

Zbl 863.11014

Burr, Stefan A.; Erdős, Paul; Graham, Ronald L.; Li, W.Wen-Ching

Complete sequences of sets of integer powers. (In English)

Acta Arith. 77, No.2, 133-138 (1996). [ISSN 0065-1036]

For a sequence $S = (s_1, s_2, \dots)$ of positive integers, define $\Sigma(S) := \{\sum_{i=1}^{\infty} \varepsilon_i s_i : \varepsilon_i = 0 \text{ or } 1, \sum_{i=1}^{\infty} \varepsilon_i < \infty\}$. Call S complete if $\Sigma(S)$ contains all sufficiently large integers. It has been known for some time that if $\gcd(a, b) = 1$ then the (nondecreasing) sequence formed from the values $a^s b^t$ with $s_0 \leq s, t_0 \leq t \leq f(s_0, t_0)$ is complete, where s_0 and t_0 are arbitrary, and $f(s_0, t_0)$ is sufficiently large.

In this note we consider the analogous question for sequences formed from pure powers of integers.

S.A.Burr (New York)

Classification:

11B83 Special sequences of integers and polynomials

11B13 Additive bases

Keywords:

complete sequences; sets of integer powers; bases; sumsets