Zbl 578.30018

Edrei, A.; Erdős, Paul

Entire functions bounded outside a finite area. (In English)

Acta Math. Hung. 45, 367-376 (1985). [0236-5294]

Problem: Under what circumstances can it happen that for an entire function f(z) the 2-dimensional Lebesgue measure of $\{z : |f(z)| > B\}$ is finite for some positive B? The authors answer this problem completely by proving that this can only happen, if

$$\lim\inf_{r\to\infty}\log\log\log M(r)/\log r\geq 2.$$

An example shows that 2 can not be replaced by a larger number.

W.H.J.Fuchs

Classification:

30D20 General theory of entire functions

30D35 Distribution of values (one complex variable)

Keywords:

Lebesgue measure