $\begin{aligned} & 46 \mathrm{~T} 25 \\ & 46 \mathrm{~T} 30 \end{aligned}$ | [See also 46G05] <br> Holomorphic maps [See also 46G20] <br> Distributions and generalized functions |
| 46L99 | None of the above, but in this section |  | nonlinear spaces [See also 46Fxx] |
| 46Mxx | Methods of category theory in functional analysis [See also 18-XX] | 46 T 99 $\mathbf{4 7 - X X}$ | None of the above, but in this section OPERATOR THEORY |
| 46M05 | Tensor products [See also 46A32, 46B28, 47A80] | 47-XX $47-00$ | General reference works (handbooks, dictionaries, |
| 46 M 07 46 M 10 | Ultraproducts [See also 46B08, 46S20] Projective and injective objects [See als |  | bibliographies, etc.) |
| 46M15 | Categories, functors \{For $K$-theory, EXT, etc., see 19K33, 46L80, 46M18, 46M20\} | 47-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 46M18 | Homological methods (exact sequences, right inverses, lifting, etc.) | $47-02$ $47-03$ | Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) |
| 46M20 | Methods of algebraic topology (cohomology, sheaf and bundle theory, etc.) [See also 14F05, $18 \mathrm{Fxx}, 19 \mathrm{Kxx}, 32 \mathrm{Cxx}$, 32Lxx, 46L80, 46M15, 46M18, 55Rxx] | $47-04$ $47-06$ | Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc. |
| 46 M 35 46 M 40 | Abstract interpolation of topological vector spaces [See also 46B70] | 47Axx 47 A 05 | General theory of linear operators <br> General (adjoints, conjugates, products, inverses, domains, ranges, etc.) |
| 46M40 46M99 | Inductive and projective limits [See also 46A13] None of the above, but in this section | 47A06 | Linear relations (multivalued linear operators) |
| 46Nxx | Miscellaneous applications of functional analysis [See also 47Nxx] | 47 A 07 47 A 10 | Forms (bilinear, sesquilinear, multilinear) Spectrum, resolvent |
| 46N10 | Applications in optimization, convex analysis, mathematical programming, economics | $\begin{aligned} & 47 \mathrm{~A} 11 \\ & 47 \mathrm{~A} 12 \end{aligned}$ | Local spectral properties Numerical range, numerical radius |
| 46N20 | Applications to differential and integral equations | 47A13 | Several-variable operator theory (spectral, |
| 46N30 | Applications in probability theory and statistics |  | Fredholm, etc.) |
| 46N40 | Applications in numerical a | 47A15 | Invariant subspaces |
|  | [See also 65Jxx] | 47A16 | Cyclic and hypercyclic vectors |
| 46N50 | Applications in quantum physics | 47A20 | Dilations, extensions, compressions |
| 46N55 | Applications in statistical physics | 47A25 | Spectral sets |
| 46N60 | Applications in biology and other sciences | 47A30 | Norms (inequalities, more than one norm, etc.) |
| 46N99 | None of the above, but in this section | 47A35 | Ergodic theory [See also 28Dxx, 37Axx] |
| 46Sxx | Other (nonclassical) types of functional analysis [See also 47Sxx] | 47A40 | Scattering theory [See also 34L25, 35P25, 81Uxx] |
| 46S10 | Functional analysis over fields other than $\mathbf{R}$ or $\mathbf{C}$ or the quaternions; non-Archimedean functional analysis [See also 12J25, 32P05] | 47 A 45 47 A 46 | Canonical models for contractions and nonselfadjoint operators Chains (nests) of projections or of invariant |
| 46S20 | Nonstandard functional analysis [See also 03H05] |  | subspaces, integrals along chains, etc. |
| 46S30 | Constructive functional analysis [See also 03F60] | 47A48 | Operator colligations (= nodes), vessels, linear |
| 46S40 | Fuzzy functional analysis [See also 03E72] |  | systems, characteristic functions, realizations, etc. |
| 46S50 | Functional analysis in probabilistic metric linear spaces | 47A50 | Equations and inequalities involving linear operators, with vector unknowns |
| 46S60 | Functional analysis on superspaces (supermanifolds) or graded spaces [See also 58A50 and 58C50] | $\begin{aligned} & \text { 47A52 } \\ & \text { 47A53 } \end{aligned}$ | Ill-posed problems, regularization (Semi-) Fredholm operators; index theories [See also 58B15, 58J20] |
| 46S99 | None of the above, but in this section | 47A55 | Perturbation theory |


| 47A56 | Functions whose values are linear operators <br> (operator and matrix valued functions, etc., <br> including analytic and meromorphic ones) | 47B60 <br> Operator methods in interpolation, moment and <br> extension problems [See also 30E05, 42A70, | Operators on ordered spaces <br> Positive operators and order-bounded operators |
| :--- | :--- | :--- | :--- |
| 47A57 | 47B80 | Random operators [See also 60H25] <br> 47B99 | None of the above, but in this section <br> Individual linear operators as elements of <br> 4lgebraic systems |
| 47A82, 44A60] |  |  |  |


| 47H40 | Random operators [See also 60H25] |
| :---: | :---: |
| 47H50 | Potential operators |
| 47H60 | Multilinear and polynomial operators [See also 46G25] |
| 47H99 | None of the above, but in this section |
| 47Jxx | Equations and inequalities involving nonlinear operators [See also 46Txx] \{For global and geometric aspects, see $\mathbf{5 8} \mathbf{- X X}\}$ |
| 47J05 | Equations involving nonlinear operators (general) |
| 47J06 | Nonlinear ill-posed problems |
| 47J07 | Abstract inverse mapping and implicit function theorems [See also 46T20 and 58C15] |
| 47J10 | Nonlinear eigenvalue problems |
| 47J15 | Abstract bifurcation theory [See also 58E07, 58E09] |
| 47J20 | Variational and other types of inequalities involving nonlinear operators (general) |
| 47J25 | Methods for solving nonlinear operator equations (general) |
| 47J30 | Variational methods [See also 58Exx] |
| 47J35 | Nonlinear evolution equations [See also 34G20, 35K90, 35L90, 35Qxx, 35R20, 37Kxx, 37Lxx, 58D25] |
| 47J40 | Equations with hysteresis operators |
| 47J99 | None of the above, but in this section |
| 47Lxx | Linear spaces and algebras of operators [See also 46Lxx] |
| 47L05 | Linear spaces of operators [See also 46A32 and 46B28] |
| 47L07 | Convex sets and cones of operators [See also 46A55] |
| 47L10 | Algebras of operators on Banach spaces and other topological linear spaces |
| 47L15 | Operator algebras with symbol structure |
| 47L20 | Operator ideals |
| 47L25 | Operator spaces (= matricially normed spaces) [See also 46L07] |
| 47L30 | Abstract operator algebras on Hilbert spaces |
| 47L35 | Nest algebras, CSL algebras |
| 47L40 | Limit algebras, subalgebras of $C^{*}$-algebras |
| 47L45 | Dual algebras; weakly closed singly generated operator algebras |
| 47L50 | Dual spaces of operator algebras |
| 47L55 | Representations of (nonselfadjoint) operator algebras |
| 47L60 | Algebras of unbounded operators; partial algebras of operators |
| 47L65 | Crossed product algebras (analytic crossed products) |
| 47L70 | Nonassociative nonselfadjoint operator algebras |
| 47L75 | Other nonselfadjoint operator algebras |
| 47L80 | Algebras of specific types of operators (Toeplitz, integral, pseudodifferential, etc.) |
| 47L90 | Applications of operator algebras to physics |
| 47L99 | None of the above, but in this section |

47Jxx Equations and inequalities involving nonlinear operators [See also 46Txx] \{For global and geometric aspects, see 58-XX $\}$
47J05 Equations involving nonlinear operators (general)
47J06
47J07

47J10
47J15

47J20

47J25

47J30
47J35

47J40
47J99
None of the above, but in this section
[See also 46Lxx]
47L05 Linear spaces of operators [See also 46A32 and 46B28]
47L07 Convex sets and cones of operators [See also 46A55]
47L10

47L15 Operator algebras with symbol structure
47L20 Operator ideals
47L25 Operator spaces (= matricially normed spaces) [See also 46L07]
Abstract operator algebras on Hilbert spaces
Nest algebras, CSL algebras

47L45 Dual algebras; weakly closed singly generated operator algebras
47L50 Dual spaces of operator algebras
47L55 Representations of (nonselfadjoint) operator algebras
47L60 Algebras of unbounded operators; partial algebras of operators
47L65 Crossed product algebras (analytic crossed products)
Nonassociative nonselfadjoint operator algebras
Other nonselfadjoint operator algebras
47L80 Algebras of specific types of operators (Toeplitz, integral, pseudodifferential, etc.)

47L99 None of the above, but in this section

| 47Nxx | Miscellaneous applications of operator theory [See also 46Nxx] |
| :---: | :---: |
| 47N10 | Applications in optimization, convex analysis, mathematical programming, economics |
| 47N20 | Applications to differential and integral equations |
| 47N30 | Applications in probability theory and statistics |
| 47N40 | Applications in numerical analysis [See also 65Jxx] |
| 47N50 | Applications in quantum physics |
| 47N55 | Applications in statistical physics |
| 47N60 | Applications in biology and other sciences |
| 47N70 | Applications in systems theory, circuits, etc. |
| 47N99 | None of the above, but in this section |
| 47Sxx | Other (nonclassical) types of operator theory [See also 46Sxx] |
| 47S10 | Operator theory over fields other than $\mathbf{R}, \mathbf{C}$ or the quaternions; non-Archimedean operator theory |
| 47S20 | Nonstandard operator theory [See also 03H05] |
| 47S30 | Constructive operator theory [See also 03F60] |
| 47S40 | Fuzzy operator theory [See also 03E72] |
| 47S50 | Operator theory in probabilistic metric linear spaces |
| 47S99 | None of the above, but in this section |
| 49-XX | CALCULUS OF VARIATIONS AND OPTIMAL CONTROL; OPTIMIZATION [See also 34H05, 34K35, 65Kxx, 90Cxx, 93-XX] |
| 49-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 49-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 49-02 | Research exposition (monographs, survey articles) |
| 49-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 49-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 49-06 | Proceedings, conferences, collections, etc. |
| 49Jxx | Existence theories |
| 49J05 | Free problems in one independent variable |
| 49J10 | Free problems in two or more independent variables |
| 49J15 | Optimal control problems involving ordinary differential equations |
| 49J20 | Optimal control problems involving partial differential equations |
| 49J22 | Optimal control problems involving integral equations |
| 49J24 | Optimal control problems involving differential inclusions [See also 34A60] |
| 49J25 | Optimal control problems involving equations with retarded arguments [See also 34K35] |
| 49J27 | Problems in abstract spaces [See also 90C48, 93C25] |
| 49J30 | Optimal solutions belonging to restricted classes <br> (Lipschitz controls, bang-bang controls, etc.) |
| 49J35 | Minimax problems |

Miscellaneous applications of operator theory [See also 46Nxx]
Applications in optimization, convex analysis, mathematical programming, economics
x
Applications in probability theory and statistics

Applications in numerical analysis
[See also 65Jxx]
Applications in quantum physics
Applications in statistical physics
Applications in biology and other sciences
Applications in systems theory, circuits, etc.
None of the above, but in this section
[See also 46Sxx]
Operator theory over fields other than $\mathbf{R}, \mathbf{C}$ or quaternions, non-Archimedean operator theory
47S20 Nonstandard operator theory [See also 03H05]
47S30 Constructive operator theory [See also 03F60]
47S40 Fuzzy operator theory [See also 03E72]
47S50 Operator theory in probabilistic metric linear spaces
47S99 None of the above, but in this section

## 49-XX CALCULUS OF VARIATIONS AND

OPTIMAL CONTROL; OPTIMIZATION [See also 34 H 05 , 34 K 35 , 65 Kxx , 90 Cxx , 93-XX] bibliographies, etc.) papers, etc.)
49-02
Research exposition (monographs, survey articles)
Historical (must also be assigned at least one classification number from Section 01)
the theory of computation or programming)
Proceedings, conferences, collections, etc.
Existence theories
Free problems in one independent variable
Free problems in two or more independent
Optimal control problems involving ordinary differential equations
Optimal control problems involving partial differential equations
Optimal control problems involving integral equations
Optimal control problems involving differentia Option [See so 34A60] with retarded arguments [See also 34K35]
Problems in abstract spaces [See also 90C48, 93C25]
Optimal solutions belonging to restricted classes (Lipschitz controls, bang-bang controls, etc.)
Minimax problems

| 49J40 | Variational methods including variational inequalities [See also 47J20] | 49N30 | Problems with incomplete information [See also 93C41] |
| :---: | :---: | :---: | :---: |
| 49J45 | Methods involving semicontinuity and | 49N35 | Optimal feedback synthesis [See also 93B52] |
|  | convergence; relaxation | 49N45 | Inverse problems |
| 49J50 | Fréchet and Gateaux differentiability | 49N60 | Regularity of solutions |
|  | [See also 46G05, 58C20] | 49N70 | Differential games |
| 49 J 52 | Nonsmooth analysis [See also 46G05, 58C50] | 49N75 | Pursuit and evasion games |
| 49J53 | Set-valued and variational analysis [See also 28B20, 47H04, 54C60, 58C06] | 49N90 | Applications of optimal control and differential games [See also 90C90, 93C95] |
| 49 J 55 | Problems involving randomness [See also 93E20] | 49N99 | None of the above, but in this section |
| 49J99 | None of the above, but in this section | 49Qxx | Manifolds [See also 58Exx] |
| 49Kxx | Necessary conditions and sufficient conditions | 49Q05 | Minimal surfaces [See also 53A10, 58E12] |
|  | for optimality | 49Q10 | Optimization of shapes other than minimal |
| 49K05 | Free problems in one independent variable |  | surfaces [See also 90C90] |
| 49K10 | Free problems in two or more independent | 49Q12 | Sensitivity analysis |
|  | variables | 49Q15 | Geometric measure and integration theory, |
| 49K15 | Problems involving ordinary differential equations |  | integral and normal currents [See also 28A75, |
| 49K20 | Problems involving partial differential equations |  | 32C30, 58A25, 58C35] |
| 49K22 | Problems involving integral equations | 49Q20 | Variational problems in a geometric measure- |
| 49K24 | Problems involving differential inclusions |  | theoretic setting |
|  | [See also 34A60] | 49Q99 | None of the above, but in this section |
| 49K25 | Problems involving equations with retarded arguments [See also 34K35] | 49 R 50 | Variational methods for eigenvalues of operators [See also 47A75] |
| 49K27 | Problems in abstract spaces [See also 90C48, | 49S05 | Variational principles of physics |
|  | 93C25] | 51-XX | GEOMETRY \{For algebraic geometry, see |
| 49K30 | Optimal solutions belonging to restricted classes |  | $\mathbf{1 4 - X X}\}$ |
| 49K35 | Minimax problems | 51-00 | General reference works (handbooks, dictionaries, |
| 49K40 | Sensitivity, stability, well-posedness [See also 90C31] | 51-01 | bibliographies, etc.) <br> Instructional exposition (textbooks, tutorial |
| 49K45 | Problems involving randomness [See also 93E20] |  | papers, etc.) |
| 49K99 | None of the above, but in this section | 51-02 | Research exposition (monographs, survey articles) |
| 49Lxx | Hamilton-Jacobi theories, including dynamic programming | 51-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 49L20 | Dynamic programming method | 51-04 | Explicit machine computation and programs (not |
| 49L25 | Viscosity solutions |  | the theory of computation or programming) |
| 49L99 | None of the above, but in this section | 51-06 | Proceedings, conferences, collections, etc. |
| 49Mxx | Methods of successive approximations | 51Axx | Linear incidence geometry |
|  | [See also 90Cxx, 65Kxx] | 51A05 | General theory and projective geometries |
| 49M05 | Methods based on necessary conditions | 51 A 10 | Homomorphism, automorphism and dualities |
| 49M15 | Methods of Newton-Raphson, Galerkin and Ritz | 51 A 15 | Structures with parallelism |
|  | types | 51A20 | Configuration theorems |
| 49M20 | Methods of relaxation type | 51 A 25 | Algebraization [See also 12Kxx, 20N05] |
| 49M25 | Discrete approximations | 51 A 30 | Desarguesian and Pappian geometries |
| 49M27 | Decomposition methods | 51 A 35 | Non-Desarguesian affine and projective planes |
| 49M29 | Methods involving duality | 51A40 | Translation planes and spreads |
| 49M30 | Other methods, not based on necessary conditions (penalty function, etc.) | 51A45 | Incidence structures imbeddable into projective geometries |
| 49M37 | Methods of nonlinear programming type [See also 90C30, 65Kxx] | 51A50 | Polar geometry, symplectic spaces, orthogonal spaces |
| 49M99 | None of the above, but in this section | 51A99 | None of the above, but in this section |
| 49Nxx | Miscellaneous topics | 51Bxx | Nonlinear incidence geometry |
| 49N05 | Linear optimal control problems | 51B05 | General theory |
|  | [See also 93C05] | 51B10 | Möbius geometries |
| 49N10 | Linear-quadratic problems | 51B15 | Laguerre geometries |
| 49N15 | Duality theory | 51B20 | Minkowski geometries |
| 49N20 | Periodic optimization | 51B25 | Lie geometries |
| 49N25 | Impulsive optimal control problems | 51B99 | None of the above, but in this section |


| 51C05 | Ring geometry (Hjelmslev, Barbilian, etc.) |
| :--- | :--- |
| 51Dxx | Geometric closure systems |
| 51D05 | Abstract (Maeda) geometries |
| 51D10 | Abstract geometries with exchange axiom |
| 51D15 | Abstract geometries with parallelism |
| 51D20 | Combinatorial geometries [See also 05B25, <br> 05B35] |
| 51D25 | Lattices of subspaces [See also 05B35] |
| 51D30 | Continuous geometries and related topics |
|  | [See also 06Cxx] |

51J99 None of the above, but in this section

51Kxx
51K05
51K10
51K99
51Lxx
51L05
51L10
51L15
51L20
51L99
51Mxx
51M04
51M05

51M09

51M10
51M15
51M16 Inequalities and extremum problems \{For convex problems, see 52A40\}
51M20

51M25
51M30
51M35

51M99
51Nxx
51N05
51N10
51N15
51N20
51N25 Analytic geometry with other transformation
51N30 $\begin{aligned} & \text { groups } \\ & \text { Geometry of classical groups [See also 20Gxx, }\end{aligned}$
$51 \mathrm{~N} 30 \quad \begin{aligned} & \text { groups } \\ & \text { Geometry of classical groups [See also 20Gxx, }\end{aligned}$ 14L35]
51N35 Questions of classical algebraic geometry [See also 14 Nxx ]
51N99 None of the above, but in this section
51P05 Geometry and physics (should also be assigned
at least one other classification number from Sections 70-86)
52-XX CONVEX AND DISCRETE GEOMETRY
52-00 General reference works (handbooks, dictionaries, bibliographies, etc.)
52-01 Instructional exposition (textbooks, tutorial papers, etc.)
52-02
52-03

52-04

## Distance geometry

General theory
Synthetic differential geometry
None of the above, but in this section
Geometric order structures [See also 53C75]
Geometry of orders of nondifferentiable curves
Directly differentiable curves
$n$-vertex theorems via direct methods
Geometry of orders of surfaces
None of the above, but in this section
Real and complex geometry
Elementary problems in Euclidean geometries
Euclidean geometries (general) and generalizations
Elementary problems in hyperbolic and elliptic geometries
Hyperbolic and elliptic geometries (general) and generalizations
Geometric constructions

Polyhedra and polytopes; regular figures, division of spaces [See also 51F15]
Length, area and volume [See also 26B15]
Line geometries and their generalizations
[See also 53A25]
Synthetic treatment of fundamental manifolds
in projective geometries (Grassmannians,
Veronesians and their generalizations)
[See also 14M15]
None of the above, but in this section
Analytic and descriptive geometry
Descriptive geometry [See also 65D17, 68U07]
Affine analytic geometry
Projective analytic geometry
Euclidean analytic geometry

Research exposition (monographs, survey articles)
Historical (must also be assigned at least one classification number from Section 01)
Explicit machine computation and programs (not the theory of computation or programming)

| 52-06 | Proceedings, conferences, collections, etc. |
| :---: | :---: |
| 52Axx | General convexity |
| 52A01 | Axiomatic and generalized convexity |
| 52 A 05 | Convex sets without dimension restrictions |
| 52 A 07 | Convex sets in topological vector spaces [See also 46A55] |
| 52A10 | Convex sets in 2 dimensions (including convex curves) [See also 53A04] |
| 52A15 | Convex sets in 3 dimensions (including convex surfaces) [See also 53A05, 53C45] |
| 52A20 | Convex sets in $n$ dimensions (including convex hypersurfaces) [See also 53A07, 53C45] |
| 52A21 | Finite-dimensional Banach spaces (including special norms, zonoids, etc.) [See also 46Bxx] |
| 52A22 | Random convex sets and integral geometry [See also 53C65, 60D05] |
| 52A27 | Approximation by convex sets |
| 52A30 | Variants of convex sets (star-shaped, $(m, n)$ convex, etc.) |
| 52A35 | Helly-type theorems and geometric transversal theory |
| 52 A 37 | Other problems of combinatorial convexity |
| 52A38 | Length, area, volume [See also 26B15, 28A75, 49 Q 20 ] |
| 52A39 | Mixed volumes and related topics |
| 52 A 40 | Inequalities and extremum problems |
| 52A41 | Convex functions and convex programs [See also 26B25, 90C25] |
| 52A55 | Spherical and hyperbolic convexity |
| 52A99 | None of the above, but in this section |
| 52Bxx | Polytopes and polyhedra |
| 52B05 | Combinatorial properties (number of faces, shortest paths, etc.) [See also 05Cxx] |
| 52B10 | Three-dimensional polytopes |
| 52B11 | $n$-dimensional polytopes |
| 52B12 | Special polytopes (linear programming, centrally symmetric, etc.) |
| 52B15 | Symmetry properties of polytopes |
| 52B20 | Lattice polytopes (including relations with commutative algebra and algebraic geometry) [See also 06A11, 13F20, 13Hxx] |
| 52B22 | Shellability |
| 52B35 | Gale and other diagrams |
| 52B40 | Matroids (realizations in the context of convex polytopes, convexity in combinatorial structures, etc.) [See also 05B35, 52Cxx] |
| 52B45 | Dissections and valuations (Hilbert's third problem, etc.) |
| 52B55 | Computational aspects related to convexity \{For computational geometry and algorithms, see 68Q25, 68U05; for numerical algorithms, see $65 \mathrm{Yxx}\}$ [See also 68Uxx] |
| 52B60 | Isoperimetric problems for polytopes |
| 52B70 | Polyhedral manifolds |
| 52B99 | None of the above, but in this section |
| 52Cxx | Discrete geometry |
| 52C05 | Lattices and convex bodies in 2 dimensions [See also 11H06, 11H31, 11P21] |

52C07
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53-06
53Axx
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53A10

53A15
53A17
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53A35
53A40
53A45

53A60
53A99
53Bxx
53B05
53B10

52C45 Combinatorial complexity of geometric structures [See also 68U05]

53A07 Higher-dimensional and -codimensional surfaces in Euclidean $n$-space

53A55 Differential invariants (local theory), geometric objects
Lattices and convex bodies in $n$ dimensions [See also 11H06, 11H31, 11P21]
Erdős problems and related topics of discrete geometry [See also 11 Hxx ]
Packing and covering in 2 dimensions [See also 05B40, 11H31]
Packing and covering in $n$ dimensions [See also 05B40, 11H31]
Tilings in 2 dimensions [See also 05B45, 51M20] Tilings in $n$ dimensions [See also 05B45, 51M20] Quasicrystals, aperiodic tilings Rigidity and flexibility of structures [See also 70B15]
Circle packings and discrete conformal geometry
Planar arrangements of lines and pseudolines
Arrangements of points, flats, hyperplanes
[See also 32S22]
Oriented matroids

None of the above, but in this section
DIFFERENTIAL GEOMETRY \{For differential topology, see 57Rxx. For foundational questions of differentiable manifolds, see 58Axx
General reference works (handbooks, dictionaries, bibliographies, etc.)
Instructional exposition (textbooks, tutorial papers, etc.)
Research exposition (monographs, survey articles)
Historical (must also be assigned at least one classification number from Section 01)
Explicit machine computation and programs (not
the theory of computation or programming)
Proceedings, conferences, collections, etc.
Classical differential geometry
Curves in Euclidean space
Surfaces in Euclidean space

Minimal surfaces, surfaces with prescribed mean
curvature [See also 49Q05, 49Q10, 53C42]
Affine differential geometry

## Kinematics

Projective differential geometry
Differential line geometry
Conformal differential geometry
Non-Euclidean differential geometry
Other special differential geometries
Vector and tensor analysis

Geometry of webs [See also 14C21, 20N05]
None of the above, but in this section

## Local differential geometry

Linear and affine connections
Projective connections

| 53B15 | Other connections | 53C60 | Finsler spaces and generalizations (areal metrics) [See also 58B20] |
| :---: | :---: | :---: | :---: |
| 53B20 | Local Riemannian geometry |  |  |
| 53B21 | Methods of Riemannian geometry | $53 \mathrm{C65}$ | Integral geometry [See also 52A22, |
| 53B25 | Local submanifolds [See also 53C40] |  | 60D05]; differential forms, currents, etc. |
| 53B30 | Lorentz metrics, indefinite metrics |  | [See mainly 58Axx] |
| 53B35 | Hermitian and Kählerian structures | 53C70 | Direct methods ( $G$-spaces of Busemann, etc.) |
|  | [See also 32Cxx] | 53 C 75 | Geometric orders, order geometry |
| 53B40 | Finsler spaces and generalizations (areal metrics) |  | [See also 51Lxx] |
| 53B50 | Applications to physics | 53 C 80 | Applications to physics |
| 53B99 | None of the above, but in this section | 53 C 99 | None of the above, but in this section |
| 53Cxx | Global differential geometry [See also 51 H 25 , 58-XX; for related bundle theory, see 55Rxx, | 53Dxx | Symplectic geometry, contact geometry [See also 37Jxx, 70Gxx, 70Hxx] |
|  | $57 \mathrm{Rxx}]$ | 53D05 | Symplectic manifolds, general |
| 53C05 | Connections, general theory | 53D10 | Contact manifolds, general |
| 53C07 | Special connections and metrics on vector | 53D12 | Lagrangian submanifolds; Maslov index |
|  | bundles (Hermite-Einstein-Yang-Mills) | 53D15 | Almost contact and almost symplectic manifolds |
|  | [See also 32Q20] | 53D17 | Poisson manifolds |
| 53C10 | $G$-structures | 53D20 | Momentum maps; symplectic reduction |
| 53 C 12 | Foliations (differential geometric aspects) | 53D22 | Canonical transformations |
|  | [See also 57R30, 57R32] | 53D25 | Geodesic flows |
| 53C15 | General geometric structures on manifolds | 53D30 | Symplectic structures of moduli spaces |
|  | (almost complex, almost product structures, etc.) | 53D35 | Global theory of symplectic and contact |
| 53 C 17 | Sub-Riemannian geometry |  | manifolds [See also 57Rxx] |
| 53C20 | Global Riemannian geometry, including pinching [See also 31C12, 58B20] | 53D40 | Floer homology and cohomology, symplectic aspects |
| 53C21 | Methods of Riemannian geometry, including PDE methods; curvature restrictions [See also 58J60] | 53D45 | Gromov-Witten invariants, quantum cohomology, Frobenius manifolds [See also 14N35] |
| 53C22 | Geodesics [See also 58E10] | 53D50 | Geometric quantization |
| 53C23 | Global topological methods (à la Gromov) | 53D55 | Deformation quantization, star products |
| 53 C 24 | Rigidity results | 53D99 | None of the above, but in this section |
| 53C25 | Special Riemannian manifolds (Einstein, | 53Z05 | Applications to physics |
| 53C26 | Sasakian, etc.) <br> Hyper-Kähler and quaternionic Kähler geometry, "special" geometry | 54-XX 54-00 | GENERAL TOPOLOGY \{For the topology of manifolds of all dimensions, see 57 Nxx$\}$ General reference works (handbooks, dictionaries, |
| 53 C 27 | Spin and Spin ${ }^{c}$ geometry |  | bibliographies, etc.) |
| 53 C 28 | Twistor methods [See also 32L25] | 54-01 | Instructional exposition (textbooks, tutorial |
| 53 C 29 | Issues of holonomy |  | papers, etc.) |
| 53C30 | Homogeneous manifolds [See also 14M15, | 54-02 | Research exposition (monographs, survey articles) |
|  | 14M17, 32M10, 57T15] | 54-03 | Historical (must also be assigned at least one |
| 53C35 | Symmetric spaces [See also 32M15, 57T15] |  | classification number from Section 01) |
| 53 C 38 | Calibrations and calibrated geometries | 54-04 | Explicit machine computation and programs (not |
| 53 C 40 | Global submanifolds [See also 53B25] |  | the theory of computation or programming) |
| 53C42 | Immersions (minimal, prescribed curvature, tight, | 54-06 | Proceedings, conferences, collections, etc. |
|  | etc.) [See also 49Q05, 49Q10, 53A10, 57R40, | 54Axx | Generalities |
|  | 57R42] | 54A05 | Topological spaces and generalizations (closure |
| 53C43 | Differential geometric aspects of harmonic maps [See also 58E20] | 54A1 | spaces, etc.) <br> Several topologies on one set (change of |
| 53C44 | Geometric evolution equations (mean curvature flow) |  | topology, comparison of topologies, lattices of topologies) |
| 53C45 | Global surface theory (convex surfaces à la A. D. | 54A15 | Syntopogeneous structures |
|  | Aleksandrov) | 54A20 | Convergence in general topology (sequences, |
| 53C50 | Lorentz manifolds, manifolds with indefinite metrics | 54A25 | filters, limits, convergence spaces, etc.) Cardinality properties (cardinal functions and |
| 53C55 | Hermitian and Kählerian manifolds [See also 32Cxx] |  | inequalities, discrete subsets) [See also 03Exx] \{For ultrafilters, see 54D80\} |
| 53C56 | Other complex differential geometry [See also 32Cxx] | 54A35 | Consistency and independence results [See also 03E35] |


| 54A40 | Fuzzy topology [See also 03E72] |
| :---: | :---: |
| 54A99 | None of the above, but in this section |
| 54Bxx | Basic constructions |
| 54B05 | Subspaces |
| 54B10 | Product spaces |
| 54B15 | Quotient spaces, decompositions |
| 54B17 | Adjunction spaces and similar constructions |
| 54B20 | Hyperspaces |
| 54B30 | Categorical methods [See also 18B30] |
| 54B35 | Spectra |
| 54B40 | Presheaves and sheaves [See also 18F20] |
| 54B99 | None of the above, but in this section |
| 54Cxx | Maps and general types of spaces defined by maps |
| 54C05 | Continuous maps |
| 54C08 | Weak and generalized continuity |
| 54C10 | Special maps on topological spaces (open, closed, perfect, etc.) |
| 54C15 | Retraction |
| 54C20 | Extension of maps |
| 54C25 | Embedding |
| 54C30 | Real-valued functions [See also 26-XX] |
| 54C35 | Function spaces [See also 46Exx, 58D15] |
| 54C40 | Algebraic properties of function spaces [See also 46J10] |
| 54C45 | $C$ - and $C^{*}$-embedding |
| 54C50 | Special sets defined by functions [See also 26A21] |
| 54C55 | Absolute neighborhood extensor, absolute extensor, absolute neighborhood retract (ANR), absolute retract spaces (general properties) [See also 55M15] |
| 54C56 | Shape theory [See also 55P55, 57N25] |
| 54C60 | Set-valued maps [See also 26E25, 28B20, 47H04, 58C06] |
| 54C65 | Selections [See also 28B20] |
| 54C70 | Entropy |
| 54C99 | None of the above, but in this section |
| 54Dxx | Fairly general properties |
| 54D05 | Connected and locally connected spaces (general aspects) |
| 54D10 | Lower separation axioms ( $T_{0}-T_{3}$, etc.) |
| 54D15 | Higher separation axioms (completely regular, normal, perfectly or collectionwise normal, etc.) |
| 54D20 | Noncompact covering properties (paracompact, Lindelöf, etc.) |
| 54D25 | " $P$-minimal" and " $P$-closed" spaces |
| 54D30 | Compactness |
| 54D35 | Extensions of spaces (compactifications, supercompactifications, completions, etc.) |
| 54D40 | Remainders |
| 54D45 | Local compactness, $\sigma$-compactness |
| 54D50 | $k$-spaces |
| 54D55 | Sequential spaces |
| 54D60 | Realcompactness and realcompactification |
| 54D65 | Separability |
| 54D70 | Base properties |

54A99 None of the above, but in this section
54Bxx Basic constructions
54B05 Subspaces
54B15 Quotient spaces, decompositions
54 B 17 Adjunction spaces and similar constructions
54B30 Categorical methods [See also 18B30]
54B35 Spectra
54B40 Presheaves and sheaves [See also 18F20]
54B99 None of the above, but in this section
54Cxx Maps and general types of spaces defined by
54C05 Continuous maps
54C08 Weak and generalized continuity
54C10 Special maps on topological spaces (open, closed, perfect, etc.)

54C20 Extension of maps
54C25 Embedding
54 Real-valued functions [See also 26-XX]
$54 \mathrm{C} 40^{-}$Algebraic properties of function spaces
[See also 46J10]
54C45 $\quad C$ - and $C^{*}$-embedding
54C50 Special sets defined by functions
[See also 26A21]
54C55 Absolute neighborhood extensor, absolute
extensor, absolute neighborhood retract (ANR),
absolute retract spaces (general properties)
[See also 55M15]
54 C 56 Shape theory [See also 55P55, 57N25]
5 . Set-valued maps [See also 26E25, 28B20, 47H04, 58C06]
54C65 Selections [See also 28B20]
54C70 Entropy
54C99 None of the above, but in this section
54Dxx Fairly general properties
54D05 Connected and locally connected spaces (general
54D10 Lower separation axioms ( $T_{0}-T_{3}$, etc.)
54D15 Higher separation axioms (completely regular,
54D20 Noncompact covering properties (paracompact,
Lindelöf, etc.)
54D25 $P$-minimal" and " $P$-closed" spaces
54D35 Extensions of spaces (compactifications,
54D40 Remainders
54D45 Local compactness, $\sigma$-compactness
54D50 $k$-spaces
54D55 Sequential spaces
54D60 Realcompactness and realcompactification
54D70 Base properties

54D80

54D99
54Exx
54E05
54E15
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54E18
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54E35
54E40
54E45
54E50
54E52
54E55
54E70
54E99
54Fxx
54F05

54F15
54F35

54F45
54F50

54F55
54F65
54F99
54Gxx
54G05
54G10
54G12
54G15
54G20
54G99
54Hxx
54H05

54 H 10
54H11
54 H 12
54H13
54H15
54H20
54H25

54H99
54J05

Special constructions of spaces (spaces of ultrafilters, etc.)
None of the above, but in this section
Spaces with richer structures
Proximity structures and generalizations
Uniform structures and generalizations
Nearness spaces
$p$-spaces, $M$-spaces, $\sigma$-spaces, etc.
Stratifiable spaces, cosmic spaces, etc.
Semimetric spaces
Moore spaces
Metric spaces, metrizability
Special maps on metric spaces
Compact (locally compact) metric spaces
Complete metric spaces
Baire category, Baire spaces
Bitopologies
Probabilistic metric spaces
None of the above, but in this section

## Special properties

Linearly ordered topological spaces, generalized ordered spaces, and partially ordered spaces
[See also 06B30, 06F30]
Continua and generalizations
Higher-dimensional local connectedness
[See also 55Mxx, 55Nxx]
Dimension theory [See also 55M10]
Spaces of dimension $\leq 1$; curves, dendrites [See also 26A03]
Unicoherence, multicoherence
Topological characterizations of particular spaces
None of the above, but in this section
Peculiar spaces
Extremally disconnected spaces, $F$-spaces, etc.
$P$-spaces
Scattered spaces
Pathological spaces
Counterexamples
None of the above, but in this section

## Connections with other structures, applications

Descriptive set theory (topological aspects
of Borel, analytic, projective, etc. sets)
[See also 03E15, 26A21, 28A05]
54 H 10 Topological representations of algebraic systems [See also 22-XX]
Topological groups [See also 22A05]
Topological lattices, etc. [See also 06B30, 06F30]
Topological fields, rings, etc. [See also 12Jxx]
\{For algebraic aspects, see 13Jxx, 16W80\}
Transformation groups and semigroups
[See also 20M20, 22-XX, 57Sxx]
Topological dynamics [See also 28Dxx, 37Bxx]
Fixed-point and coincidence theorems
[See also 47H10, 55M20]
None of the above, but in this section
Nonstandard topology [See also 03H05]

| 55-XX | ALGEBRAIC TOPOLOG |
| :---: | :---: |
| 55-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 55-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 55-02 | Research exposition (monographs, survey articles) |
| 55-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 55-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 55-06 | Proceedings, conferences, collections, etc. |
| 55Mxx | Classical topics \{For the topology of Euclidean spaces and manifolds, see $\mathbf{5 7 N x x}\}$ |
| 55M05 | Duality |
| 55M10 | Dimension theory [See also 54F45] |
| 55M15 | Absolute neighborhood retracts [See also 54C55] |
| 55M20 | Fixed points and coincidences [See also 54H25] |
| 55M25 | Degree, winding number |
| 55M30 | Ljusternik-Schnirelman (Lyusternik-Shnirel'man) category of a space |
| 55M35 | Finite groups of transformations (including Smith theory) [See also 57S17] |
| 55M99 | None of the above, but in this section |
| 55Nxx | Homology and cohomology theories [See also 57Txx] |
| 55N05 | Čech types |
| 55N07 | Steenrod-Sitnikov homologies |
| 55N10 | Singular theory |
| 55N15 | $K$-theory [See also 19Lxx] \{For algebraic $K$ theory, see 18F25, 19-XX\} |
| 55N20 | Generalized (extraordinary) homology and cohomology theories |
| 55N22 | Bordism and cobordism theories, formal group laws [See also 14L05, 19L41, 57R75, 57R77, 57R85, 57R90] |
| 55N25 | Homology with local coefficients, equivariant cohomology |
| 55N30 | Sheaf cohomology [See also 18F20, 32C35, 32L10] |
| 55N33 | Intersection homology and cohomology |
| 55N34 | Elliptic cohomology |
| 55N35 | Other homology theories |
| 55N40 | Axioms for homology theory and uniqueness theorems |
| 55N45 | Products and intersections |
| 55N91 | Equivariant homology and cohomology [See also 19L47] |
| 55N99 | None of the above, but in this section |
| 55Pxx | Homotopy theory \{For simple homotopy type, see 57 Q 10$\}$ |
| 55P05 | Homotopy extension properties, cofibrations |
| 55P10 | Homotopy equivalences |
| 55P15 | Classification of homotopy type |
| 55P20 | Eilenberg-Mac Lane spaces |
| 55P25 | Spanier-Whitehead duality |
| 55P30 | Eckmann-Hilton duality |
| 55P35 | Loop spaces |
| 55 P 40 | Suspensions |

55P42
55P43
55P45
55P47
55P48
55P55
55P57
55P60
55P62
55P65
55P91
55P92

55P99
55Qxx
55Q05

55Q07
55Q10
55Q15
55Q20
55Q25
55Q35
55Q40
55Q45
55Q50
55Q51
55Q52
55Q55
55Q70
55Q91
55Q99
55Rxx

55R05
55R10
55R12
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55R25
55R35
55R37
55R40

55R45

55R50

55R55
55R60

55R65
55R70

Stable homotopy theory, spectra
Spectra with additional structure ( $E_{\infty}, A_{\infty}$, ring spectra, etc.)
$H$-spaces and duals
Infinite loop spaces
Loop space machines, operads [See also 18D50]
Shape theory [See also 54C56, 55Q07]
Proper homotopy theory
Localization and completion
Rational homotopy theory
Homotopy functors
Equivariant homotopy theory [See also 19L47]
Relations between equivariant and nonequivariant
homotopy theory
None of the above, but in this section
Homotopy groups
Homotopy groups, general; sets of homotopy classes
Shape groups
Stable homotopy groups
Whitehead products and generalizations
Homotopy groups of wedges, joins, and simple spaces
Hopf invariants
Operations in homotopy groups
Homotopy groups of spheres
Stable homotopy of spheres
$J$-morphism [See also 19L20]
$v_{n}$-periodicity
Homotopy groups of special spaces
Cohomotopy groups
Homotopy groups of special types
[See also 55N05, 55N07]
Equivariant homotopy groups [See also 19L47]
None of the above, but in this section
Fiber spaces and bundles [See also 18F15, 32Lxx, 46M20, 57R20, 57R22, 57R25]
Fiber spaces
Fiber bundles
Transfer
Classification
Spectral sequences and homology of fiber spaces [See also 55Txx]
Sphere bundles and vector bundles
Classifying spaces of groups and $H$-spaces
Maps between classifying spaces
Homology of classifying spaces, characteristic
classes [See also 57Txx, 57R20]
Homology and homotopy of $B \mathrm{O}$ and $B \mathrm{U}$; Bott periodicity
Stable classes of vector space bundles, $K$-theory
[See also 19Lxx] \{For algebraic $K$-theory, see
18F25, 19-XX
Fiberings with singularities
Microbundles and block bundles
[See also 57N55, 57Q50]
Generalizations of fiber spaces and bundles
Fibrewise topology

| 55R80 | Discriminantal varieties, configuration spaces | 57M07 | Topological methods in group theory |
| :---: | :---: | :---: | :---: |
| 55R91 | Equivariant fiber spaces and bundles | 57M10 | Covering spaces |
|  | [See also 19L47] | 57M12 | Special coverings, e.g. branched |
| 55R99 | None of the above, but in this section | 57M15 | Relations with graph theory [See also 05Cxx] |
| 55Sxx | Operations and obstructions | 57M20 | Two-dimensional complexes |
| 55S05 | Primary cohomology operations | 57M25 | Knots and links in $S^{3}$ \{For higher dimensions, |
| 55S10 | Steenrod algebra |  | see 57Q45\} |
| 55S12 | Dyer-Lashof operations | 57M27 | Invariants of knots and 3-manifolds |
| 55S15 | Symmetric products, cyclic products | 57M30 | Wild knots and surfaces, etc., wild embeddings |
| 55S20 | Secondary and higher cohomology operations | 57M35 | Dehn's lemma, sphere theorem, loop theorem, |
| 55S25 | $K$-theory operations and generalized cohomology operations [See also 19D55, 19Lxx] | 57M40 | asphericity <br> Characterizations of $E^{3}$ and $S^{3}$ (Poincaré |
| 55S30 | Massey products |  | conjecture) [See also 57N12] |
| 55S35 | Obstruction theory | 57M50 | Geometric structures on low-dimensional |
| 55S36 | Extension and compression of mappings |  | manifolds |
| 55S37 | Classification of mappings | 57M60 | Group actions in low dimensions |
| 55S40 | Sectioning fiber spaces and bundles | 57M99 | None of the above, but in this section |
| 55S45 | Postnikov systems, $k$-invariants | 57Nxx | Topological manifolds |
| 55S91 | Equivariant operations and obstructions | 57N05 | Topology of $E^{2}$, 2-manifolds |
|  | [See also 19L47] | 57N10 | Topology of general 3-manifolds |
| 55S99 | None of the above, but in this section |  | [See also 57Mxx] |
| 55Txx | Spectral sequences [See also 18G40, 55R20] | 57N12 | Topology of $E^{3}$ and $S^{3}$ [See also 57M40] |
| 55 T 05 | General | 57N13 | Topology of $E^{4}, 4$-manifolds [See also 14Jxx, |
| 55 T 10 | Serre spectral sequences |  | 32Jxx] |
| 55 T 15 | Adams spectral sequences | 57N15 | Topology of $E^{n}$, $n$-manifolds ( $4<n<\infty$ ) |
| 55 T 20 | Eilenberg-Moore spectral sequences [See also 57T35] | 57N16 | Geometric structures on manifolds [See also 57M50] |
| 55 T 25 | Generalized cohomology | 57N17 | Topology of topological vector spaces |
| 55 T 99 | None of the above, but in this section | 57N20 | Topology of infinite-dimensional manifolds |
| 55Uxx | Applied homological algebra and category theory [See also 18Gxx] | 57N25 | [See also 58Bxx] Shapes [See also 54C56, 55P55, 55Q07] |
| 55U05 | Abstract complexes | 57N30 | Engulfing |
| 55U10 | Simplicial sets and complexes | 57N35 | Embeddings and immersions |
| 55U15 | Chain complexes | 57N37 | Isotopy and pseudo-isotopy |
| 55U20 | Universal coefficient theorems, Bockstein | 57N40 | Neighborhoods of submanifolds |
|  | operator | 57N45 | Flatness and tameness |
| 55U25 | Homology of a product, Künneth formula | 57N50 | $S^{n-1} \subset E^{n}$, Schoenflies problem |
| 55 U 30 | Duality | 57N55 | Microbundles and block bundles [See also 55R60 57050] |
| 55U35 | Abstract and axiomatic homotopy theory | 57N60 | Cellularity |
| 55U40 | Topological categories, foundations of homotopy theory | 57 N 60 57 N 65 | Algebraic topology of manifolds |
| 55U99 | None of the above, but in this section | 57 N 70 | Cobordism and concordance |
| 57-XX | MANIFOLDS AND CELL COMPLEXES | 57N80 | Stratifications |
|  | \{For complex manifolds, see 32Qxx\} | 57N99 | None of the above, but in this section |
| 57-00 | General reference works (handbooks, dictionaries, | 57Pxx | Generalized manifolds [See also 18F15] |
|  | bibliographies, etc.) | 57P05 | Local properties of generalized manifolds |
| 57-01 | Instructional exposition (textbooks, tutorial | 57P10 | Poincaré duality spaces |
|  | papers, etc.) | 57P99 | None of the above, but in this section |
| 57-02 | Research exposition (monographs, survey articles) | 57Qxx | PL-topology |
| 57-03 | Historical (must also be assigned at least one | 57Q05 | General topology of complexes |
|  | classification number from Section 01) | 57Q10 | Simple homotopy type, Whitehead torsion, |
| 57-04 | Explicit machine computation and programs (not the theory of computation or programming) | 57 Q 12 | Reidemeister-Franz torsion, etc. [See also 19B28] Wall finiteness obstruction for CW-complexes |
| 57-06 | Proceedings, conferences, collections, etc. | 57Q15 | Triangulating manifolds |
| 57Mxx | Low-dimensional topology | 57Q20 | Cobordism |
| 57M05 | Fundamental group, presentations, free differential calculus | 57Q25 | Comparison of PL-structures: classification, Hauptvermutung |


| 57Q30 | Engulfing |
| :---: | :---: |
| 57Q35 | Embeddings and immersions |
| 57Q37 | Isotopy |
| 57Q40 | Regular neighborhoods |
| 57Q45 | Knots and links (in high dimensions) \{For the low-dimensional case, see 57M25\} |
| 57Q50 | Microbundles and block bundles [See also 55R60, 57N55] |
| 57Q55 | Approximations |
| 57Q60 | Cobordism and concordance |
| 57Q65 | General position and transversality |
| 57Q91 | Equivariant PL-topology |
| 57Q99 | None of the above, but in this section |
| 57Rxx | Differential topology \{For foundational questions of differentiable manifolds, see 58Axx; for infinite-dimensional manifolds, see 58Bxx $\}$ |
| 57R05 | Triangulating |
| 57R10 | Smoothing |
| 57R12 | Smooth approximations |
| 57R15 | Specialized structures on manifolds (spin manifolds, framed manifolds, etc.) |
| 57R17 | Symplectic and contact topology |
| 57R19 | Algebraic topology on manifolds |
| 57R20 | Characteristic classes and numbers |
| 57R22 | Topology of vector bundles and fiber bundles [See also 55Rxx] |
| 57R25 | Vector fields, frame fields |
| 57R27 | Controllability of vector fields on $C^{\infty}$ and realanalytic manifolds [See also 49Qxx, 37C10, 93B05] |
| 57R30 | Foliations; geometric theory |
| 57R32 | Classifying spaces for foliations; Gel'fand-Fuks cohomology [See also 58H10] |
| 57R35 | Differentiable mappings |
| 57R40 | Embeddings |
| 57R42 | Immersions |
| 57R45 | Singularities of differentiable mappings |
| 57R50 | Diffeomorphisms |
| 57R52 | Isotopy |
| 57R55 | Differentiable structures |
| 57R56 | Topological quantum field theories |
| 57R57 | Applications of global analysis to structures on manifolds, Donaldson and Seiberg-Witten invariants [See also 58-XX] |
| 57R58 | Floer homology |
| 57R60 | Homotopy spheres, Poincaré conjecture |
| 57R65 | Surgery and handlebodies |
| 57R67 | Surgery obstructions, Wall groups [See also 19J25] |
| 57R70 | Critical points and critical submanifolds |
| 57R75 | O- and SO-cobordism |
| 57R77 | Complex cobordism (U- and SU-cobordism) [See also 55N22] |
| 57R80 | $h$ - and $s$-cobordism |
| 57R85 | Equivariant cobordism |
| 57R90 | Other types of cobordism [See also 55N22] |
| 57R91 | Equivariant algebraic topology of manifolds |


| 57R95 | Realizing cycles by subm |
| :---: | :---: |
| 57R99 | None of the above, but in this section |
| 57Sxx | Topological transformation groups [See also 20F34, 22-XX, 37-XX, 54H15, 58D05] |
| 57S05 | Topological properties of groups of homeomorphisms or diffeomorphisms |
| 57S10 | Compact groups of homeomorphisms |
| 57S15 | Compact Lie groups of differentiable transformations |
| 57S17 | Finite transformation groups |
| 57S20 | Noncompact Lie groups of transformations |
| 57S25 | Groups acting on specific manifolds |
| 57S30 | Discontinuous groups of transformations |
| 57S99 | None of the above, but in this section |
| 57Txx | Homology and homotopy of topological groups and related structures |
| 57 T 05 | Hopf algebras [See also 16W30] |
| 57 T 10 | Homology and cohomology of Lie groups |
| 57 T 15 | Homology and cohomology of homogeneous spaces of Lie groups |
| 57 T 20 | Homotopy groups of topological groups and homogeneous spaces |
| 57 T 25 | Homology and cohomology of $H$-spaces |
| 57 T 30 | Bar and cobar constructions [See also 18G55, 55Uxx] |
| 57 T 35 | Applications of Eilenberg-Moore spectral sequences [See also 55R20, 55T20] |
| 57 T 99 | None of the above, but in this section |
| 58-XX | GLOBAL ANALYSIS, ANALYSIS ON MANIFOLDS [See also 32Cxx, 32Fxx, 32Wxx, 46-XX, 47Hxx, 53Cxx]\{For geometric integration theory, see 49Q15\} |
| 58-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 58-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 58-02 | Research exposition (monographs, survey articles) |
| 58-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 58-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 58-06 | Proceedings, conferences, collections, etc. |
| 58Axx | General theory of differentiable manifolds [See also 32Cxx] |
| 58A03 | Topos-theoretic approach to differentiable manifolds |
| 58A05 | Differentiable manifolds, foundations |
| 58A07 | Real-analytic and Nash manifolds [See also 14P20, 32C07] |
| 58A10 | Differential forms |
| 58A12 | de Rham theory [See also 14Fxx] |
| 58A14 | Hodge theory [See also 14C30, 14Fxx, 32J25, 32S35] |
| 58A15 | Exterior differential systems (Cartan theory) |
| 58A17 | Pfaffian systems |
| 58A20 | Jets |


| $\begin{aligned} & 58 \mathrm{~A} 25 \\ & 58 \mathrm{~A} 30 \end{aligned}$ | Currents [See also 32C30, 53C65] | 58D27 | Moduli problems for differential geometric structures <br> Moduli problems for topological structures |
| :---: | :---: | :---: | :---: |
|  | Vector distributions (subbundles of the tangent |  |  |
|  | bundles) | 58D29 |  |
| 58A32 | Natural bundles | 58D30 | Applications (in quantum mechanics (Feynman |
| 58A35 | Stratified sets [See also 32S60] |  | path integrals), relativity, fluid dynamics, etc.) |
| 58A40 | Differential spaces | 58D99 | None of the above, but in this section |
| 58A50 | Supermanifolds and graded manifolds [See also 14A22, 32C11] | 58Exx | Variational problems in infinite-dimensional spaces |
| 58A99 | None of the above, but in this section | 58E05 | Abstract critical point theory (Morse theory, |
| 58Bxx | Infinite-dimensional manifolds |  | Ljusternik-Schnirelman (Lyusternik-Shnirel'man) |
| 58B05 | Homotopy and topological questions |  | theory, etc.) |
| 58B10 | Differentiability questions | 58E07 | Abstract bifurcation theory |
| 58B12 | Questions of holomorphy [See also 32-XX, | 58E09 | Group-invariant bifurcation theory |
|  | 46G20] | 58E10 | Applications to the theory of geodesics (problems |
| 58B15 | Fredholm structures [See also 47A53] |  | in one independent variable) |
| 58B20 | Riemannian, Finsler and other geometric | 58E11 | Critical metrics |
|  | structures [See also 53C20, 53C60] | 58 E 12 | Applications to minimal surfaces (problems in |
| 58B25 | Group structures and generalizations on infinitedimensional manifolds [See also 22E65, 58D05] | 58E15 | two independent variables) [See also 49Q05] Application to extremal problems in |
| 58B32 | Geometry of quantum groups |  | several variables; Yang-Mills functionals |
| 58B34 | Noncommutative geometry (à la Connes) |  | [See also 81T13], etc. |
| 58B99 | None of the above, but in this section | 58 E 17 | Pareto optimality, etc., applications to economics |
| 58Cxx | Calculus on manifolds; nonlinear operators |  | [See also 90C29] |
|  | [See also 46Txx, 47Hxx, 47Jxx] | 58E20 | Harmonic maps [See also 53C43], etc. |
| 58 C 05 | Real-valued functions | 58E25 | Applications to control theory [See also 49-XX, |
| 58C06 | Set valued and function-space valued mappings |  | 93-XX] |
|  | [See also 47H04, 54C60] | 58E30 | Variational principles |
| 58C07 | Continuity properties of mappings | 58E35 | Variational inequalities (global problems) |
| 58 C 10 | Holomorphic maps [See also 32-XX] | 58 E 40 | Group actions |
| 58C15 | Implicit function theorems; global Newton | 58E50 | Applications |
|  | methods | 58E99 | None of the above, but in this section |
| 58C20 | Differentiation theory (Gateaux, Fréchet, etc.) [See also 26Exx, 46G05] | 58Hxx | Pseudogroups, differentiable groupoids and general structures on manifolds |
| 58 C 25 | Differentiable maps | 58H05 | Pseudogroups and differentiable groupoids |
| 58C30 | Fixed point theorems on manifolds |  | [See also 22A22, 22E65] |
|  | [See also 47H10] | 58H10 | Cohomology of classifying spaces for |
| 58C35 | Integration on manifolds; measures on manifolds [See also 28Cxx] |  | pseudogroup structures (Spencer, Gel'fand-Fuks, etc.) [See also 57R32] |
| 58C40 | Spectral theory; eigenvalue problems [See also 47J10, 58E07] | 58H15 | Deformations of structures [See also 32Gxx, 58J10] |
| 58 C 50 | Analysis on supermanifolds or graded manifolds | 58H99 | None of the above, but in this section |
| 58C99 | None of the above, but in this section | 58Jxx | Partial differential equations on manifolds; |
| 58Dxx | Spaces and manifolds of mappings (including nonlinear versions of 46Exx) [See also 46Txx, |  | differential operators [See also 32 Wxx , $35-\mathrm{XX}$, 53Cxx] |
|  | 53Cxx] | 58J05 | Elliptic equations on manifolds, general theory |
| 58D05 | Groups of diffeomorphisms and homeomorphisms |  | [See also 35-XX] |
|  | as manifolds [See also 22E65, 57S05] | 58J10 | Differential complexes [See also 35Nxx]; elliptic |
| 58D07 | Groups and semigroups of nonlinear operators |  | complexes |
|  | [See also 17B65, 47H20] | 58J15 | Relations with hyperfunctions |
| 58D10 | Spaces of imbeddings and immersions | 58J20 | Index theory and related fixed point theorems |
| 58D15 | Manifolds of mappings [See also 46T10, 54C35] |  | [See also 19K56, 46L80] |
| 58D17 | Manifolds of metrics (esp. Riemannian) | 58J22 | Exotic index theories [See also 19K56, 46L05, |
| 58D19 | Group actions and symmetry properties |  | 46L10, 46L80, 46M20] |
| 58D20 | Measures (Gaussian, cylindrical, etc.) on | 58J26 | Elliptic genera |
|  | manifolds of maps [See also 28Cxx, 46T12] | 58J28 | Eta-invariants, Chern-Simons invariants |
| 58D25 | Equations in function spaces; evolution equations | 58J30 | Spectral flows |
|  | [See also 34Gxx, 35K90, 35L90, 35R15, 37Lxx, | 58J32 | Boundary value problems on manifolds |
|  | 47Jxx] | 58J35 | Heat and other parabolic equation methods |


| 58J37 | Perturbations; asymptotics |
| :---: | :---: |
| 58J40 | Pseudodifferential and Fourier integral operators on manifolds [See also 35Sxx] |
| 58J42 | Noncommutative global analysis, noncommutative residues |
| 58J45 | Hyperbolic equations [See also 35Lxx] |
| 58J47 | Propagation of singularities; initial value problems |
| 58J50 | Spectral problems; spectral geometry; scattering theory [See also 35Pxx] |
| 58J52 | Determinants and determinant bundles, analytic torsion |
| 58J53 | Isospectrality |
| 58J55 | Bifurcation [See also 35B32] |
| 58J60 | Relations with special manifold structures (Riemannian, Finsler, etc.) |
| 58J65 | Diffusion processes and stochastic analysis on manifolds [See also 35R60, 60H10, 60J60] |
| 58J70 | Invariance and symmetry properties [See also 35A30] |
| 58J72 | Correspondences and other transformation methods (e.g. Lie-Bäcklund) [See also 35A22] |
| 58 J 90 | Applications |
| 58J99 | None of the above, but in this section |
| 58Kxx | Theory of singularities and catastrophe theory [See also 32Sxx, 37-XX] |
| 58K05 | Critical points of functions and mappings |
| 58K10 | Monodromy |
| 58K15 | Topological properties of mappings |
| 58K20 | Algebraic and analytic properties of mappings |
| 58K25 | Stability |
| 58K30 | Global theory |
| 58K35 | Catastrophe theory |
| 58K40 | Classification; finite determinacy of map germs |
| 58K45 | Singularities of vector fields, topological aspects |
| 58K50 | Normal forms |
| 58K55 | Asymptotic behavior |
| 58K60 | Deformation of singularities |
| 58K65 | Topological invariants |
| 58K70 | Symmetries, equivariance |
| 58K99 | None of the above, but in this section |
| 58Z05 | Applications to physics |
| 60-XX | PROBABILITY THEORY AND STOCHASTIC PROCESSES \{For additional applications, see $11 \mathrm{Kxx}, 62-\mathrm{XX}, 90-\mathrm{XX}$, 91-XX, 92-XX, 93-XX, 94-XX $\}$ |
| 60-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 60-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 60-02 | Research exposition (monographs, survey articles) |
| 60-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 60-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 60-06 | Proceedings, conferences, collections, etc. |

60-08

60Axx
60A05
60A10

60A99
60Bxx

60B05
60B10
60B11

60B12
60B15
60B99
60 C 05
60D05
60Exx
60E05
60 E 07
60E10
60E15
60E99
60Fxx
60F05
60F10
60F15
60F17
60F20
60F25
60F99
60Gxx
60G05
60G07
60G09
60G10
60G12
60G15
60 G 17
60G18
60G20
60G25
60G30
60G35
60G40
60G42
60G44
60G46
60G48
60G50

Computational methods (not classified at a more specific level) [See also 65C50]
Foundations of probability theory
Axioms; other general questions
Probabilistic measure theory $\{$ For ergodic theory, see 28Dxx and 60Fxx $\}$
None of the above, but in this section
Probability theory on algebraic and topological structures
Probability measures on topological spaces
Convergence of probability measures
Probability theory on linear topological spaces [See also 28C20]
Limit theorems for vector-valued random variables (infinite-dimensional case)
Probability measures on groups, Fourier transforms, factorization
None of the above, but in this section
Combinatorial probability
Geometric probability, stochastic geometry,
random sets [See also 52A22, 53C65]
Distribution theory [See also 62Exx, 62Hxx]
Distributions: general theory
Infinitely divisible distributions; stable distributions
Characteristic functions; other transforms
Inequalities; stochastic orderings
None of the above, but in this section
Limit theorems [See also 28Dxx, 60B12]
Central limit and other weak theorems
Large deviations
Strong theorems
Functional limit theorems; invariance principles
Zero-one laws
$L^{p}$-limit theorems
None of the above, but in this section
Stochastic processes
Foundations of stochastic processes
General theory of processes
Exchangeability
Stationary processes
General second-order processes
Gaussian processes
Sample path properties
Self-similar processes
Generalized stochastic processes
Prediction theory [See also 62M20]
Continuity and singularity of induced measures
Applications (signal detection, filtering, etc.)
[See also 62M20, 93E10, 93E11, 94Axx]
Stopping times; optimal stopping problems;
gambling theory [See also 62L15, 91A60]
Martingales with discrete parameter
Martingales with continuous parameter
Martingales and classical analysis
Generalizations of martingales
Sums of independent random variables; random walks

| 60G51 | Processes with independent increments |
| :--- | :--- |
| 60G52 | Stable processes |
| 60G55 | Point processes |
| 60G57 | Random measures |
| 60G60 | Random fields |
| 60G70 | Extreme value theory; extremal processes |
| 60G99 | None of the above, but in this section |
| 60Hxx | Stochastic analysis [See also 58J65] |
| 60H05 | Stochastic integrals |
| 60H07 | Stochastic calculus of variations and the <br> Malliavin calculus |
| 60H10 | Stochastic ordinary differential equations |
| [See also 34F05] |  |

60K20

60 K 25
60K30
60K35

60K37
60K40
60K99
62-XX

62-02
62-03
62-04

62-06
62-07
62-09
62 A 01
62Bxx
62B05
62B10
62B15
62B99
62Cxx
62C05
62 C 07
62 C 10
62 C 12
62 C 15
62C20
62 C 25
62C99
62D05
62Exx
62E10
62E15
62E17
62E20
62E99
62Fxx
62F03
62 F 05
62 F 07
62 F10
62 F 12
62F15

62-00 General reference works (handbooks, dictionaries, bibliographies, etc.)
62-01 Instructional exposition (textbooks, tutorial papers, etc.)
Applications of Markov renewal processes (reliability, queueing networks, etc.)
[See also 90Bxx]
Queueing theory [See also 68M20, 90B22]
Applications (congestion, allocation, storage, traffic, etc.) [See also 90Bxx]
Interacting random processes; statistical mechanics type models; percolation theory [See also 82B43, 82C43]
Processes in random environments
Other physical applications of random processes
None of the above, but in this section

## STATISTICS

Research exposition (monographs, survey articles)
Historical (must also be assigned at least one classification number from Section 01)
Explicit machine computation and programs (not
the theory of computation or programming)
Proceedings, conferences, collections, etc.
Data analysis
Graphical methods

## Foundational and philosophical topics

 Sufficiency and informationSufficient statistics and fields
Information-theoretic topics [See also 94A17]
Theory of statistical experiments
None of the above, but in this section
Decision theory [See also 90B50, 91B06; for game theory, see 91A35]
General considerations
Complete class results
Bayesian problems; characterization of Bayes procedures
Empirical decision procedures; empirical Bayes procedures
Admissibility
Minimax procedures
Compound decision problems
None of the above, but in this section
Sampling theory, sample surveys
Distribution theory [See also 60Exx]
Characterization and structure theory
Exact distribution theory
Approximations to distributions (nonasymptotic)
Asymptotic distribution theory
None of the above, but in this section
Parametric inference
Hypothesis testing
Asymptotic properties of tests
Ranking and selection
Point estimation
Asymptotic properties of estimators
Bayesian inference

| 62F25 | Tolerance and confidence regions |
| :---: | :---: |
| 62F30 | Inference under constraints |
| 62F35 | Robustness and adaptive procedures |
| 62F40 | Bootstrap, jackknife and other resampling methods |
| 62F99 | None of the above, but in this section |
| 62Gxx | Nonparametric inference |
| 62G05 | Estimation |
| 62G07 | Density estimation |
| 62G08 | Nonparametric regression |
| 62G09 | Resampling methods |
| 62G10 | Hypothesis testing |
| 62G15 | Tolerance and confidence regions |
| 62G20 | Asymptotic properties |
| 62G30 | Order statistics; empirical distribution functions |
| 62G32 | Statistics of extreme values; tail inference |
| 62G35 | Robustness |
| 62G99 | None of the above, but in this section |
| 62Hxx | Multivariate analysis [See also 60Exx] |
| 62H05 | Characterization and structure theory |
| 62 H 10 | Distribution of statistics |
| 62 H 11 | Directional data; spatial statistics |
| 62 H 12 | Estimation |
| 62 H 15 | Hypothesis testing |
| 62 H 17 | Contingency tables |
| 62 H 20 | Measures of association (correlation, canonical correlation, etc.) |
| 62H25 | Factor analysis and principal components; correspondence analysis |
| 62H30 | Classification and discrimination; cluster analysis [See also 68T10] |
| 62H35 | Image analysis |
| 62H99 | None of the above, but in this section |
| 62Jxx | Linear inference, regression |
| 62J02 | General nonlinear regression |
| 62 J 05 | Linear regression |
| 62J07 | Ridge regression; shrinkage estimators |
| 62 J 10 | Analysis of variance and covariance |
| 62 J 12 | Generalized linear models |
| 62J15 | Paired and multiple comparisons |
| 62 J 20 | Diagnostics |
| 62J99 | None of the above, but in this section |
| 62Kxx | Design of experiments [See also 05Bxx] |
| 62 K 05 | Optimal designs |
| 62 K 10 | Block designs |
| 62K15 | Factorial designs |
| 62K20 | Response surface designs |
| 62K25 | Robust parameter designs |
| 62K99 | None of the above, but in this section |
| 62Lxx | Sequential methods |
| 62L05 | Sequential design |
| 62L10 | Sequential analysis |
| 62L12 | Sequential estimation |
| 62L15 | Optimal stopping [See also 60G40, 91A60] |
| 62L20 | Stochastic approximation |
| 62L99 | None of the above, but in this section |


| 62Mxx | Inference from stochastic processes |
| :---: | :---: |
| 62 M 02 | Markov processes: hypothesis testing |
| 62 M 05 | Markov processes: estimation |
| 62 M 07 | Non-Markovian processes: hypothesis testing |
| 62M09 | Non-Markovian processes: estimation |
| 62 M 10 | Time series, auto-correlation, regression, etc. [See also 91B84] |
| 62M15 | Spectral analysis |
| 62M20 | Prediction [See also 60G25]; filtering [See also 60G35, 93E10, 93E11] |
| 62M30 | Spatial processes |
| 62M40 | Random fields; image analysis |
| 62M45 | Neural nets and related approaches |
| 62M99 | None of the above, but in this section |
| 62 Nxx | Survival analysis and censored data |
| 62N01 | Censored data models |
| 62N02 | Estimation |
| 62N03 | Testing |
| 62N05 | Reliability and life testing [See also 90B25] |
| 62N99 | None of the above, but in this section |
| 62 Pxx | Applications [See also 90-XX, 91-XX, 92-XX] |
| 62 P 05 | Applications to actuarial sciences and financial mathematics |
| 62 P 10 | Applications to biology and medical sciences |
| 62 P 12 | Applications to environmental and related topics |
| 62 P 15 | Applications to psychology |
| 62 P 20 | Applications to economics [See also 91Bxx] |
| 62 P 25 | Applications to social sciences |
| 62 P 30 | Applications in engineering and industry |
| 62 P 35 | Applications to physics |
| 62 P 99 | None of the above, but in this section |
| 62 Q 05 | Statistical tables |
| 65-XX | NUMERICAL ANALYSIS |
| 65-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 65-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 65-02 | Research exposition (monographs, survey articles) |
| 65-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 65-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 65-05 | Experimental papers |
| 65-06 | Proceedings, conferences, collections, etc. |
| $65 A 05$ | Tables |
| $65 B x x$ | Acceleration of convergence |
| 65B05 | Extrapolation to the limit, deferred corrections |
| 65B10 | Summation of series |
| 65B15 | Euler-Maclaurin formula |
| 65B99 | None of the above, but in this section |
| 65 Cxx | Probabilistic methods, simulation and stochastic differential equations \{For theoretical aspects, see 68 U 20 and 60 H 35$\}$ |
| 65 C 05 | Monte Carlo methods |
| 65 C 10 | Random number generation |
| 65 C 20 | Models, numerical methods [See also 68U20] |
| 65C30 | Stochastic differential and integral equations |


| 65C35 | Stochastic particle methods [See also 82C80] | 65Jxx | Numerical analysis in abstract spaces |
| :---: | :---: | :---: | :---: |
| 65 C 40 | Computational Markov chains | 65J05 | General theory |
| 65C50 | Other computational problems in probability | 65J10 | Equations with linear operators (do not use |
| 65 C 60 | Computational problems in statistics |  | 65 Fxx ) |
| 65C99 | None of the above, but in this section | 65J15 | Equations with nonlinear operators (do not use |
| 65Dxx | Numerical approximation and computational geometry (primarily algorithms) \{For theory, see 41-XX and 68Uxx $\}$ | $\begin{aligned} & 65 \mathrm{~J} 20 \\ & 65 \mathrm{~J} 22 \end{aligned}$ | 65Hxx) <br> Improperly posed problems; regularization Inverse problems |
| 65D05 | Interpolation | 65 J 99 | None of the above, but in this section |
| 65D07 | Splines | 65Kxx | Mathematical programming, optimization and |
| 65D10 | Smoothing, curve fitting |  | variational techniques |
| 65D15 | Algorithms for functional approximation | 65 K 05 | Mathematical programming algorithms \{For theory see 90 Cxx$\}$ |
| 65D17 | Computer aided design (modeling of curves and surfaces) [See also 68U07] | 65K10 | Optimization and variational techniques [See also 49Mxx, 93B40] |
| 65D18 | Computer graphics and computational geometry [See also 51N05, 68U05] | 65K99 65Lxx | None of the above, but in this section |
| 65D20 | Computation of special functions, construction of tables [See also 33F05] | 65L05 <br> 65 L 06 | Initial value problems <br> Multistep, Runge-Kutta and extrapolation |
| 65D25 | Numerical differentiation |  | methods |
| 65D30 | Numerical integration | 65L07 | Numerical investigation of stability of solutions |
| 65D32 | Quadrature and cubature formulas | 65L08 | Improperly posed problems |
| 65D99 | None of the above, but in this section | 65L09 | Inverse problems |
| 65E05 | Numerical methods in complex analysis | 65L10 | Boundary value problems |
|  | (potential theory, etc.) \{For numerical methods | 65L12 | Finite difference methods |
|  | in conformal mapping, see 30C30\} | 65L15 | Eigenvalue problems |
| 65Fxx | Numerical linear algebra | 65L20 | Stability and convergence of numerical methods |
| 65F05 | Direct methods for linear systems and matrix | 65L50 | Mesh generation and refinement |
|  | inversion | 65L60 | Finite elements, Rayleigh-Ritz, Galerkin and |
| 65F10 | Iterative methods for linear systems |  | collocation methods |
|  | [See also 65N22] | 65L70 | Error bounds |
| 65F15 | Eigenvalues, eigenvectors | 65L80 | Methods for differential-algebraic equations |
| 65 F 18 | Inverse eigenvalue problems | 65L99 | None of the above, but in this section |
| 65F20 | Overdetermined systems, pseudoinverses | 65Mxx | Partial differential equations, initial value |
| 65F22 | Ill-posedness, regularization |  | and time-dependent initial-boundary value |
| 65F25 | Orthogonalization |  | problems |
| 65F30 | Other matrix algorithms | 65M06 | Finite difference methods |
| 65F35 | Matrix norms, conditioning, scaling | 65M12 <br> 65M15 | Stability and convergence of numerical methods Error bounds |
|  | [See also 15A12, 15A60] | 65M15 | Error bounds |
| 65F40 | Determinants | 65M20 | Method of lines |
| 65F50 | Sparse matrices | 65M25 | Method of characteristics |
| 65F99 | None of the above, but in this section | 65M30 | Improperly posed problems |
| 65Gxx | Error analysis and interval analysis | 65M32 | Inverse problems |
| 65G20 | Algorithms with automatic result verification | 65M50 | Mesh generation and refinement |
| 65G30 | Interval and finite arithmetic | 65M55 | Multigrid methods; domain decomposition |
| 65G40 | General methods in interval analysis | 65M60 | Finite elements, Rayleigh-Ritz and Galerkin methods, finite methods |
| 65G50 | Roundoff error | 65M70 | Spectral, collocation and related methods |
| 65G99 | None of the above, but in this section | 65M99 | None of the above, but in this section |
| 65Hxx | Nonlinear algebraic or transcendental equations | 65Nxx | Partial differential equations, boundary value problems |
| 65H05 | Single equations | 65N06 | Finite difference methods |
| 65H10 | Systems of equations | 65N12 | Stability and convergence of numerical methods |
| 65H17 | Eigenvalues, eigenvectors [See also 47Hxx, | 65N15 | Error bounds |
|  | 47Jxx, 58C40, 58E07, 90C30] | 65N21 | Inverse problems |
| 65H20 | Global methods, including homotopy approaches [See also 58C30, 90C30] | 65 N 22 | Solution of discretized equations [See also 65Fxx, $65 \mathrm{Hxx}]$ |
| 65H99 | None of the above, but in this section | 65N25 | Eigenvalue problems |


| 65N30 | Finite elements, Rayleigh-Ritz and Galerkin methods, finite methods |
| :---: | :---: |
| 65N35 | Spectral, collocation and related methods |
| 65N38 | Boundary element methods |
| 65N40 | Method of lines |
| 65N45 | Method of contraction of the boundary |
| 65N50 | Mesh generation and refinement |
| 65 N 55 | Multigrid methods; domain decomposition |
| 65N99 | None of the above, but in this section |
| 65Pxx | Numerical problems in dynamical systems [See also 37Mxx] |
| 65P10 | Hamiltonian systems including symplectic integrators |
| 65P20 | Numerical chaos |
| 65P30 | Bifurcation problems |
| 65P40 | Nonlinear stabilities |
| $65 \mathrm{P9} 9$ | None of the above, but in this section |
| 65 Q 05 | Difference and functional equations, recurrence relations |
| 65Rxx | Integral equations, integral transforms |
| 65R10 | Integral transforms |
| 65R20 | Integral equations |
| 65R30 | Improperly posed problems |
| 65R32 | Inverse problems |
| 65 R 99 | None of the above, but in this section |
| $65 \mathrm{S05}$ | Graphical methods |
| 65 Txx | Numerical methods in Fourier analysis |
| 65 T 40 | Trigonometric approximation and interpolation |
| 65 T 50 | Discrete and fast Fourier transforms |
| 65 T 60 | Wavelets |
| 65 T 99 | None of the above, but in this section |
| 65Yxx | Computer aspects of numerical algorithms |
| 65 Y 05 | Parallel computation |
| 65 Y 10 | Algorithms for specific classes of architectures |
| 65 Y 15 | Packaged methods |
| $65 Y 20$ | Complexity and performance of numerical algorithms [See also 68Q25] |
| 65 Y 99 | None of the above, but in this section |
| 65Z05 | Applications to physics |
| 68-XX | COMPUTER SCIENCE \{For papers involving machine computations and programs in a specific mathematical area, see Section -04 in that area |
| 68-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 68-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 68-02 | Research exposition (monographs, survey articles) |
| 68-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 68-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 68-06 | Proceedings, conferences, collections, etc. |
| 68Mxx | Computer system organization |
| 68M01 | General |
| 68M07 | Mathematical problems of computer architecture |

68M10

68M12
68M14
68M15

68M20

68M99
68 Nxx
68N01
68N15
68N17
68N18 Functional programming and lambda calculus [See also 03B40]
68N19

68N20
68N25
68N30

68N99
68Pxx
68P01
68P05
68 P 10
68 P 15
68P20
68 P 25
68P30

68P99
68Qxx
68Q01
68Q05 Models of computation (Turing machines, etc.) [See also 03D10, 81P68]
68Q10 Modes of computation (nondeterministic, parallel, interactive, probabilistic, etc.) [See also 68Q85]
68Q15 Complexity classes (hierarchies, relations among complexity classes, etc.) [See also 03D15, 68Q17, 68Q19]
68Q17 Computational difficulty of problems (lower bounds, completeness, difficulty of approximation, etc.) [See also 68Q15]
68Q19 Descriptive complexity and finite models [See also 03C13]
68Q25 Analysis of algorithms and problem complexity [See also 68W40]
68Q30 Algorithmic information theory (Kolmogorov complexity, etc.)
68Q32 Computational learning theory [See also 68T05]
68Q42 Grammars and rewriting systems
68Q45 Formal languages and automata [See also 03D05, 68Q70, 94A45]
68Q55
Network design and communication [See also 68R10, 90B18]
Network protocols
Distributed systems
Reliability, testing and fault tolerance [See also 94C12]
Performance evaluation; queueing; scheduling [See also 60K25, 90Bxx]
None of the above, but in this section
Software
General
Programming languages

Other programming techniques (object-oriented,
sequential, concurrent, automatic, etc.)
Compilers and interpreters
Operating systems
Mathematical aspects of software engineering
(specification, verification, metrics, requirements,
etc.)
None of the above, but in this section
Theory of data
General
Data structures
Searching and sorting
Database theory
Information storage and retrieval
Data encryption [See also 94A60, 81P68]
Coding and information theory (compaction, compression, models of communication, encoding schemes, etc.) [See also 94Axx]
None of the above, but in this section

## Theory of computing

General

Semantics [See also 03B70, 06B35, 18C50]

| 68Q60 | Specification and verification (program logics, model checking, etc.) [See also 03B70] |
| :---: | :---: |
| 68Q65 | Abstract data types; algebraic specification [See also 18C50] |
| 68Q70 | Algebraic theory of languages and automata [See also 18B20, 20M35] |
| 68Q80 | Cellular automata [See also 37B15] |
| 68Q85 | Models and methods for concurrent and distributed computing (process algebras, bisimulation, transition nets, etc.) |
| 68Q99 | None of the above, but in this section |
| 68Rxx | Discrete mathematics in relation to computer science |
| 68R01 | General |
| 68R05 | Combinatorics |
| 68R10 | Graph theory [See also 05Cxx, 90B10, 90B35, 90C35] |
| 68R15 | Combinatorics on words |
| 68R99 | None of the above, but in this section |
| 68Txx | Artificial intelligence |
| 68 T 01 | General |
| 68 T 05 | Learning and adaptive systems [See also 68Q32, 91E40] |
| 68 T 10 | Pattern recognition, speech recognition $\{$ For cluster analysis, see 62 H 30$\}$ |
| 68 T 15 | Theorem proving (deduction, resolution, etc.) [See also 03B35] |
| 68 T 20 | Problem solving (heuristics, search strategies, etc.) |
| 68 T 27 | Logic in artificial intelligence |
| 68 T 30 | Knowledge representation |
| 68 T 35 | Languages and software systems (knowledgebased systems, expert systems, etc.) |
| 68 T 37 | Reasoning under uncertainty |
| 68 T 40 | Robotics [See also 93C85] |
| 68 T 45 | Machine vision and scene understanding |
| 68 T 50 | Natural language processing [See also 03B65] |
| 68 T 99 | None of the above, but in this section |
| 68Uxx | Computing methodologies and applications |
| 68U01 | General |
| 68U05 | Computer graphics; computational geometry [See also 65D18] |
| 68U07 | Computer-aided design [See also 65D17] |
| 68U10 | Image processing |
| 68U15 | Text processing; mathematical typography |
| 68 U 20 | Simulation [See also 65Cxx] |
| 68U35 | Information systems (hypertext navigation, interfaces, decision support, etc.) |
| 68U99 | None of the above, but in this section |
| 68Wxx | Algorithms \{For numerical algorithms, see 65 XX; for combinatorics and graph theory, see 68Rxx $\}$ |
| 68W01 | General |
| 68W05 | Nonnumerical algorithms |
| 68W10 | Parallel algorithms |
| 68W15 | Distributed algorithms |
| 68W20 | Randomized algorithms |
| 68W25 | Approximation algorithms |

68W30 Symbolic computation and algebraic computation [See also 11Yxx, 12Y05, 13Pxx, 14Qxx, 16Z05, 17-08, 33F10]
68W35
68W40
68W99

## 70-XX

$70-00$
$70-01$

70-02
70-03

70-04

70-05
70-06
70-08
70A05
70 Bxx
70B05
70B10
70B15
70B99
70 C 20
70Exx

70E05
70E15
70E17
70E18
70E20
70E40
70E45
70E50
70E55
70E60

70E99

70F05
70F07
70F10
70F15
70F16
70F17
70F20
70F25
70F35
70F40

70Fxx Dynamics of a system of particles, including celestial mechanics
VLSI algorithms
Analysis of algorithms [See also 68Q25]
None of the above, but in this section
MECHANICS OF PARTICLES AND SYSTEMS \{For relativistic mechanics, see 83 A 05 and 83 C 10 ; for statistical mechanics, see $82-X X\}$
General reference works (handbooks, dictionaries, bibliographies, etc.)
Instructional exposition (textbooks, tutorial papers, etc.)
Research exposition (monographs, survey articles)
Historical (must also be assigned at least one classification number from Section 01)
Explicit machine computation and programs (not the theory of computation or programming)
Experimental work
Proceedings, conferences, collections, etc.
Computational methods
Axiomatics, foundations
Kinematics [See also 53A17]
Kinematics of a particle
Kinematics of a rigid body
Mechanisms, robots [See also 68T40, 70Q05, 93C85]
None of the above, but in this section
Statics
Dynamics of a rigid body and of multibody systems
Motion of the gyroscope
Free motion of a rigid body [See also 70M20]
Motion of a rigid body with a fixed point
Motion of a rigid body in contact with a solid surface [See also 70F25]
Perturbation methods for rigid body dynamics
Integrable cases of motion
Higher-dimensional generalizations
Stability problems
Dynamics of multibody systems
Robot dynamics and control [See also 68T40, 70Q05, 93C85]
None of the above, but in this section

Two-body problems
Three-body problems
$n$-body problems
Celestial mechanics
Collisions in celestial mechanics, regularization
Inverse problems
Holonomic systems
Nonholonomic systems
Collision of rigid or pseudo-rigid bodies
Problems with friction

| 70F45 | Infinite particle systems |
| :---: | :---: |
| 70F99 | None of the above, but in this section |
| 70Gxx | General models, approaches, and methods [See also 37-XX] |
| 70G10 | Generalized coordinates; event, impulse-energy, configuration, state, or phase space |
| 70G40 | Topological and differential-topological methods |
| 70G45 | Differential-geometric methods (tensors, connections, symplectic, Poisson, contact, Riemannian, nonholonomic, etc.) [See also 53Cxx, 53Dxx, 58Axx] |
| 70G55 | Algebraic geometry methods |
| 70G60 | Dynamical systems methods |
| 70G65 | Symmetries, Lie-group and Lie-algebra methods |
| 70G70 | Functional-analytic methods |
| 70G75 | Variational methods |
| 70G99 | None of the above, but in this section |
| 70Hxx | Hamiltonian and Lagrangian mechanics [See also 37Jxx] |
| 70 H 03 | Lagrange's equations |
| 70 H 05 | Hamilton's equations |
| 70H06 | Completely integrable systems and methods of integration |
| 70 H 07 | Nonintegrable systems |
| 70H08 | Nearly integrable Hamiltonian systems, KAM theory |
| 70H09 | Perturbation theories |
| 70 H 11 | Adiabatic invariants |
| 70 H 12 | Periodic and almost periodic solutions |
| 70H14 | Stability problems |
| 70H15 | Canonical and symplectic transformations |
| 70H20 | Hamilton-Jacobi equations |
| 70H25 | Hamilton's principle |
| 70H30 | Other variational principles |
| 70H33 | Symmetries and conservation laws, reverse symmetries, invariant manifolds and their bifurcations, reduction |
| 70H40 | Relativistic dynamics |
| 70H45 | Constrained dynamics, Dirac's theory of constraints [See also 70F20, 70F25, 70Gxx] |
| 70H50 | Higher-order theories |
| 70H99 | None of the above, but in this section |
| 70Jxx | Linear vibration theory |
| 70J10 | Modal analysis |
| 70 J 25 | Stability |
| 70 J 30 | Free motions |
| 70 J 35 | Forced motions |
| 70 J 40 | Parametric resonances |
| 70 J 50 | Systems arising from the discretization of structural vibration problems |
| 70 J 99 | None of the above, but in this section |
| 70Kxx | Nonlinear dynamics [See also 34Cxx, 37-XX] |
| 70K05 | Phase plane analysis, limit cycles |
| 70K20 | Stability |
| 70K25 | Free motions |
| 70K28 | Parametric resonances |
| 70K30 | Nonlinear resonances |
| 70K40 | Forced motions |


| 70K42 | Equilibria and periodic trajectories |
| :---: | :---: |
| 70K43 | Quasi-periodic motions and invariant tori |
| 70K44 | Homoclinic and heteroclinic trajectories |
| 70K45 | Normal forms |
| 70K50 | Bifurcations and instability |
| 70K55 | Transition to stochasticity (chaotic behavior) [See also 37D45] |
| 70K60 | General perturbation schemes |
| 70K65 | Averaging of perturbations |
| 70K70 | Systems with slow and fast motions |
| 70K75 | Nonlinear modes |
| 70K99 | None of the above, but in this section |
| $70 \mathrm{L05}$ | Random vibrations [See also 74H50] |
| 70M20 | Orbital mechanics |
| 70P05 | Variable mass, rockets |
| 70Q05 | Control of mechanical systems [See also 58F13, 58F27, 60Gxx, 60 Jxx ] |
| 70Sxx | Classical field theories [See also 37Kxx, 37Lxx, 78-XX, 81Txx, 83-XX] |
| 70S05 | Lagrangian formalism and Hamiltonian formalism |
| 70S10 | Symmetries and conservation laws |
| 70S15 | Yang-Mills and other gauge theories |
| 70S20 | More general nonquantum field theories |
| 70S99 | None of the above, but in this section |
| 74-XX | MECHANICS OF DEFORMABLE SOLIDS |
| 74-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 74-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 74-02 | Research exposition (monographs, survey articles) |
| 74-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 74-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 74-05 | Experimental work |
| 74-06 | Proceedings, conferences, collections, etc. |
| 74Axx | Generalities, axiomatics, foundations of continuum mechanics of solids |
| 74A05 | Kinematics of deformation |
| 74A10 | Stress |
| 74A15 | Thermodynamics |
| 74A20 | Theory of constitutive functions |
| 74A25 | Molecular, statistical, and kinetic theories |
| 74A30 | Nonsimple materials |
| 74A35 | Polar materials |
| 74A40 | Random materials and composite materials |
| 74A45 | Theories of fracture and damage |
| 74A50 | Structured surfaces and interfaces, coexistent phases |
| 74A55 | Theories of friction (tribology) |
| 74A60 | Micromechanical theories |
| 74A65 | Reactive materials |
| 74A99 | None of the above, but in this section |
| 74Bxx | Elastic materials |
| 74B05 | Classical linear elasticity |
| 74B10 | Linear elasticity with initial stresses |


| 74B15 | Equations linearized about a deformed state <br> (small deformations superposed on large) |
| :--- | :--- |
| 74B20 | Nonlinear elasticity |
| 74B99 | None of the above, but in this section |
| 74Cxx | Plastic materials, materials of stress-rate and <br> internal-variable type |
|  | Small-strain, rate-independent theories (including <br> 74C05 |
|  | rigid-plastic and elasto-plastic materials) |
| 74C10 | Small-strain, rate-dependent theories (including |
| theories of viscoplasticity) |  |


| 74Hxx | Dynamical problems |
| :---: | :---: |
| 74H05 | Explicit solutions |
| 74H10 | Analytic approximation of solutions (perturbation methods, asymptotic methods, series, etc.) |
| 74H15 | Numerical approximation of solutions |
| 74H20 | Existence of solutions |
| 74H25 | Uniqueness of solutions |
| 74H30 | Regularity of solutions |
| 74H35 | Singularities, blowup, stress concentrations |
| 74H40 | Long-time behavior of solutions |
| 74H45 | Vibrations |
| 74H50 | Random vibrations |
| 74H55 | Stability |
| 74H60 | Dynamical bifurcation |
| 74H65 | Chaotic behavior |
| 74H99 | None of the above, but in this section |
| 74Jxx | Waves |
| 74J05 | Linear waves |
| 74J10 | Bulk waves |
| 74J15 | Surface waves |
| 74J20 | Wave scattering |
| 74J25 | Inverse problems |
| 74J30 | Nonlinear waves |
| 74J35 | Solitary waves |
| 74 J 40 | Shocks and related discontinuities |
| 74J99 | None of the above, but in this section |
| 74Kxx | Thin bodies, structures |
| 74K05 | Strings |
| 74K10 | Rods (beams, columns, shafts, arches, rings, etc.) |
| 74K15 | Membranes |
| 74K20 | Plates |
| 74K25 | Shells |
| 74K30 | Junctions |
| 74K35 | Thin films |
| 74K99 | None of the above, but in this section |
| 74Lxx | Special subfields of solid mechanics |
| 74L05 | Geophysical solid mechanics [See also 86-XX] |
| 74L10 | Soil and rock mechanics |
| 74L15 | Biomechanical solid mechanics [See also 92C10] |
| 74L99 | None of the above, but in this section |
| 74Mxx | Special kinds of problems |
| 74M05 | Control, switches and devices ("smart materials") [See also 93Cxx] |
| 74M10 | Friction |
| 74M15 | Contact |
| 74M20 | Impact |
| 74M25 | Micromechanics |
| 74M99 | None of the above, but in this section |
| 74Nxx | Phase transformations in solids [See also 74A50, 80Axx, 82B26, 82C26] |
| 74N05 | Crystals |
| 74N10 | Displacive transformations |
| 74N15 | Analysis of microstructure |
| 74N20 | Dynamics of phase boundaries |
| 74N25 | Transformations involving diffusion |
| 74N30 | Problems involving hysteresis |
| 74N99 | None of the above, but in this section |


| 74Pxx | Optimization [See also 49Qxx] | 76B10 | Jets and cavities, cavitation, free-streamline |
| :---: | :---: | :---: | :---: |
| 74P05 | Compliance or weight optimization |  | theory, water-entry problems, airfoil and hydrofoil |
| 74 P 10 | Optimization of other properties |  | theory, sloshing |
| 74 P 15 | Topological methods | 76B15 | Water waves, gravity waves; dispersion and scattering, nonlinear interaction [See also 35Q30, 35Q53] |
| 74P20 | Geometrical methods |  |  |
| 74P99 | None of the above, but in this section |  |  |
| 74Qxx | Homogenization, determination of effective properties | 76 B 20 76 B 25 | Ship waves <br> Solitary waves [See also 35Q51] |
| 74Q05 | Homogenization in equilibrium problems | 76B45 | Capillarity (surface tension) [See also 76D45] |
| 74Q10 | Homogenization and oscillations in dynamical problems | 76 B 47 76 B 55 | Vortex flows Internal waves |
| 74Q15 | Effective constitutive equations | 76B60 | Atmospheric waves [See also 86A10] |
| 74Q20 | Bounds on effective properties | $76 \mathrm{B65}$ | Rossby waves [See also 86A05, 86A10] |
| 74Q99 | None of the above, but in this section | $76 B 70$ $76 B 75$ | Stratification effects in inviscid fluids <br> Flow control and optimization [See also 49Q10, |
| 74Rxx | Fracture and damage |  | 93C20, 93C95] |
| 74R05 | Brittle damage | 76B99 | None of the above, but in this section |
| 74R10 | Brittle fracture | 76Dxx | Incompressible viscous fluids |
| 74R15 | High-velocity fracture | 76D03 | Existence, uniqueness, and regularity theory |
| 74R20 | Anelastic fracture and damage |  | [See also 35Q30, 35Q35] |
| 74R99 | None of the above, but in this section | 76D05 | Navier-Stokes equations [See also 35Q30] |
| 74Sxx | Numerical methods [See also 65-XX, 74G15, 74H15] | 76D06 | Statistical solutions of Navier-Stokes and related equations [See also 60H30, 76M35] |
| 74S05 | Finite element methods | 76D07 | Stokes and related (Oseen, etc.) flows |
| 74S10 | Finite volume methods | 76D08 | Lubrication theory |
| 74S15 | Boundary element methods | 76D09 | Viscous-inviscid interaction |
| 74S20 | Finite difference methods | 76D10 | Boundary-layer theory, separation and reattachment, higher-order effects |
| 74S25 | Spectral and related methods |  |  |
| 74S30 | Other numerical methods | 76D17 | Viscous vortex flows |
| 74S99 | None of the above, but in this section | 76D25 | Wakes and jets |
| 74S | None of the above, but in this section | 76D27 | Other free-boundary flows; Hele-Shaw flows |
| 76-XX | FLUID MECHANICS \{For general continuum | 76D33 | Waves |
|  | mechanics, see 74Axx, or other parts of | 76D45 | Capillarity (surface tension) [See also 76B45] |
|  | 74-XX $\}$ | 76D50 | Stratification effects in viscous fluids |
| 76-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) | 76D55 | Flow control and optimization [See also 49Q10, 93C20, 93C95] |
| 76-01 | Instructional exposition (textbooks, tutorial papers, etc.) | $\begin{aligned} & \text { 76D99 } \\ & \text { 76Exx } \end{aligned}$ | None of the above, but in this section Hydrodynamic stability |
| 76-02 | Research exposition (monographs, survey articles) | 76E05 | Parallel shear flows |
| 76-03 | Historical (must also be assigned at least one | 76E06 | Convection |
|  | classification number from Section 01) | 76 E 07 | Rotation |
| 76-04 | Explicit machine computation and programs (not the theory of computation or programming) | $\begin{aligned} & 76 \mathrm{E} 09 \\ & 76 \mathrm{E} 15 \end{aligned}$ | Stability and instability of nonparallel flows Absolute and convective instability and stability |
| 76-05 | Experimental work | 76 E 17 | Interfacial stability and instability |
| 76-06 | Proceedings, conferences, collections, etc. | 76 E 19 | Compressibility effects |
| 76Axx | Foundations, constitutive equations, rheology | 76E20 | Stability and instability of geophysical and |
| 76A02 | Foundations of fluid mechanics | 76E25 | Stability and instability of magnetohydrodynamic and electrohydrodynamic flows |
| 76A05 | Non-Newtonian fluids |  |  |
| 76A10 | Viscoelastic fluids | 76E30 |  |
| 76A15 | Liquid crystals [See also 82D30] | 76 E 99 | None of the above, but in this section |
| 76A20 | Thin fluid films | 76Fxx | Turbulence [See also 37-XX, 60Gxx, 60Jxx] |
| 76A25 | Superfluids (classical aspects) | 76F02 | Fundamentals |
| 76A99 | None of the above, but in this section | 76F05 | Isotropic turbulence; homogeneous turbulence |
| 76Bxx | Incompressible inviscid fluids | 76F06 | Transition to turbulence |
| 76B03 | Existence, uniqueness, and regularity theory | 76F10 | Shear flows |
|  | [See also 35Q35] | 76F20 | Dynamical systems approach to turbulence |
| 76B07 | Free-surface potential flows |  | [See also 37-XX] |


| 76F25 | Turbulent transport, mixing |
| :---: | :---: |
| 76F30 | Renormalization and other field-theoretical methods [See also 81T99] |
| 76F35 | Convective turbulence [See also 76E15, 76Rxx] |
| 76F40 | Turbulent boundary layers |
| 76F45 | Stratification effects |
| 76F50 | Compressibility effects |
| 76 F 55 | Statistical turbulence modeling [See also 76M35] |
| 76F60 | $k$ - $\varepsilon$ modeling |
| 76F65 | Direct numerical and large eddy simulation of turbulence |
| 76F70 | Control of turbulent flows |
| 76F99 | None of the above, but in this section |
| 76G25 | General aerodynamics and subsonic flows |
| 76H05 | Transonic flows |
| 76J20 | Supersonic flows |
| 76K05 | Hypersonic flows |
| 76L05 | Shock waves and blast waves [See also 35L67] |
| 76Mxx | Basic methods in fluid mechanics [See also 65$\mathrm{XX}]$ |
| 76M10 | Finite element methods |
| 76M12 | Finite volume methods |
| 76M15 | Boundary element methods |
| 76M20 | Finite difference methods |
| 76M22 | Spectral methods |
| 76M23 | Vortex methods |
| 76M25 | Other numerical methods |
| 76M27 | Visualization algorithms |
| 76M28 | Particle methods and lattice-gas methods |
| 76M30 | Variational methods |
| 76M35 | Stochastic analysis |
| 76M40 | Complex-variables methods |
| 76M45 | Asymptotic methods, singular perturbations |
| 76M50 | Homogenization |
| 76M55 | Dimensional analysis and similarity |
| 76M60 | Symmetry analysis, Lie group and algebra methods |
| 76M99 | None of the above, but in this section |
| 76Nxx | Compressible fluids and gas dynamics, general |
| 76N10 | Existence, uniqueness, and regularity theory [See also 35L60, 35L65, 35Q30] |
| 76N15 | Gas dynamics, general |
| 76N17 | Viscous-inviscid interaction |
| 76N20 | Boundary-layer theory |
| 76N25 | Flow control and optimization |
| 76N99 | None of the above, but in this section |
| 76P05 | Rarefied gas flows, Boltzmann equation [See also 82B40, 82C40, 82D05] |
| 76Q05 | Hydro- and aero-acoustics |
| 76Rxx | Diffusion and convection |
| 76R05 | Forced convection |
| 76R10 | Free convection |
| 76R50 | Diffusion [See also 60J60] |
| 76R99 | None of the above, but in this section |
| 76S05 | Flows in porous media; filtration; seepage |

76M10 Finite element methods
76M15 Boundary element methods
76M20 Finite difference methods
76M22 Spectral methods
Vortex methods
76M25 Other numerical methods
76M27 Visualization algorithms
76M28 Particle methods and lattice-gas methods
76M30 Variational methods
76M35 Stochastic analysis
76M40 Complex-variables methods
76M45 Asymptotic methods, singular perturbations
76M50 Homogenization
76M55 Dimensional analysis and similarity
76M60 Symmetry analysis, Lie group and algebra
methods
76M99 None of the above, but in this section
76Nxx Compressible fluids and gas dynamics, general
76N10 Existence, uniqueness, and regularity theory
[See also 35L60, 35L65, 35Q30]
Gas dynamics, general
76N17 Viscous-inviscid interaction
76N20 Boundary-layer theory
76N25 Flow control and optimization
76N99 None of the above, but in this section
76P05 Rarefied gas flows, Boltzmann equation
[See also 82B40, 82C40, 82D05]
76Q05 Hydro- and aero-acoustics
76Rxx Diffusion and convection
76R05 Forced convection
76R10 Free convection
76R50 Diffusion [See also 60J60]
$\begin{array}{ll}\text { 76R05 } & \text { None of the above, but in this section } \\ \text { Flows in porous media; filtration; seepage }\end{array}$

76Txx
76 T 10
76 T 15
76 T 20
76 T 25
76 T 30
76 T 99
76U05
76V05
76W05

76X05
76Y05
76Zxx
$76 Z 05$
76Z10
76Z99
78-XX
78-00
78-01

78-02
78-03
78-04

78-05
78-06
78Аxx
78A02
78A05
78A10
78A15
78A20
78A25
78A30
78A35
78A40
78A45

78A46
78A48
78A50
78A55

78A70
78 A 97

78A99

78A60 Lasers, masers, optical bistability, nonlinear optics [See also 81V80]
Two-phase and multiphase flows
Liquid-gas two-phase flows, bubbly flows
Dusty-gas two-phase flows
Suspensions
Granular flows [See also 74C99, 74E20]
Three or more component flows
None of the above, but in this section
Rotating fluids
Reaction effects in flows [See also 80A32]
Magnetohydrodynamics and electrohydrodynamics
Ionized gas flow in electromagnetic fields; plasmic flow [See also 82D10]
Quantum hydrodynamics and relativistic hydrodynamics [See also 83C55, 85A30]
Biological fluid mechanics [See also 74F10, 74L15, 92Cxx]
Physiological flows [See also 92C35]
Biopropulsion in water and in air None of the above, but in this section

## OPTICS, ELECTROMAGNETIC THEORY

\{For quantum optics, see 81V80\}
General reference works (handbooks, dictionaries, bibliographies, etc.)
Instructional exposition (textbooks, tutorial papers, etc.)
Research exposition (monographs, survey articles)
Historical (must also be assigned at least one classification number from Section 01)
Explicit machine computation and programs (not the theory of computation or programming)
Experimental work
Proceedings, conferences, collections, etc.
General
Foundations
Geometric optics
Physical optics
Electron optics
Space charge waves
Electromagnetic theory, general
Electro- and magnetostatics
Motion of charged particles
Waves and radiation
Diffraction, scattering [See also 34E20 for WKB methods]
Inverse scattering problems
Composite media; random media
Antennas, wave-guides
Technical applications

Biological applications [See also 91D30, 92C30]
Mathematically heuristic optics and
electromagnetic theory (must also be assigned
at least one other classification number in this section)
Miscellaneous topics

| 78Mxx | Basic methods |
| :---: | :---: |
| 78M05 | Method of moments |
| 78M10 | Finite element methods |
| 78M15 | Boundary element methods |
| 78M20 | Finite difference methods |
| 78M25 | Other numerical methods |
| 78M30 | Variational methods |
| 78M35 | Asymptotic analysis |
| 78M40 | Homogenization |
| 78M50 | Optimization |
| 78M99 | None of the above, but in this section |
| 80-XX | CLASSICAL THERMODYNAMICS, HEAT TRANSFER \{For thermodynamics of solids, see 74A15\} |
| 80-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 80-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 80-02 | Research exposition (monographs, survey articles) |
| 80-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 80-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 80-05 | Experimental work |
| 80-06 | Proceedings, conferences, collections, etc. |
| 80Axx | Thermodynamics and heat transfer |
| 80A05 | Foundations |
| 80A10 | Classical thermodynamics, including relativistic |
| 80A17 | Thermodynamics of continua [See also 74A15] |
| 80A20 | Heat and mass transfer, heat flow |
| 80A22 | Stefan problems, phase changes, etc. [See also 74Nxx] |
| 80A23 | Inverse problems |
| 80A25 | Combustion |
| 80A30 | Chemical kinetics [See also 76V05, 92C45, 92E20] |
| 80A32 | Chemically reacting flows [See also 92C45, 92E20] |
| 80A50 | Chemistry (general) [See mainly 92Exx] |
| 80A99 | None of the above, but in this section |
| 80Mxx | Basic methods |
| 80M10 | Finite element methods |
| 80M15 | Boundary element methods |
| 80M20 | Finite difference methods |
| 80M25 | Other numerical methods |
| 80M30 | Variational methods |
| 80M35 | Asymptotic analysis |
| 80M40 | Homogenization |
| 80M50 | Optimization |
| 80M99 | None of the above, but in this section |
| 81-XX | QUANTUM THEORY |
| 81-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 81-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 81-02 | Research exposition (monographs, survey articles) |


| 81R99 | of the above, but in this se |
| :---: | :---: |
| 81Sxx | General quantum mechanics and problems of quantization |
| 81S05 | Commutation relations and statistics |
| 81S10 | Geometry and quantization, symplectic methods [See also 53D50] |
| 81S20 | Stochastic quantization |
| 81S25 | Quantum stochastic calculus |
| 81S30 | Phase space methods including Wigner distributions, etc. |
| 81S40 | Path integrals [See also 58D30] |
| 81S99 | None of the above, but in this section |
| 81Txx | Quantum field theory; related classical field theories [See also 70Sxx] |
| 81 T 05 | Axiomatic quantum field theory; operator algebras |
| 81 T 08 | Constructive quantum field theory |
| 81 T 10 | Model quantum field theories |
| 81 T 13 | Yang-Mills and other gauge theories [See also 53C07, 58E15] |
| 81 T 15 | Perturbative methods of renormalization |
| 81 T 16 | Nonperturbative methods of renormalization |
| 81 T 17 | Renormalization group methods |
| 81 T 18 | Feynman diagrams |
| 81 T 20 | Quantum field theory on curved space backgrounds |
| 81 T 25 | Quantum field theory on lattices |
| 81 T27 | Continuum limits |
| 81 T 30 | String and superstring theories; other extended objects (e.g., branes) [See also 83E30] |
| 81 T 40 | Two-dimensional field theories, conformal field theories, etc. |
| 81 T 45 | Topological field theories [See also 57R56, 58Dxx] |
| 81 T50 | Anomalies |
| 81 T60 | Supersymmetric field theories |
| 81 T 70 | Quantization in field theory; cohomological methods [See also 58D29] |
| 81 T 75 | Noncommutative geometry methods [See also 46L85, 46L87, 58B34] |
| 81 T80 | Simulation and numerical modeling |
| 81 T 99 | None of the above, but in this section |
| 81Uxx | Scattering theory [See also 34A55, 34L25, 34L40, 35P25, 47A40] |
| 81U05 | 2-body potential scattering theory [See also 34E20 for WKB methods] |
| 81 U 10 | $n$-body potential scattering theory |
| 81U15 | Exactly and quasi-solvable systems |
| 81U20 | $S$-matrix theory, etc. |
| 81U30 | Dispersion theory, dispersion relations |
| 81 U 40 | Inverse scattering problems |
| 81U99 | None of the above, but in this section |
| 81Vxx | Applications to specific physical systems |
| 81V05 | Strong interaction, including quantum chromodynamics |
| 81 V 10 | Electromagnetic interaction; quantum electrodynamics |
| 81 V 15 | Weak interaction |

81 V 17

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82Bxx
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82B05

82B10
82B20 Lattice systems (Ising, dimer, Potts, etc.) and systems on graphs
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82B28
82B30
82B31
82B35 Irreversible thermodynamics, including OnsagerMachlup theory [See also 92E20]
82B40 Kinetic theory of gases
82B41 Random walks, random surfaces, lattice animals, etc. [See also 60G50, 82C41]
82B43 Percolation [See also 60K35]
82B44 Disordered systems (random Ising models, random Schrödinger operators, etc.)
82B80 Numerical methods (Monte Carlo, series resummation, etc.) [See also 65-XX, 81T80]
82B99 None of the above, but in this section
82Cxx Time-dependent statistical mechanics (dynamic and nonequilibrium)
82C03 Foundations
82C05 Classical dynamic and nonequilibrium statistical mechanics (general)

| 82C10 | Quantum dynamics and nonequilibrium statistical <br> mechanics (general) |
| :---: | :--- |
| 82C20 | Dynamic lattice systems (kinetic Ising, etc.) and <br> systems on graphs |
| 82C21 | Dynamic continuum models (systems of particles, <br> etc.) |
| 82C22 | Interacting particle systems [See also 60K35] |
| 82C23 | Exactly solvable dynamic models |
|  | [See also 37K60] |

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83C35
83C40 Gravitational energy and conservation laws; groups of motions
83C45
83C47

83C50
83C55 Macroscopic interaction of the gravitational field with matter (hydrodynamics, etc.)
83C57 Black holes
83C60 Spinor and twistor methods; Newman-Penrose formalism
83C65 Methods of noncommutative geometry [See also 58B34]
83C75 Space-time singularities, cosmic censorship, etc.
83C80 Analogues in lower dimensions
83C99 None of the above, but in this section
83D05 Relativistic gravitational theories other than Einstein's, including asymmetric field theories
83Exx Unified, higher-dimensional and super field theories
83E05 Geometrodynamics
83E15 Kaluza-Klein and other higher-dimensional theories
83E30 String and superstring theories [See also 81T30]
83E50 Supergravity
83E99 None of the above, but in this section
83F05 Cosmology
85-XX ASTRONOMY AND ASTROPHYSICS $\{$ For celestial mechanics, see 70F15\}
85-00 General reference works (handbooks, dictionaries, bibliographies, etc.)
85-01 Instructional exposition (textbooks, tutorial papers, etc.)
85-02 Research exposition (monographs, survey articles)

| 85-03 | Historical (must also be assigned at least one classification number from Section 01) |
| :---: | :---: |
| 85-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 85-05 | Experimental work |
| 85-06 | Proceedings, conferences, collections, etc. |
| 85-08 | Computational methods |
| 85A04 | General |
| 85A05 | Galactic and stellar dynamics |
| 85A15 | Galactic and stellar structure |
| 85A20 | Planetary atmospheres |
| 85A25 | Radiative transfer |
| 85A30 | Hydrodynamic and hydromagnetic problems [See also 76Y05] |
| 85A35 | Statistical astronomy |
| 85A40 | Cosmology \{For relativistic cosmology, see 83F05\} |
| 85A99 | Miscellaneous topics |
| 86-XX | GEOPHYSICS [See also 76U05, 76V05] |
| 86-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 86-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 86-02 | Research exposition (monographs, survey articles) |
| 86-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 86-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 86-05 | Experimental work |
| 86-06 | Proceedings, conferences, collections, etc. |
| 86-08 | Computational methods |
| 86A04 | General |
| 86A05 | Hydrology, hydrography, oceanography <br> [See also 76Bxx, 76E20, 76Q05, 76Rxx, 76U05] |
| 86A10 | Meteorology and atmospheric physics [See also 76Bxx, 76E20, 76N15, 76Q05, 76Rxx, 76U05] |
| 86A15 | Seismology |
| 86A17 | Global dynamics, earthquake problems |
| 86A20 | Potentials, prospecting |
| 86A22 | Inverse problems [See also 35R30] |
| 86A25 | Geo-electricity and geomagnetism [See also 76W05, 78A25] |
| 86A30 | Geodesy, mapping problems |
| 86A32 | Geostatistics |
| 86A40 | Glaciology |
| 86A60 | Geological problems |
| 86A99 | Miscellaneous topics |
| 90-XX | OPERATIONS RESEARCH, MATHEMATICAL PROGRAMMING |
| 90-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 90-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 90-02 | Research exposition (monographs, survey articles) |
| 90-03 | Historical (must also be assigned at least one classification number from Section 01) |

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90C29
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90C31
90C32
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90C39
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90 C 46
90C47
90C48

90Cxx Mathematical programming [See also 49Mxx, 65Kxx]
Explicit machine computation and programs (not the theory of computation or programming)
Proceedings, conferences, collections, etc.
Computational methods

## Operations research and management science

Inventory, storage, reservoirs
Transportation, logistics
Network models, deterministic
Network models, stochastic
Communication networks [See also 68M10, 94A05]
Traffic problems
Queues and service [See also 60K25, 68M20]
Reliability, availability, maintenance, inspection
[See also 60K10, 62N05]
Production models
Scheduling theory, deterministic
[See also 68M20]
Scheduling theory, stochastic [See also 68M20]
Search theory
Management decision making, including multiple
objectives [See also 90C31, 91A35, 91B06]
Marketing, advertising [See also 91B60]
Theory of organizations, manpower planning [See also 91D35]
Discrete location and assignment
[See also 90C10]
Continuous location
Case-oriented studies
None of the above, but in this section

Linear programming
Large-scale problems
Special problems of linear programming
(transportation, multi-index, etc.)
Boolean programming
Integer programming
Mixed integer programming
Stochastic programming
Quadratic programming
Semidefinite programming
Convex programming
Nonconvex programming
Combinatorial optimization
Multi-objective and goal programming
Nonlinear programming
Sensitivity, stability, parametric optimization
Fractional programming
Complementarity problems
Semi-infinite programming
Programming involving graphs or networks
[See also 90C27]
Dynamic programming [See also 49L20]
Markov and semi-Markov decision processes
Optimality conditions, duality [See also 49N15]
Minimax problems [See also 49K35]
Programming in abstract spaces

| 90 C 49 | Extreme-point and pivoting methods |
| :---: | :---: |
| 90 C 51 | Interior-point methods |
| 90 C 52 | Methods of reduced gradient type |
| 90 C 53 | Methods of quasi-Newton type |
| 90C55 | Methods of successive quadratic programming type |
| 90 C 56 | Derivative-free methods |
| 90 C 57 | Polyhedral combinatorics, branch-and-bound, branch-and-cut |
| 90 C 59 | Approximation methods and heuristics |
| 90C60 | Abstract computational complexity for mathematical programming problems [See also 68Q25] |
| 90 C 70 | Fuzzy programming |
| 90C90 | Applications of mathematical programming |
| 90C99 | None of the above, but in this section |
| 91-XX | GAME THEORY, ECONOMICS, SOCIAL AND BEHAVIORAL SCIENCES |
| 91-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 91-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 91-02 | Research exposition (monographs, survey articles) |
| 91-03 | Historical (must also be assigned at least one classification number from section 01) |
| 91-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 91-06 | Proceedings, conferences, collections, etc. |
| 91-08 | Computational methods |
| 91Axx | Game theory |
| 91 A 05 | 2-person games |
| 91A06 | $n$-person games, $n>2$ |
| 91 A 10 | Noncooperative games |
| 91 A 12 | Cooperative games |
| 91 A 13 | Games with infinitely many players |
| 91 A 15 | Stochastic games |
| 91A18 | Games in extensive form |
| 91A20 | Multistage and repeated games |
| 91 A 22 | Evolutionary games |
| 91A23 | Differential games [See also 49N70] |
| 91 A 24 | Positional games (pursuit and evasion, etc.) [See also 49N75] |
| 91 A 25 | Dynamic games |
| 91A26 | Rationality, learning |
| 91 A 28 | Signaling, communication |
| 91 A30 | Utility theory for games [See also 91B16] |
| 91A35 | Decision theory for games [See also 62Cxx, 91B06, 90B50] |
| 91A40 | Game-theoretic models |
| 91A43 | Games involving graphs |
| 91A44 | Games involving topology or set theory |
| 91 A46 | Combinatorial games |
| 91 A50 | Discrete-time games |
| 91A55 | Games of timing |
| 91A60 | Probabilistic games; gambling |
| 91 A65 | Hierarchical games |
| 91 A 70 | Spaces of games |

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91B74
91B76

91B82
91B84
91B99
91Cxx

91C05
91C15 One- and multidimensional scaling
91C20 Clustering [See also 62D05]
91C99 None of the above, but in this section
91Dxx Mathematical sociology (including anthropology)
91D10
91D20
91D25
91D30
91D35
91D99
Applications of game theory
Experimental studies
None of the above, but in this section
Mathematical economics \{For econometrics, see 62 P 20$\}$
Fundamental topics (basic mathematics, methodology; applicable to economics in general)
Decision theory [See also 62Cxx, 90B50, 91A35]
Individual preferences
Group preferences
Voting theory
Social choice
Utility theory
Public goods
Price theory and market structure
Market models (auctions, bargaining, bidding, selling, etc.)
Finance, portfolios, investment
Risk theory, insurance
Resource and cost allocation
Production theory, theory of the firm
Labor market, contracts
Consumer behavior, demand theory
Informational economics
Equilibrium: general theory
Special types of equilibria
Special types of economies
General economic models, trade models
Dynamic economic models, growth models
Macro-economic models (monetary models,
models of taxation)
Multisectoral models
Matching models
Stochastic models
Spatial models
Models of real-world systems
Environmental economics (natural resource
models, harvesting, pollution, etc.)
Statistical methods; economic indices and measures
Economic time series analysis [See also 62M10]
None of the above, but in this section
Social and behavioral sciences: general topics \{For statistics, see 62-XX\}
Measurement theory

Models of societies, social and urban evolution
Mathematical geography and demography
Spatial models [See also 91B72]
Social networks
Manpower systems [See also 91B40, 90B70]
None of the above, but in this section

| 91Exx | Mathematical psychology |
| :---: | :---: |
| 91E10 | Cognitive psychology |
| 91E30 | Psychophysics and psychophysiology; perception |
| 91E40 | Memory and learning [See also 68T05] |
| 91 E 45 | Measurement and performance |
| 91E99 | None of the above, but in this section |
| 91Fxx | Other social and behavioral sciences (mathematical treatment) |
| 91 F 10 | History, political science |
| 91F20 | Linguistics [See also 03B65, 68T50] |
| 91F99 | None of the above, but in this section |
| 92-XX | BIOLOGY AND OTHER NATURAL SCIENCES |
| 92-00 | General reference works (handbooks, dictionaries, bibliographies, etc.) |
| 92-01 | Instructional exposition (textbooks, tutorial papers, etc.) |
| 92-02 | Research exposition (monographs, survey articles) |
| 92-03 | Historical (must also be assigned at least one classification number from Section 01) |
| 92-04 | Explicit machine computation and programs (not the theory of computation or programming) |
| 92-06 | Proceedings, conferences, collections, etc. |
| 92-08 | Computational methods |
| 92Bxx | Mathematical biology in general |
| 92B05 | General biology and biomathematics |
| 92B10 | Taxonomy, statistics |
| 92B15 | General biostatistics [See also 62P10] |
| 92B20 | Neural networks, artificial life and related topics [See also 68T05, 82C32, 94Cxx] |
| 92B99 | None of the above, but in this section |
| 92Cxx | Physiological, cellular and medical topics |
| 92C05 | Biophysics |
| 92 C 10 | Biomechanics [See also 74L15] |
| 92 C 15 | Developmental biology, pattern formation |
| 92 C 17 | Cell movement (chemotaxis, etc.) |
| 92 C 20 | Neural biology |
| 92C30 | Physiology (general) |
| 92C35 | Physiological flow [See also 76Z05] |
| 92 C 37 | Cell biology |
| 92 C 40 | Biochemistry, molecular biology |
| 92C45 | Kinetics in biochemical problems (pharmacokinetics, enzyme kinetics, etc.) [See also 80A30] |
| 92C50 | Medical applications (general) |
| 92C55 | Biomedical imaging and signal processing [See also 44A12, 65R10] |
| 92C60 | Medical epidemiology |
| 92C80 | Plant biology |
| 92C99 | None of the above, but in this section |
| 92Dxx | Genetics and population dynamics |
| 92D10 | Genetics \{For genetic algebras, see 17D92\} |
| 92D15 | Problems related to evolution |
| 92D20 | Protein sequences, DNA sequences |
| 92D25 | Population dynamics (general) |
| 92D30 | Epidemiology |
| 92D40 | Ecology |

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92Exx
92E10

92E20

92E99
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93B60

Animal behavior
None of the above, but in this section
Chemistry \{For biochemistry, see $\mathbf{9 2 C 4 0}\}$
Molecular structure (graph-theoretic methods, methods of differential topology, etc.)
Classical flows, reactions, etc. [See also 80A30, 80A32]
None of the above, but in this section
Other natural sciences
SYSTEMS THEORY; CONTROL \{For optimal control, see 49-XX
General reference works (handbooks, dictionaries, bibliographies, etc.)
Instructional exposition (textbooks, tutorial papers, etc.)
Research exposition (monographs, survey articles)
Historical (must also be assigned at least one classification number from Section 01)
Explicit machine computation and programs (not the theory of computation or programming)
Proceedings, conferences, collections, etc.

## General

Axiomatic system theory
General systems
Hierarchical systems
Decentralized systems
Large scale systems
Mathematical modeling (models of systems, model-matching, etc.)
None of the above, but in this section
Controllability, observability, and system structure
Attainable sets
Controllability
Observability
Canonical structure
System structure simplification
Variable structure systems
Realizations from input-output data
Transformations
Linearizations
Minimal systems representations
Algebraic methods
Geometric methods (including algebro-geometric)
Operator-theoretic methods [See also 47A48,
47A57, 47B35, 47N70]
Differential-geometric methods
System identification
Sensitivity (robustness)
$H^{\infty}$-control
Computational methods
Synthesis problems
Design techniques (robust design, computer-aided
design, etc.)
Feedback control
Pole and zero placement problems
Eigenvalue problems

| 93B99 | None of the above, but in this section | $94-01$ | Instructional exposition (textbooks, tutorial |
| :--- | :--- | :--- | :--- |
| 93Cxx | Control systems, guided systems |  | papers, etc.) |
| 93C05 | Linear systems | $94-02$ | Research exposition (monographs, survey articles) |
| 93C10 | Nonlinear systems | $94-03$ | Historical (must also be assigned at least one <br> classification number from Section 01) |
| 93C15 | Systems governed by ordinary differential |  | $94-04$ | | Explicit machine computation and programs (not |
| :--- |
|  |
| 93C20 |
|  |
|  |
| equations [See also 34H05] |
| Systems governed by partial differential equations |
| [See also 35B37] |


| 94 C 10 | Switching theory, application of Boolean algebra; Boolean functions [See also 06E30] | 97C90 | Teaching and curriculum (innovations, teaching practices, studies of curriculum materials, |
| :---: | :---: | :---: | :---: |
| 94 C 12 | Fault detection; testing |  | effective teaching, etc. ) |
| 94 C 15 | Applications of graph theory [See also 05Cxx, 68R10] | $\begin{aligned} & \text { 97C99 } \\ & \text { 97Dxx } \end{aligned}$ | None of the above, but in this section Education and instruction in mathematics |
| 94C30 | Applications of design theory [See also 05Bxx] | 97D10 | Comparative studies on mathematics education |
| 94 C 99 | None of the above, but in this section |  | [See also 97C40] |
| 94D05 | Fuzzy sets and logic (in connection with questions of Section 94) [See also 03B52, 03E72, 28E10] | 97D20 97D30 | Philosophical and theoretical contributions to mathematical education [See also 97C50] Goals of mathematics teaching. Curriculum development |
| $\begin{gathered} \text { 97-XX } \\ 97-00 \end{gathered}$ | MATHEMATICS EDUCATION <br> General reference works (handbooks, dictionaries, bibliographies, etc.) | 97D40 | Teaching methods and classroom techniques. Lesson preparation. Educational principles \{For research aspects see 97 Cxx$\}$ |
| $97-01$ $97-02$ | Instructional exposition (textbooks, tutorial papers, etc.) | 97D50 | Teaching problem solving and heuristic strategies \{For research aspects see 97 Cxx \} |
| 97-02 | Research exposition (monographs, survey articles) | 97D60 | Achievement control and rating |
| 97-03 | Historical (must also be assigned at least one classification number from Section 01) | 97D70 | Diagnosis, analysis and remediation of learning difficulties and student errors |
| 97-04 | Explicit machine computation and programs (not the theory of computation or programming) | $\begin{aligned} & \text { 97D80 } \\ & \text { 97D99 } \end{aligned}$ | Teaching units, draft lessons and master lessons None of the above, but in this section |
| 97-06 | Proceedings, conferences, collections, etc. | 97Uxx | Educational material and media. Educational |
| 97Axx | General |  | technology |
| 97A20 | Recreational mathematics [See also 00A08] | 97U20 | Analysis of textbooks, development and |
| 97A40 | Sociological issues [See also 97C60] |  | evaluation of textbooks. Textbook use in the |
| 97A80 | Standards [See also 97B70] |  | classroom |
| 97A90 | Fiction and games | 97U30 | Teacher manuals and planning aids |
| 97Bxx | Educational policy and educational systems | 97U40 | Problem books; student competitions, |
| 97B10 | Educational research and planning |  | examination questions |
| 97 B 20 | General education | 97U50 | Computer assisted instruction and programmed |
| 97B30 | Vocational education |  | instruction |
| 97B40 | Higher education | 97U60 | Manipulative materials and their use in the |
| 97B50 | Teacher education \{For research aspects see 97C70\} | 97U70 | classroom \{For research aspects see 97 C 80$\}$ Technological tools (computers, calculators, |
| 97B60 | Out-of-school education. Adult and further education | 97U80 | software, etc.) and their use in the classroom Audiovisual media and their use in instruction |
| 97B70 | Syllabuses. Curriculum guides, official documents [See also 97A80] | 97U99 | None of the above, but in this section |
| 97B99 | None of the above, but in this section |  |  |
| 97Cxx | Psychology of and research in mathematics education |  |  |
| 97C20 | Affective aspects (motivation, anxiety, persistence, etc.) |  |  |
| 97C30 | Student learning and thinking (misconceptions, cognitive development, problem solving, etc.) |  |  |
| 97C40 | Assessment (large scale assessment, validity, reliability, etc.) [See also 97D10] |  |  |
| 97C50 | Theoretical perspectives (learning theories, epistemology, philosophies of teaching and learning, etc.) [See also 97D20] |  |  |
| 97C60 | Sociological aspects of learning (culture, group interactions, equity issues, etc.) |  |  |
| 97 C 70 | Teachers, and research on teacher education (teacher development, etc.) [See also 97B50] |  |  |
| 97C80 | Technological tools and other materials in teaching and learning (research on innovations, role in student learning, use of tools by teachers, etc.) |  |  |

