## Zbl 329.05116

Erdős, Paul; Faudree, Ralph J.; Rousseau, C.C.; Schelp, R.H. Generalized Ramsey theory for multiple colors. (In English)

J. Comb. Theory, Ser. B 20, 250-264 (1976). [0095-8956]

From the authors' abstract: In this paper, we study the generalized Ramsey number  $r(G_1, \ldots, G_k)$  where the graphs  $G_1, \ldots, G_k$  consist of complete graphs, complete bipartite graphs, paths, and cycles. Our main theorem gives the Ramsey number for the case where  $G_2, \ldots, G_k$  are fixed and  $G_1 \cong C_n$  or  $P_n$  with n sufficiently large. If among  $G_2, \ldots, G_k$  there are both complete graphs and odd cycles, the main theorem requires an additional hypothesis concerning the size of the odd cycles relative to their number. If among  $G_2, \ldots, G_k$  there are odd cycles but no complete graphs, then no additional hypothesis is necessary and complete results can be expressed in terms of a new type of Ramsey number which is introduced in this paper. For k=3 and k=4 we determine all necessary values of the new Ramsey number and so obtain, in particular, explicit and complete results for the cycle Ramsey numbers  $r(C_n, C_l, C_k)$  and  $r(C_n, C_l, C_k, C_m)$  when n is large.

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Classification:

05C35 Extremal problems (graph theory)