

Banach J. Math. Anal. 5 (2011), no. 1, 181–192

BANACH JOURNAL OF MATHEMATICAL ANALYSIS ISSN: 1735-8787 (electronic) www.emis.de/journals/BJMA/

ELEMENTARY OPERATORS AND SUBHOMOGENEOUS C^* -ALGEBRAS II

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Communicated by M. Frank

ABSTRACT. Let A be a separable unital C^* -algebra and let Θ_A be the canonical contraction from the Haagerup tensor product of A with itself to the space of completely bounded maps on A. In our previous paper we showed that if A satisfies (a) the lengths of elementary operators on A are uniformly bounded, or (b) the image of Θ_A equals the set of all elementary operators on A, then A is necessarily SFT (subhomogeneous of finite type). In this paper we extend this result; we show that if A satisfies (a) or (b) then the codimensions of 2-primal ideals of A are also finite and uniformly bounded. Using this, we provide an example of a unital separable SFT algebra which does not satisfy (a) nor (b). However, if the primitive spectrum of a unital SFT algebra A is Hausdorff, we show that such an A satisfies (a) and (b).

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Date: Received: 22 June 2010; Accepted: 1 October 2010.

²⁰¹⁰ Mathematics Subject Classification. Primary 46L05; Secondary 46L07, 47B47, 46H10. Key words and phrases. C*-algebra, subhomogeneous, elementary operator, 2-primal ideal, Glimm ideal.