

Banach J. Math. Anal. 1 (2007), no. 2, 237–244

BANACH JOURNAL OF MATHEMATICAL ANALYSIS ISSN: 1735-8787 (electronic) http://www.math-analysis.org

## REMARKS ON LIPSCHITZIAN MAPPINGS AND SOME FIXED POINT THEOREMS

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This paper is devoted to Professor Themistocles M. Rassias.

Submitted by L. Székelyhidi

ABSTRACT. Let X, Y be the normed spaces,  $C \subset X$  a convex set, and  $T : C \to Y$  a continuous mapping. Some weak conditions implying the Lipschitz continuity of T are presented. Applications to the fixed point theory and theory of composition operators are presented.

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Date: Received: 6 February 2007; Accepted: 15 October 2007.

<sup>2000</sup> Mathematics Subject Classification. Primary 47H10; Secondary 54H25.

 $Key\ words\ and\ phrases.$  Fixed point, Lipschitz mapping, subadditive function, uniformly convex space.