Zbl 017.10304

Erdős, Paul

On the sum and difference of squares of primes. II. (In English)

J. London Math. Soc. 12, 168-171 (1937).

The author proves (by Brun's method) that, for an infinity of n, the number of solutions of the equation $n=p^2+q^2$ in primes p and q is greater than $\exp\left(\frac{c\log n}{\log\log n}\right)$. This is an improvement of the author's previous result (see Zbl 016.20103). The author also proves the theorem: Let $r_1 < r_2 < \cdots$ be an infinite sequence of positive integers such that for an infinity of N the number of r's less than or equal to N is greater than $N\exp\left(-\frac{c_4\log N}{\log\log N}\right)$ with $c_4 < \frac{1}{2}\log 2$. Then for an infinity of M the number of the solutions of the equation $r_j^2 - r_i^2 = M$ is greater than $\exp\left(\frac{c_2\log M}{\log\log M}\right)$, where c_5 depends only upon c_4 .

Wright (Aberdeen)

Classification:

11N05 Distribution of primes