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## NOTE ON EXTREME POINTS IN MARCINKIEWICZ FUNCTION SPACES

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*Dedicated to Professor Lars-Erik Persson on his 65th birthday*

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ABSTRACT. We show that the unit ball of the subspace  $M_W^0$  of ordered continuous elements of  $M_W$  has no extreme points, where  $M_W$  is the Marcinkiewicz function space generated by a decreasing weight function  $w$  over the interval  $(0, \infty)$  and  $W(t) = \int_0^t w$ ,  $t \in (0, \infty)$ . We also present here a proof of the fact that a function  $f$  in the unit ball of  $M_W$  is an extreme point if and only if  $f^* = w$ .

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