Zbl 651.60072

Erdős, Paul; Chen, Robert W.

Random walks on \mathbb{Z}_2^n . (In English)

J. Multivariate Anal. 25, No.1, 111-118 (1988). [0047-259X]

Let \mathbb{Z}_2^n be the set of all (a_1, a_2, \ldots, a_n) such that $a_i = 0$ or $a_i = 1$ for all i = 1 $1, 2, \ldots, n$. Further let $(W_t^n)_{t\geq 0}$ be a random walk on Z_2^n such that $P(W_0^n =$ $A = 2^{-n}$ for all A in \mathbb{Z}_2^n and such that, given a_1, a_2, \ldots, a_n , the next transition is equally probable to $(a_2, a_3, \ldots, a_n, 0)$ or $(a_2, a_3, \ldots, a_n, 1)$.

This paper studies the behaviour of the random time C_n taken by the random walk to visit all states in \mathbb{Z}_2^n . The main result is

$$P(c_2^n 1n(2^n) < C_n < d2^n 1n(2^n)$$
a.e.) = 1, for all constants $c < 1 < d$.

We note that $(W_t^n)_{t\geq 0}$ is not the usual random walk in the sense that two (and not any neighboured) vertices are chosen with the same probability. (Also the walk permits jumps in the "diagonal", see e.g. n=3). The latter has been studied before by P. C. Mathews [Covering problems for random walks on spheres and finite groups. Tech. Rep. 234, Dept. of Statistics, Stanford Univ. (1984)] and the results turn out here to be similar, but the technique used in this paper is different.

F.T.Bruss

Classification:

60J15 Random walk

60F20 Zero-one laws

60G50 Sums of independent random variables

Keywords:

Borel-Cantelli lemma; covering time