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*The fractional parts of the Bernoulli numbers.* (In English)

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It is proved that the fractional parts of the Bernoulli numbers  $B_{2k}$  are dense in the interval  $(0, 1)$ . Furthermore, for every positive integer  $k$ , the set of all  $m$  for which  $B_{2m}$  has the same fractional part as  $B_{2k}$  as positive asymptotic density. The second statement is proved via this result on divisibility by  $p-1$ : For each  $\varepsilon > 0$ , there is a  $T = T(\varepsilon)$  so that if  $x > T$ , then the number of  $m \leq x$  which have a divisor  $p-1 > T$ , with  $p$  prime is less than  $\varepsilon x$ . The paper concludes with several related open questions.

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Classification:

11B39 Special numbers, etc.

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positive asymptotic density; divisibility; Bernoulli number; fractional part; shifted prime