Zbl 217.32202

Erdős, Paul; Turán, P.

One some general problems in the theory of partitions. I (In English)

Acta Arith. 18, 53-62 (1971). [0065-1036]

Let  $0 < \lambda_1 < \lambda_2 < \dots$  be an infinite sequence. Assume

$$\lim_{x \to \infty} \left( \sum_{\lambda_i < x} 1 \right) X^{-\alpha} (\log x)^{\beta} = A.$$

Then for almost all systems  $\lambda_{i_1} + \lambda_{i_2} + \ldots \leq N$ ,  $1 \leq i_1 < i_2 < \ldots$  the number of summands is

$$(1 + o(1))c_1 N^{\alpha/(\alpha+1)} (\log N)^{-\beta/(\alpha+1)}, \quad c_1 = c_1(\alpha, \beta, A).$$

Several related results are proved. [See the first author and *J. Lehner*, Duke Math J. 8, 335-345 (1941; Zbl 025.10703) and the authors, Acta Math. Acad. Sci. Hung. 19, 413-435 (1963; Zbl 235.20004).]

Classification:

11P81 Elementary theory of partitions

11P82 Analytic theory of partitions