

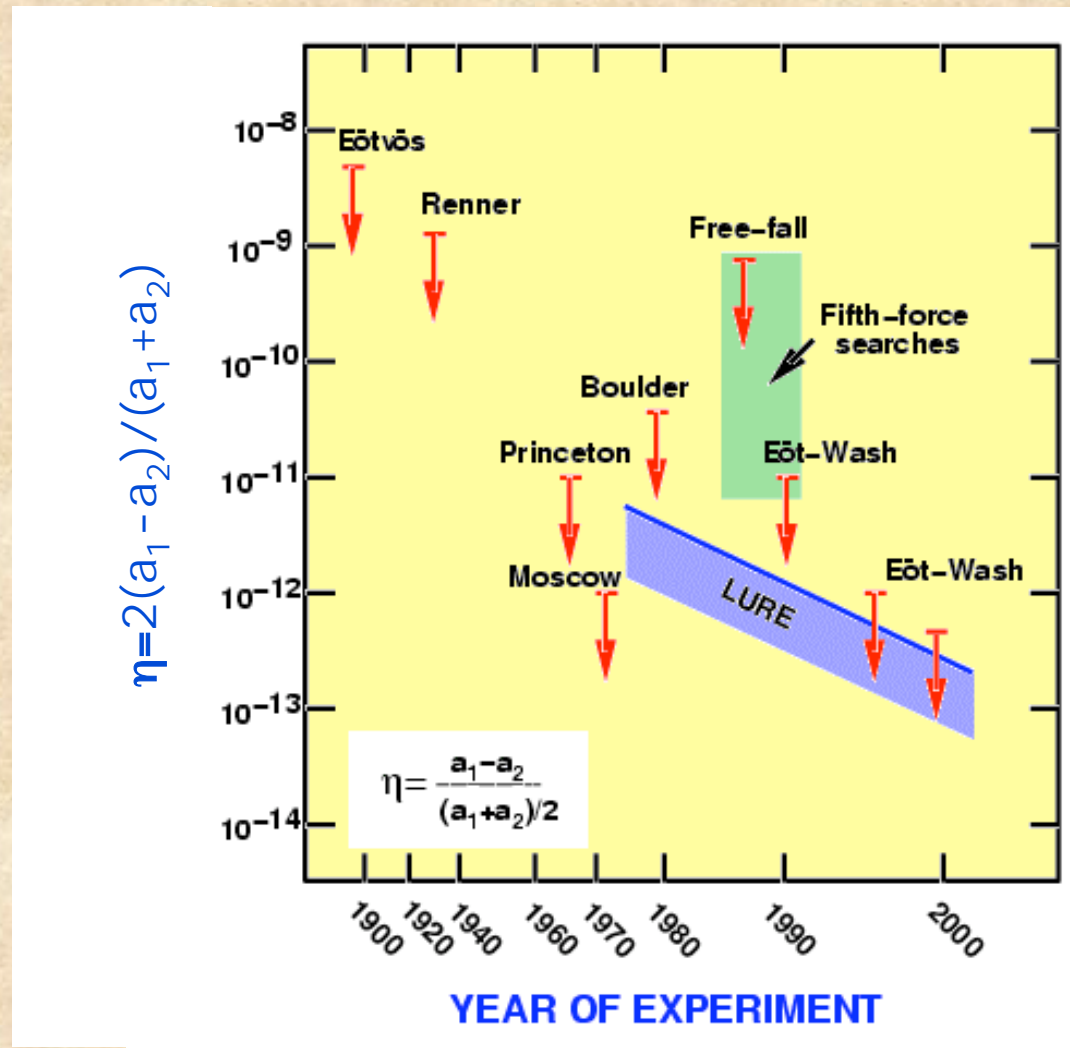
NEW TESTS OF  
STRONG-FIELD GRAVITY  
WITH NEUTRON STARS AND  
BLACK HOLES

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University of Arizona

with Simon DeDeo and Tim Johannsen

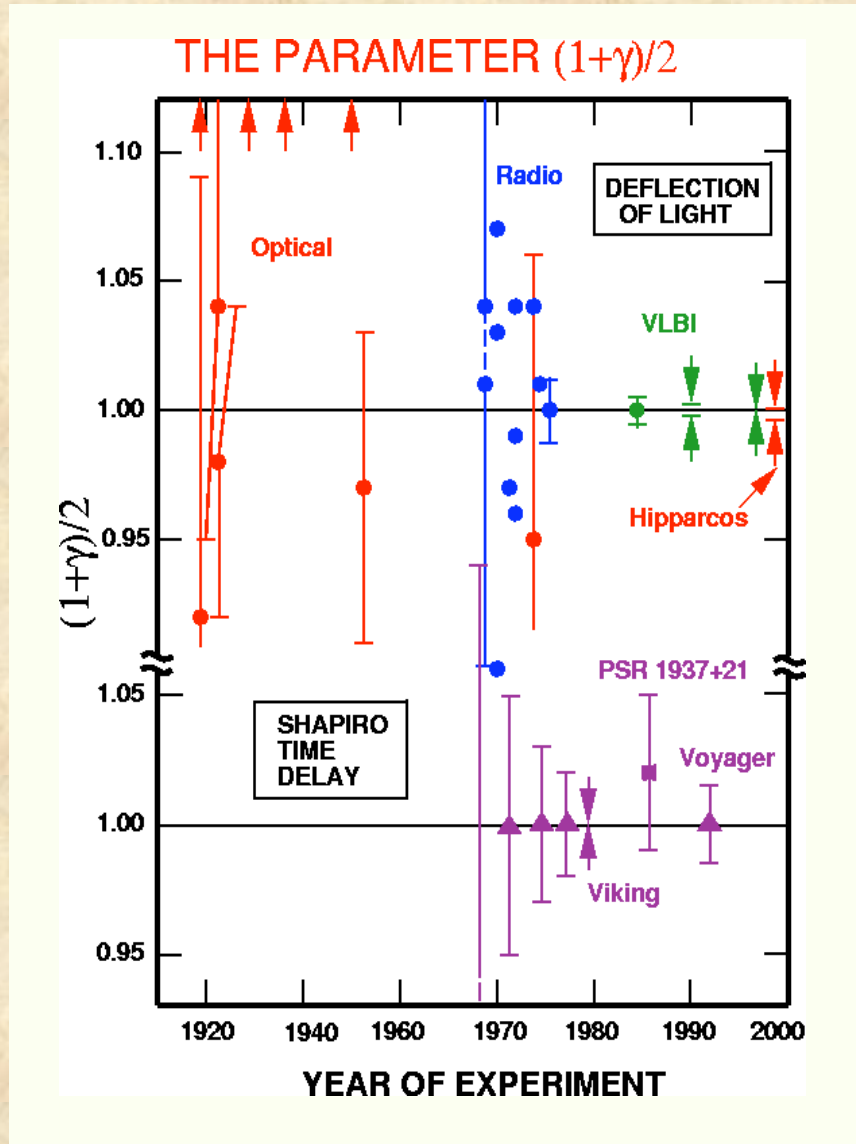
## GENERAL RELATIVITY HAS TWO INGREDIENTS

- The Equivalence Principle Has Been Tested to a Very High Degree



Will 2001

- The Einstein Field Equations has been tested to  $\sim 10^{-4}$

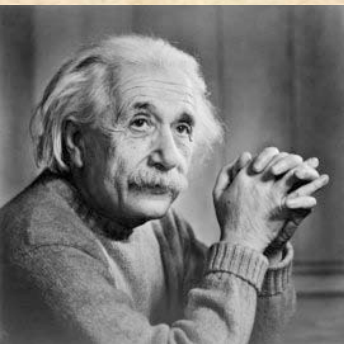


Will 2001

# What measures the strength of the gravitational field?



No scale in the theory! No field is either weak or strong!



Matter Gravity

	Weak Field	Strong Field
Potential $\epsilon \sim \frac{GM}{Rc^2}$	$\ll 1$	$\cong 1$
Velocity, $u/c$	$\ll 1$	$\cong 1$

## Extending Einstein's Equation

⇒ Einstein's equation

derived from the Hilbert action:

$$S = \frac{1}{16\pi G} \int d^4x \sqrt{-g} (R - 2\Lambda)$$

Ricci curvature

more spacetime dimensions

higher-order ( $R^2$ ) Gravity:

$$\sqrt{-g} (R + aR^2 + \dots)$$

or Gravity with additional fields, e.g., a scalar  $\phi$

$$\sqrt{-g} [R - \omega g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi - V(\phi)]$$

Cosmological constant

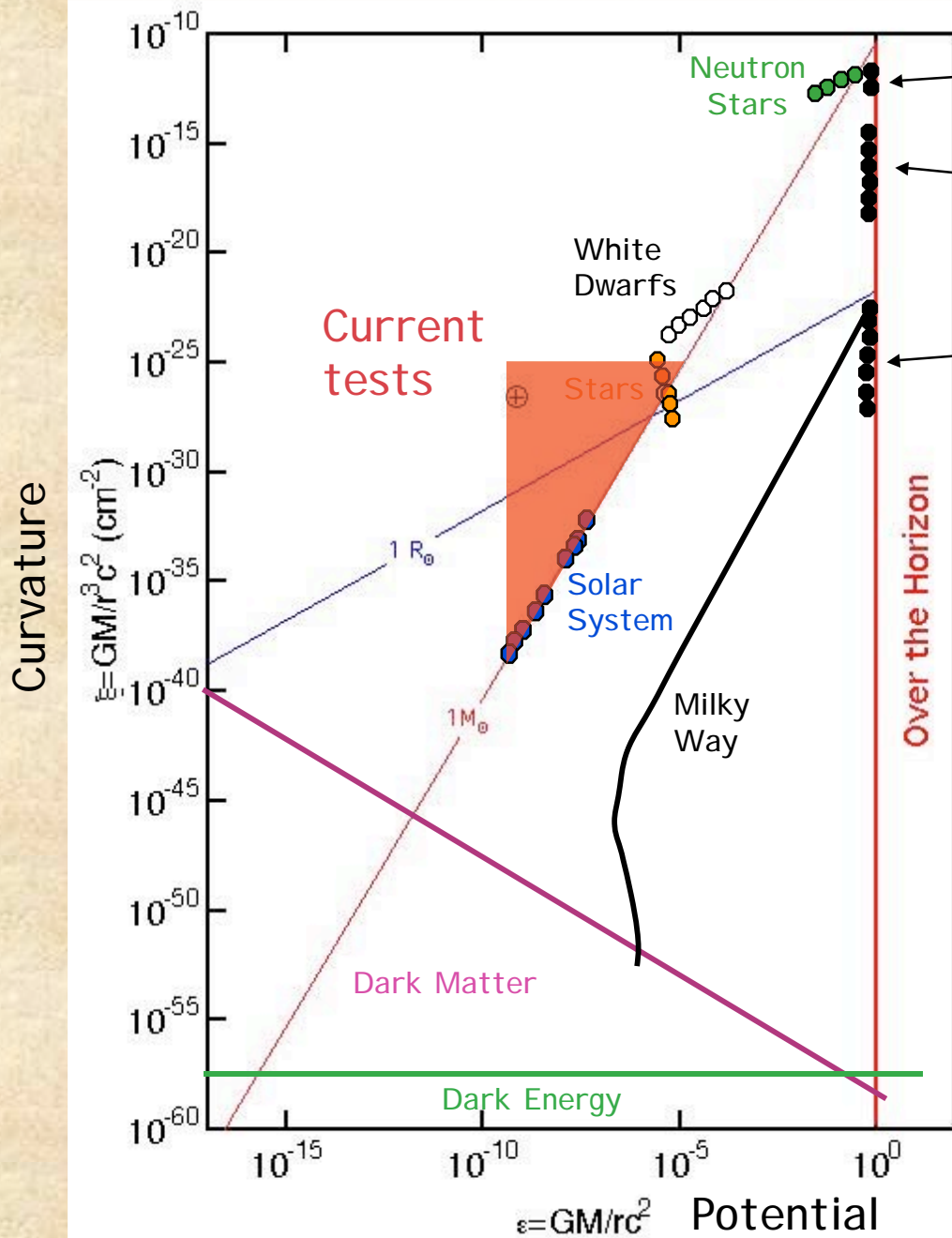
## What measures the strength of the gravitational field?

In GR, the strength of the gravitational field is measured by  
The gravitational potential

$$\varepsilon \equiv \frac{GM}{rc^2}$$

In a general Lagrangian theory with an additional scale,  
the strength of the field will be measured by the curvature

$$\xi \equiv \frac{GM}{r^3 c^2}$$



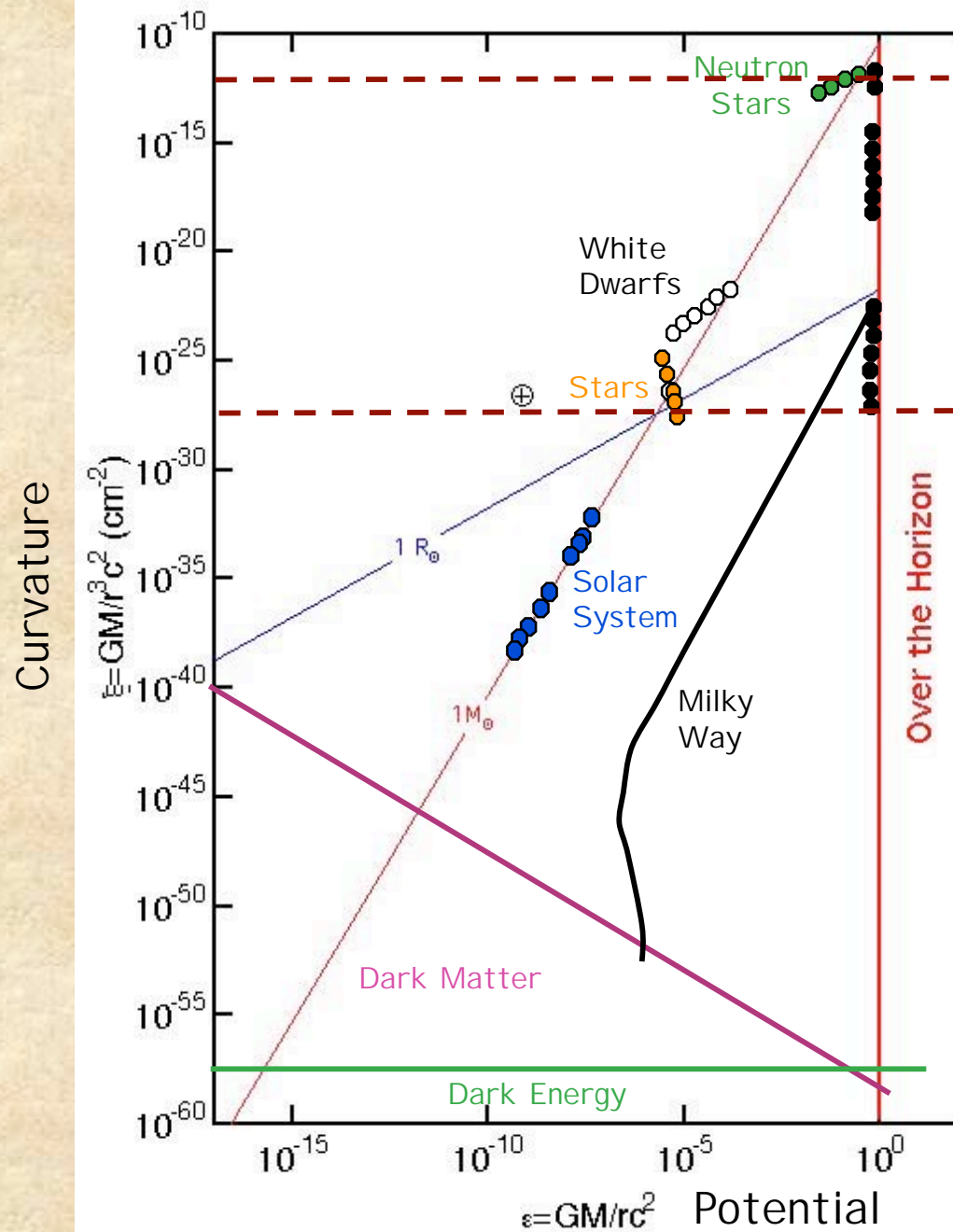
X-ray Binaries

Intermediate Mass Black-Holes

Active Galactic Nuclei

## Gravitational Fields In Astrophysical Systems

Psaltis 2008



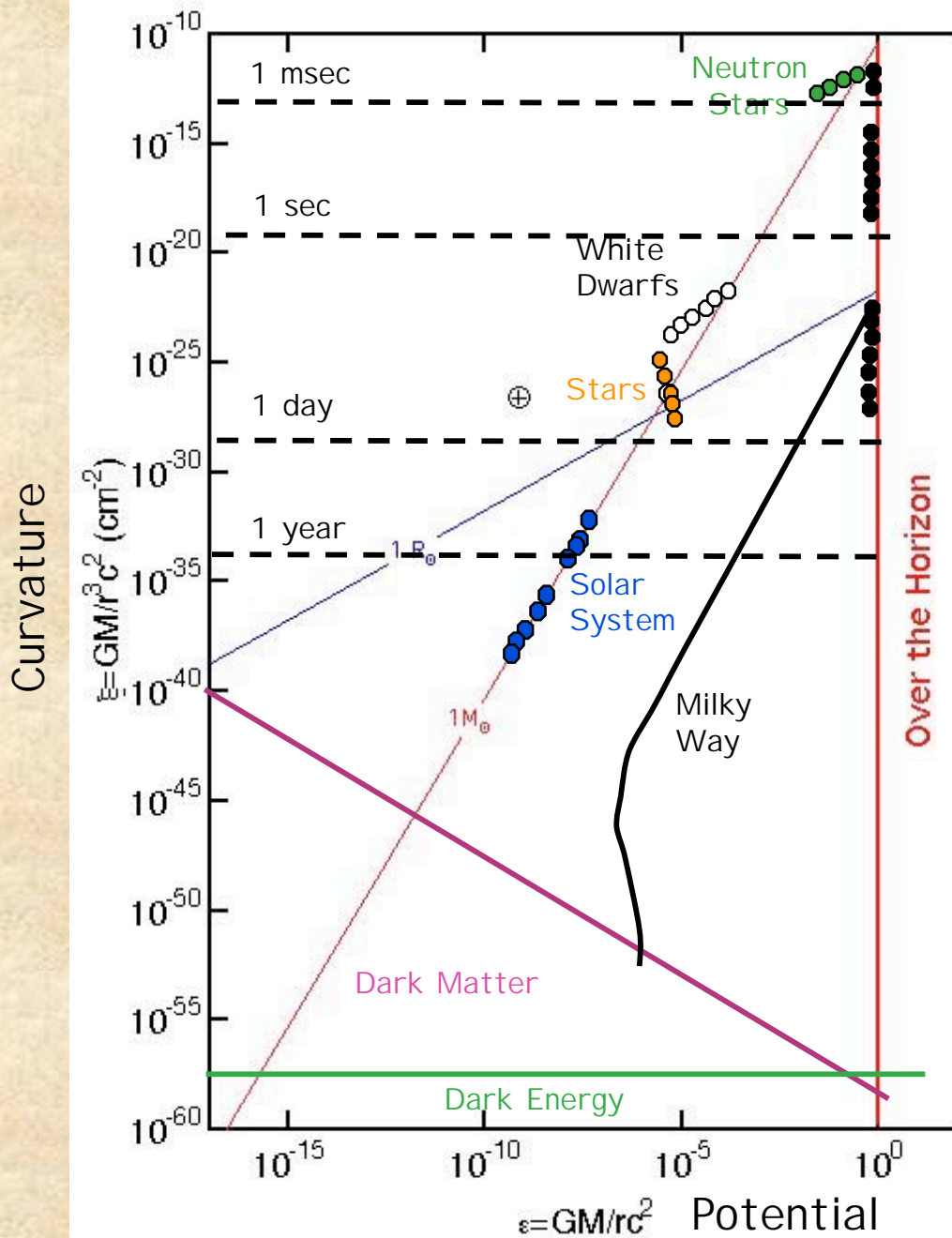
EW Baryogenesis

Nucleosynthesis

Gravitational Fields  
In **Cosmology**

Psaltis 2008

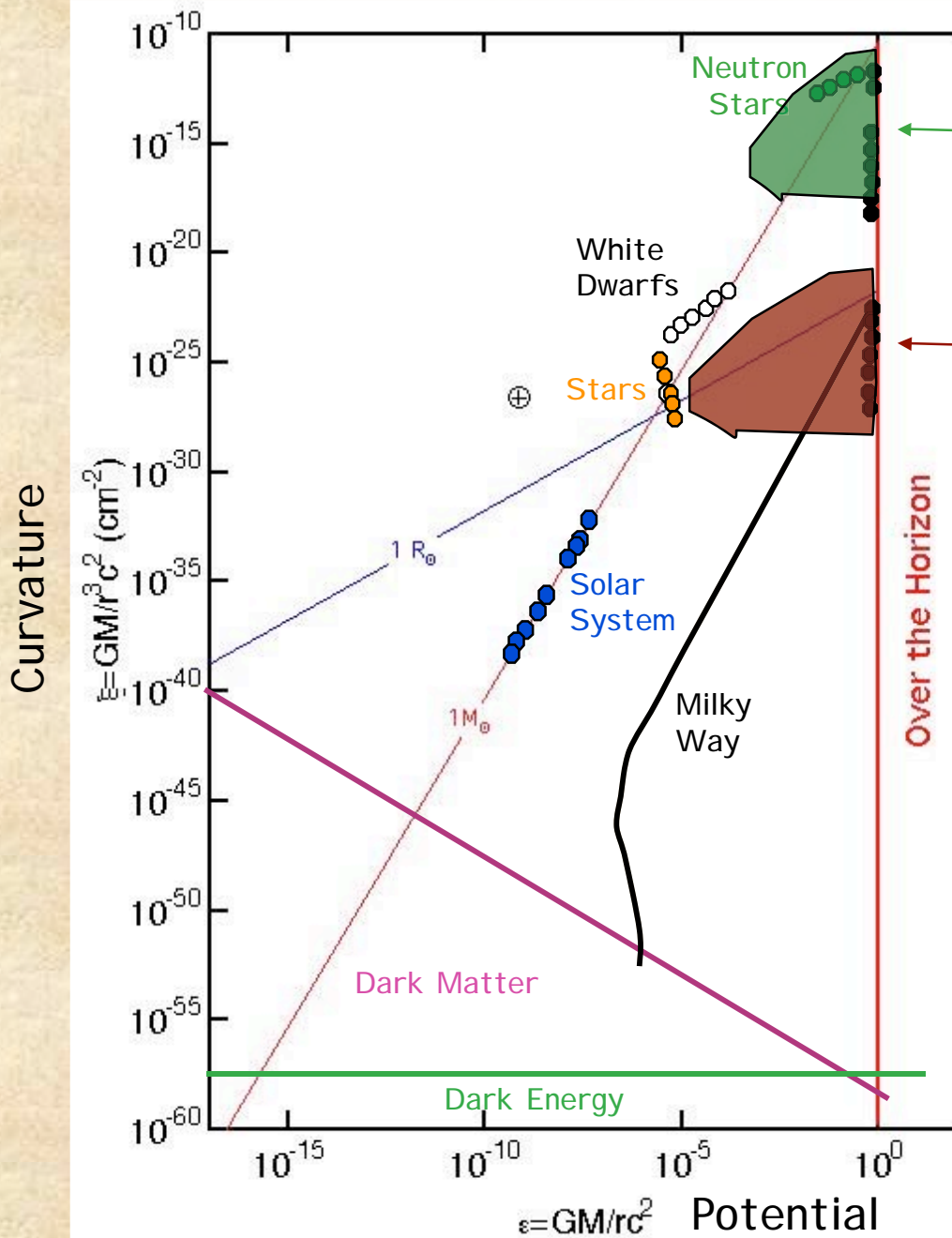




Fast X-ray timing!  
(AXTAR & XEUS)

How to Probe the  
Strong Gravitational Fields

Psaltis 2008



Fast X-ray timing!  
(AXTAR & XEUS)

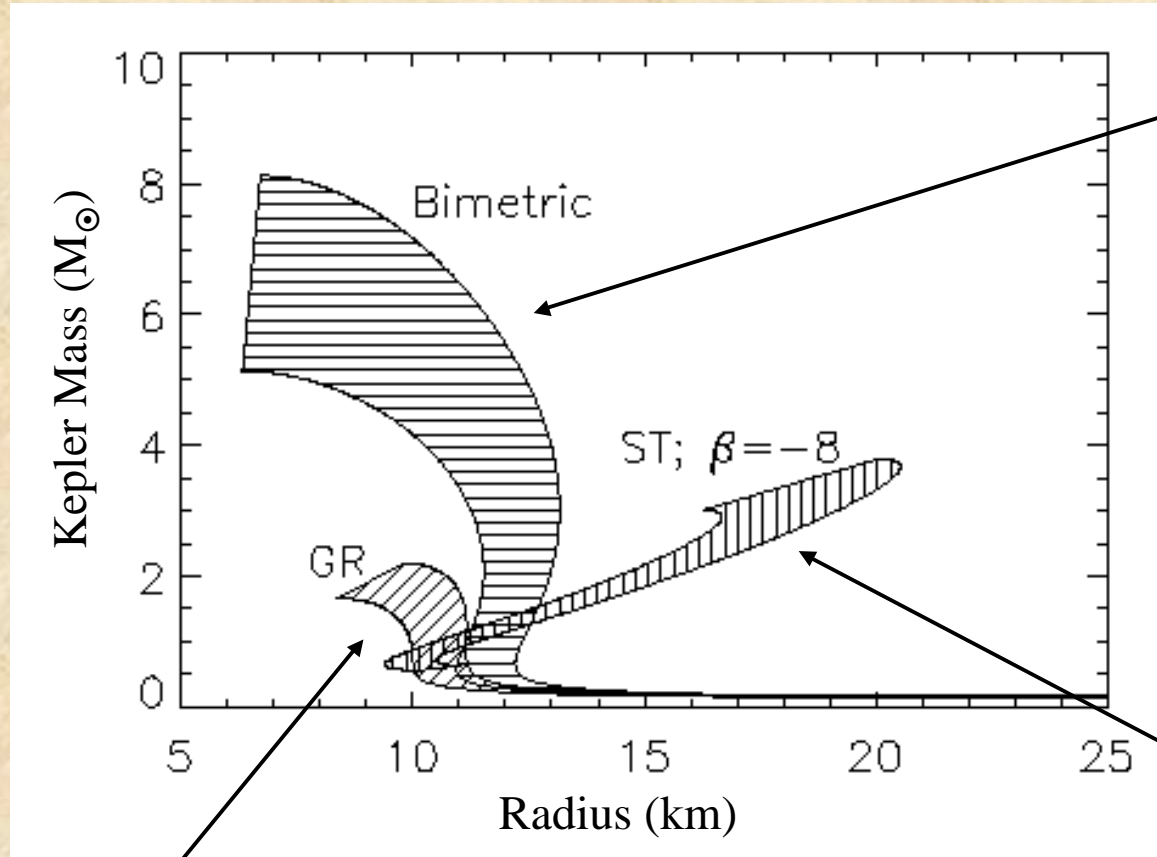
High-Frequency  
Gravity Waves  
(e.g., LIGO, GEO600)

How to Probe the  
Strong Gravitational Fields

Psaltis 2008

## NEUTRON STARS IN ALTERNATIVE GRAVITY THEORIES

DeDeo & Psaltis 2003

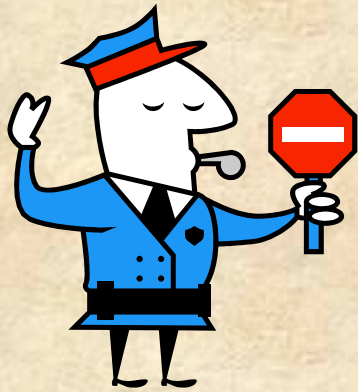


Rosen's Theory  
(prior geometry)

Scalar-Tensor  
(dynamical)

General Relativity

- All theories consistent with solar system tests!
- Uncertainty due to gravity larger than EOS!



We have to be very careful when playing with Einstein's equation...

(*aka* a lesson learned from Cosmology)



Cosmic acceleration can be produced by

$$S = \frac{1}{16\pi G} \int d^4x \sqrt{-g} \left( R - \frac{\mu^2}{R} \right)$$

Carroll et al. 2004

But:

Universe unstable to small perturbations!

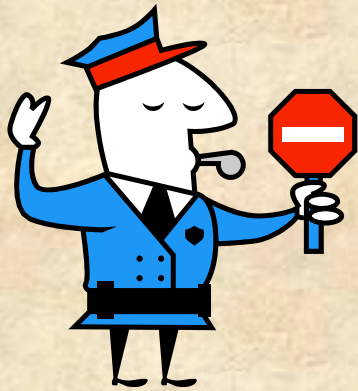
Dolgov & Kawasaki 2003; Sawicki & Hu 2007

Post-Newtonian corrections do not depend on  $\mu$ !! ( $\gamma = 1/2$ )

Chiba 2003; Ericcek et al 2006

Stars are unstable to small perturbations!!!

Seifert & Wald 2007; Seifert 2007



Cosmic acceleration can be produced by

$$S = \frac{1}{16\pi G} \int d^4x \sqrt{-g} \left( R - \frac{\mu^2}{R} \right)$$

Carroll et al. 2004

Solution to these problems requires

- fine tuning
- a chameleon field
- perturbative localization

DeDeo & Psaltis 2008, PRL, submitted

## Scalar-Tensor Gravity and Neutron Stars

(Damour & Esposito-Farese 1993; DeDeo & Psaltis 2003, 2006)

$$S = \frac{1}{16\pi G_*} \int d^4x \sqrt{-\tilde{g}} \left[ \tilde{R} - 2\tilde{g}_{\mu\nu} \partial_\mu \phi \partial_\nu \phi \right] + S_m \left[ \psi, A^2(\phi) \tilde{g}_{\mu\nu} \right]$$

and parametrize the coupling function:

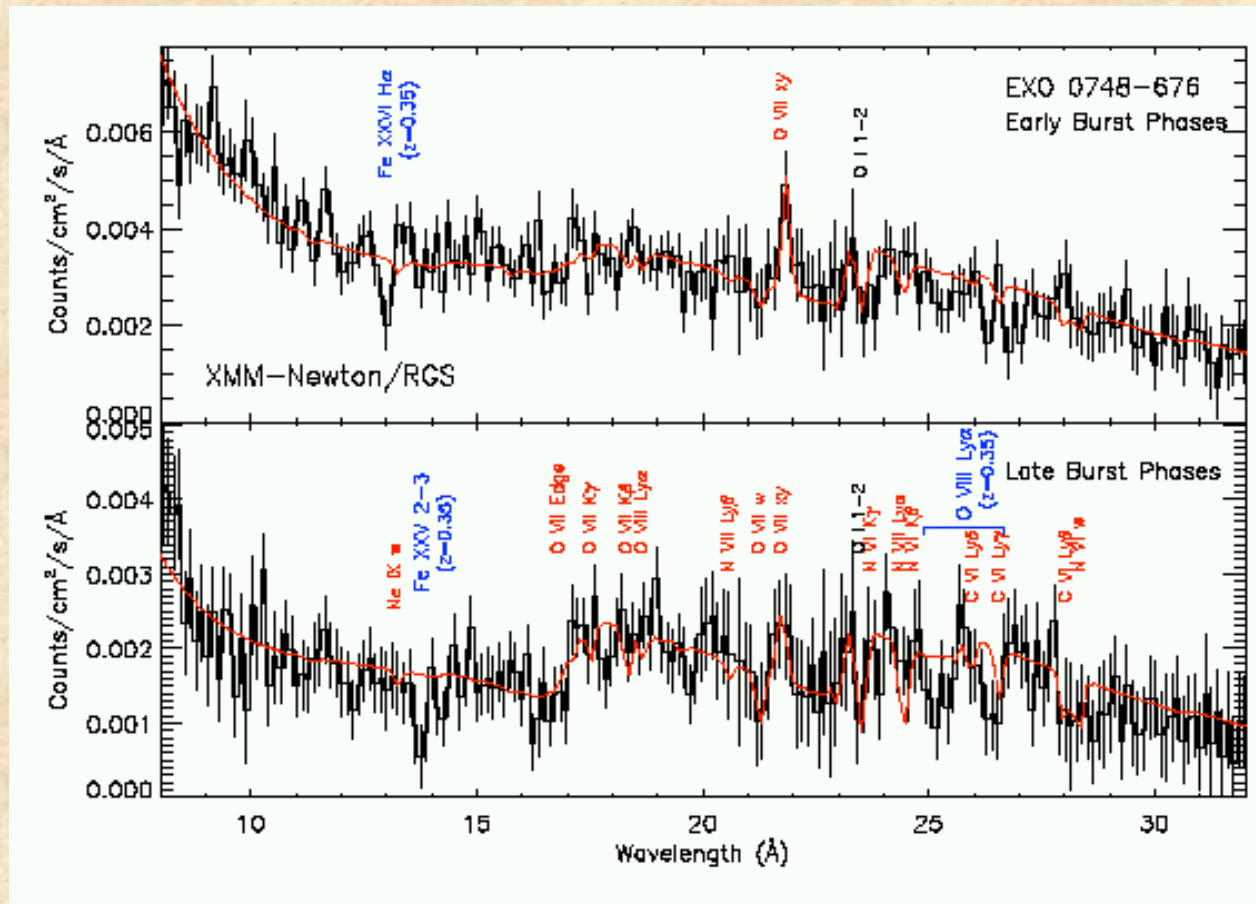
$$A(\phi) = \alpha_0 (\phi - \phi_0) + \frac{1}{2} \beta_0 (\phi - \phi_0)^2 + \dots$$

weak-field tests constrain  $\alpha_0$  (Cassini set  $\alpha_0 < 10^{-4}$ )

you need strong-field tests to constrain  $\beta_0$

# GRAVITATIONALLY REDSHIFTED LINES

Redshift for EXO 0748-676:  $\delta\lambda/\lambda=0.35$

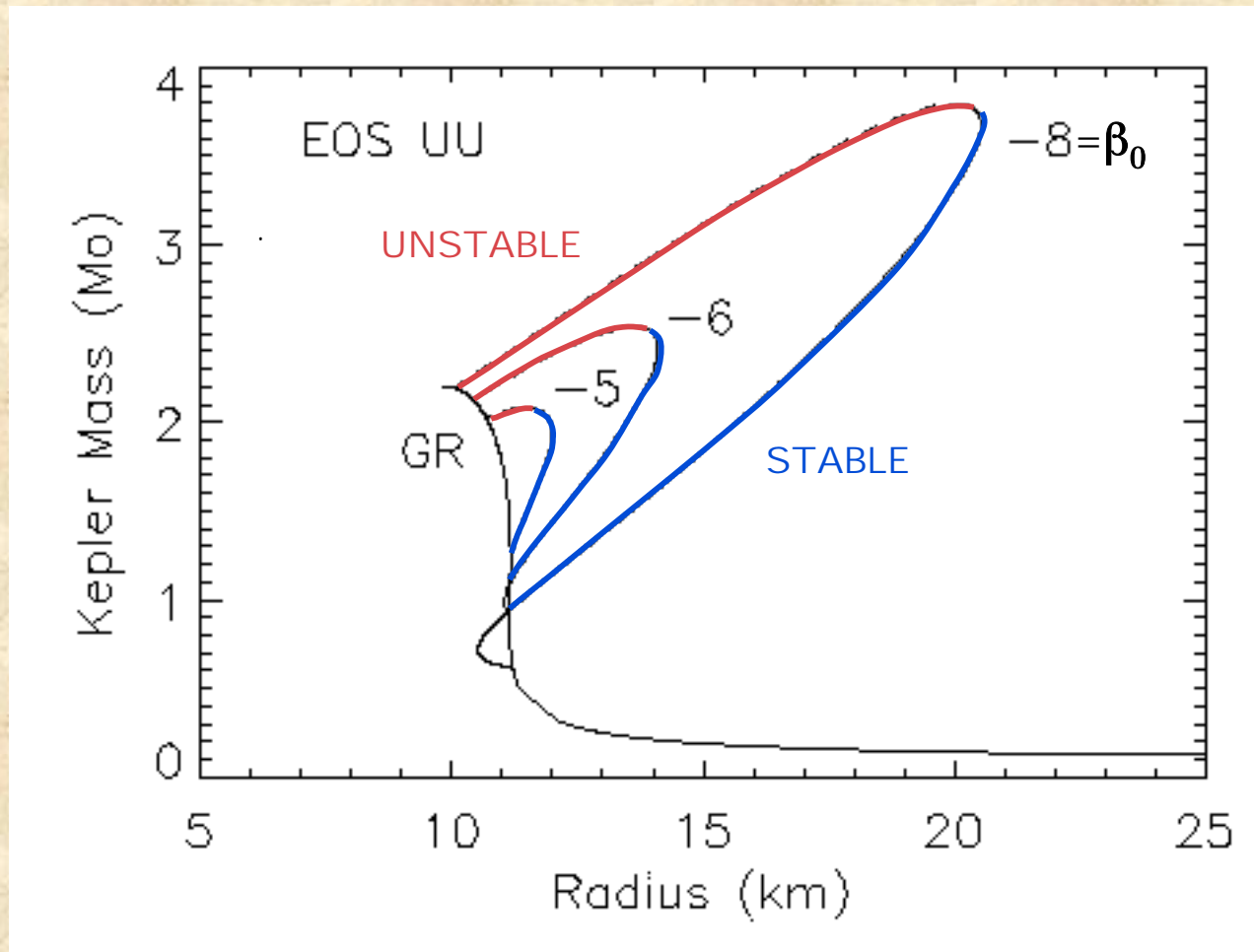


Cottam et al. 2002

**Bonus:** Neutron Stars are Spherically Symmetric  
(when slowly rotating)



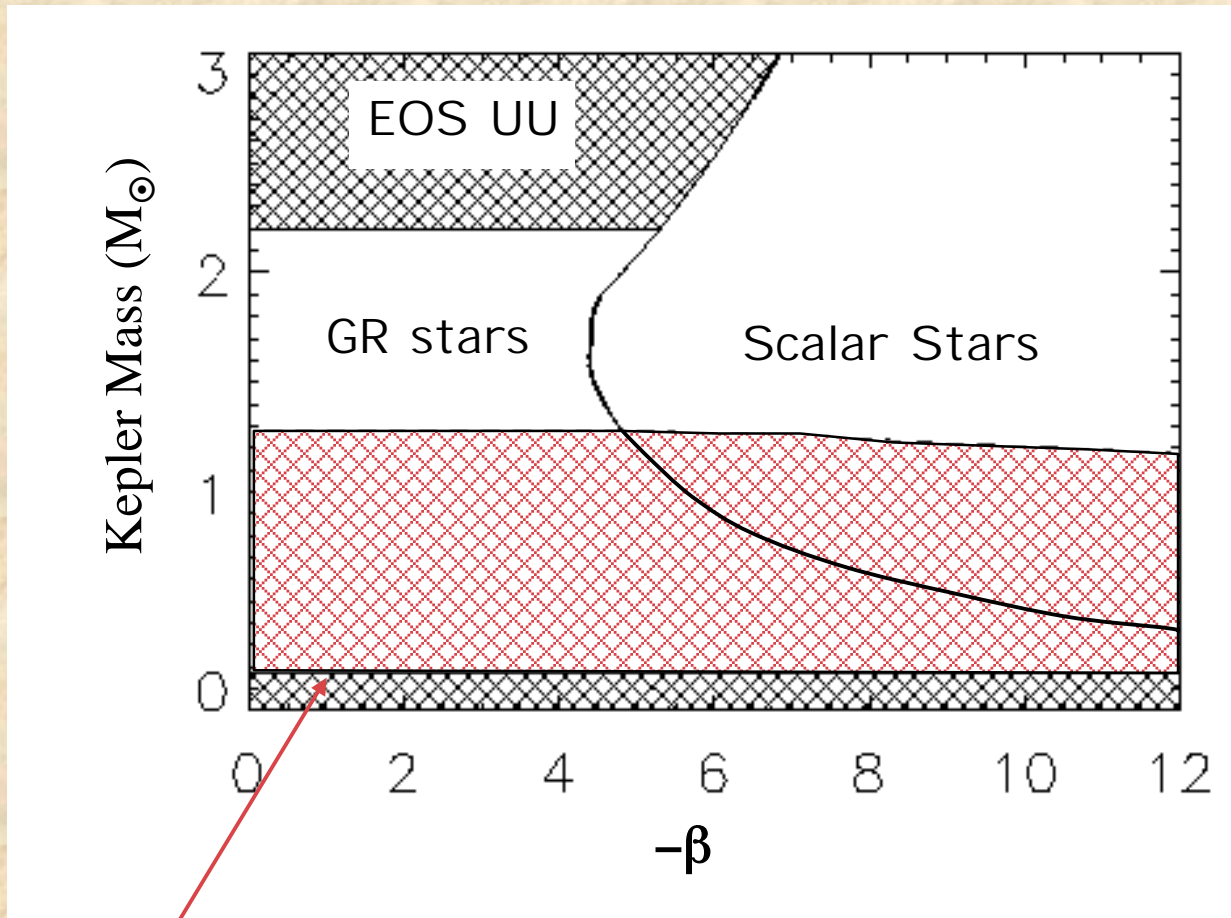
# NEUTRON STARS IN SCALAR-TENSOR GRAVITY



DeDeo & Psaltis 2003

Scalar Stars can become Large and Massive

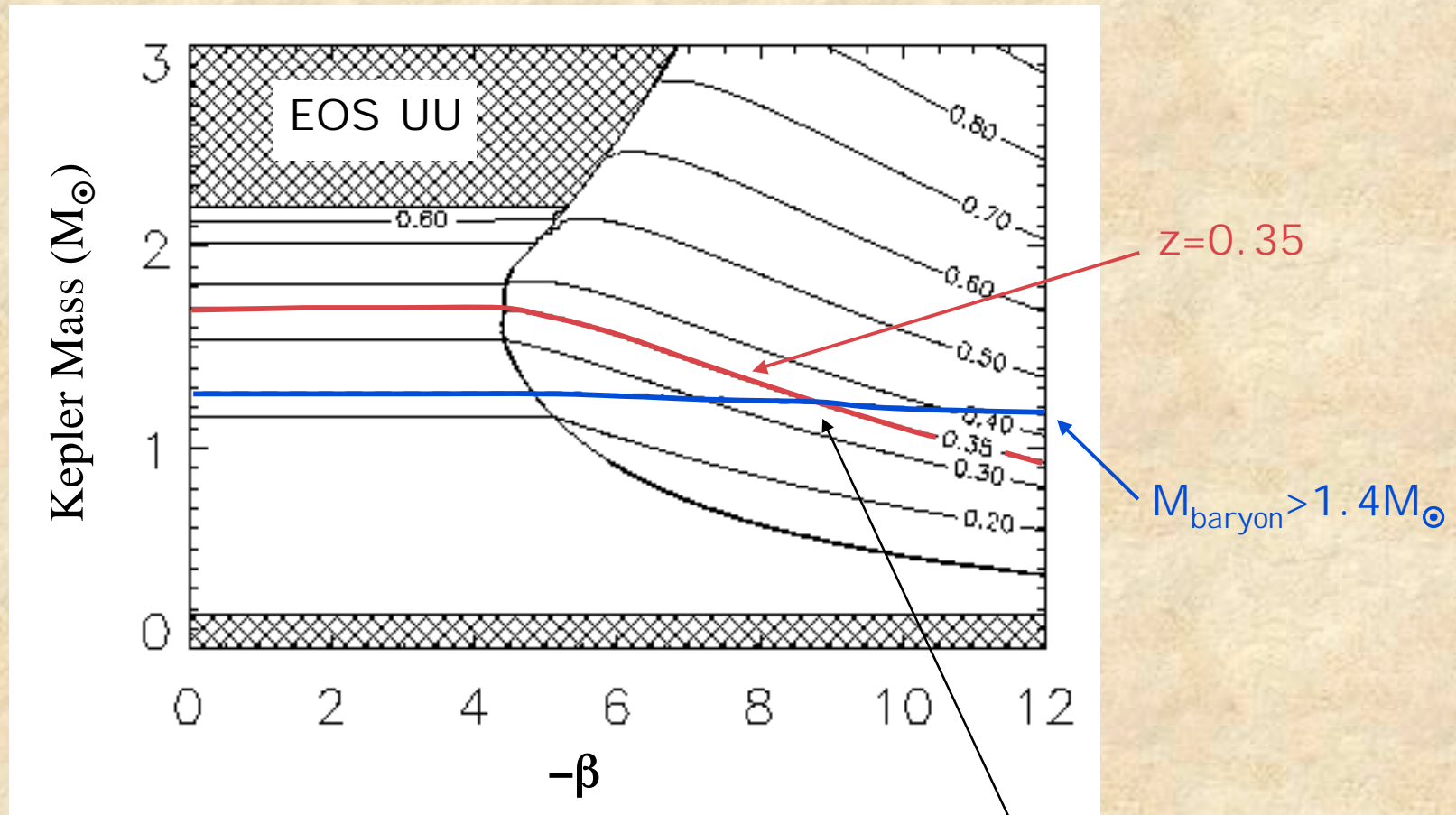
# NEUTRON STARS IN SCALAR-TENSOR GRAVITY II



DeDeo & Psaltis 2003

Baryonic Mass <  $1.4M_{\odot}$

## LIMITS FROM GRAVITATIONAL REDSHIFTS

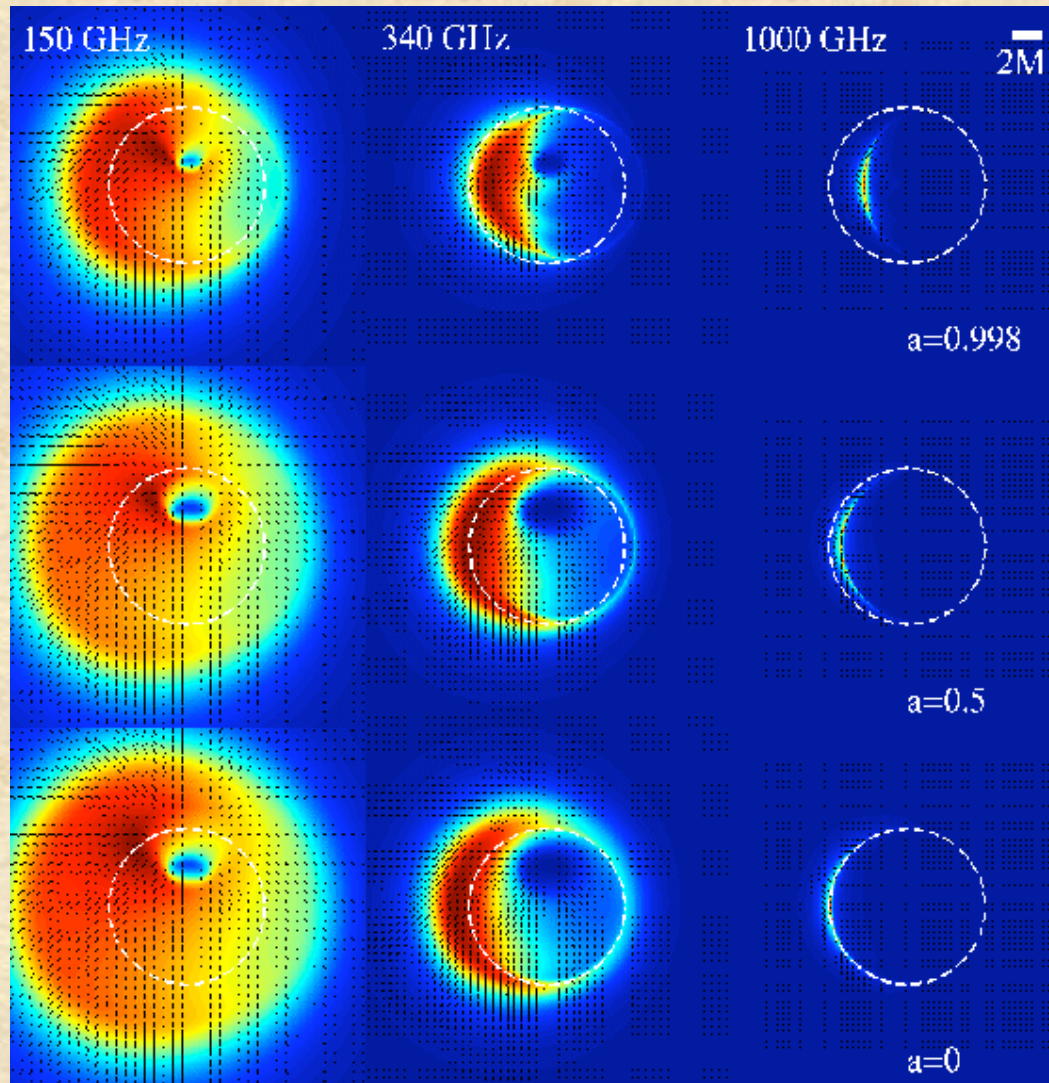


DeDeo & Psaltis 2003

Limit:  $-\beta < 9$

If the mass of EXO 0748-676 is measured, limits will become tighter

# What can we learn about strong-field GR with Black Holes?



Broderick & Loeb 2006

## Scalar-Tensor black holes are identical to GR ones!

Thorne & Dykla 1971; Hawking 1974; Bekenstein 1974; Sheel et al. 1995

Let's add:

Psaltis, Perrodin, Dienes, & Mocioiu 2008, PRL, 100, 091101

a dynamical vector field

all  $R^2$  terms

any function of  $R$

... in the Palatini formalism

**Always get Kerr Black Holes!!!**

## The Good News

We have a parameter-free solution to an astrophysical problem!

If experiments do not confirm it:

- Strong Violation of Equivalence Principle!

- Large extra dimensions!!

Empanan et al. 2002

- Massive Gravitons!!!

Berti, Buonanno, Will 2005

- Non-local physics!!!!

e.g., Simon 1990, Adams et al. 2006

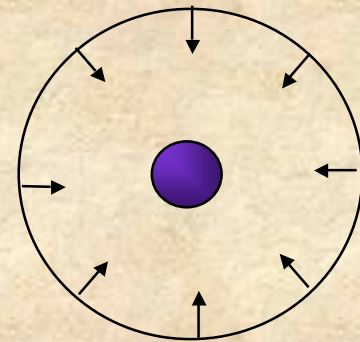
## Large extra dimensions?

Gauss' law tells us that we live in a 4D world!

$$g \sim \frac{GM}{r^2}$$

The exponent "2" is mostly geometric

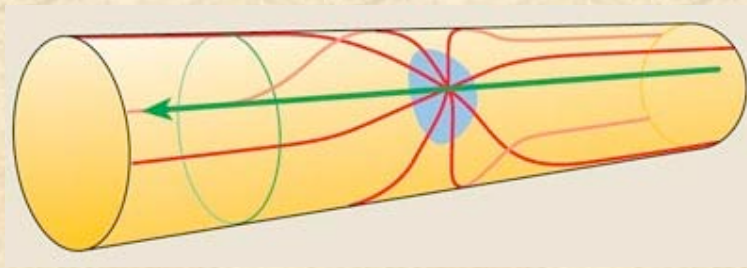
$$\int \vec{g} \cdot d\vec{S} = 4\pi r^2 g = 4\pi GM$$



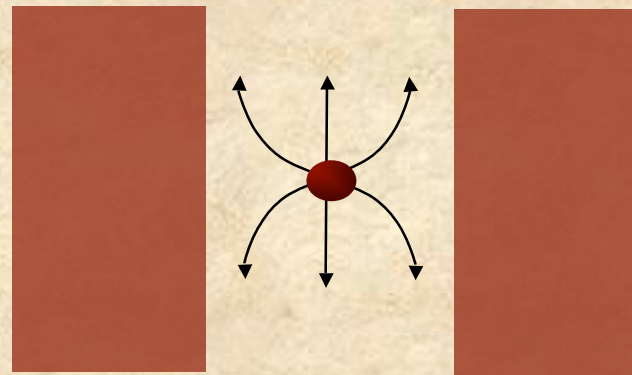
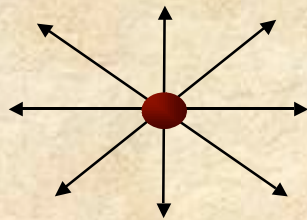
and is equal to the (number of space dimensions) - 1!

## How do we get around Gauss' law?

(I) Compactify extra dimensions (ADD)



(II) "Fill" bulk with a "cosmological constant" (RS2)

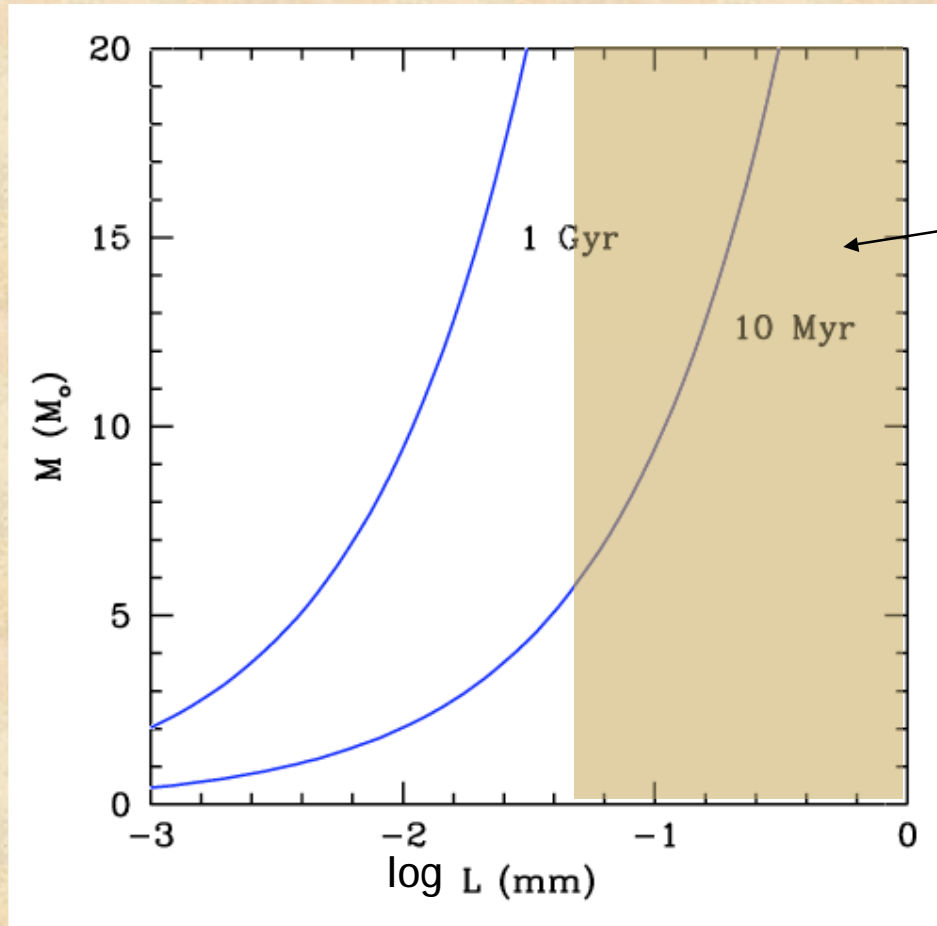




## Large Extra Dimensions?

In a universe with large 'RS' extra dimensions, black holes evaporate FAST due to emission of gravitons in the bulk

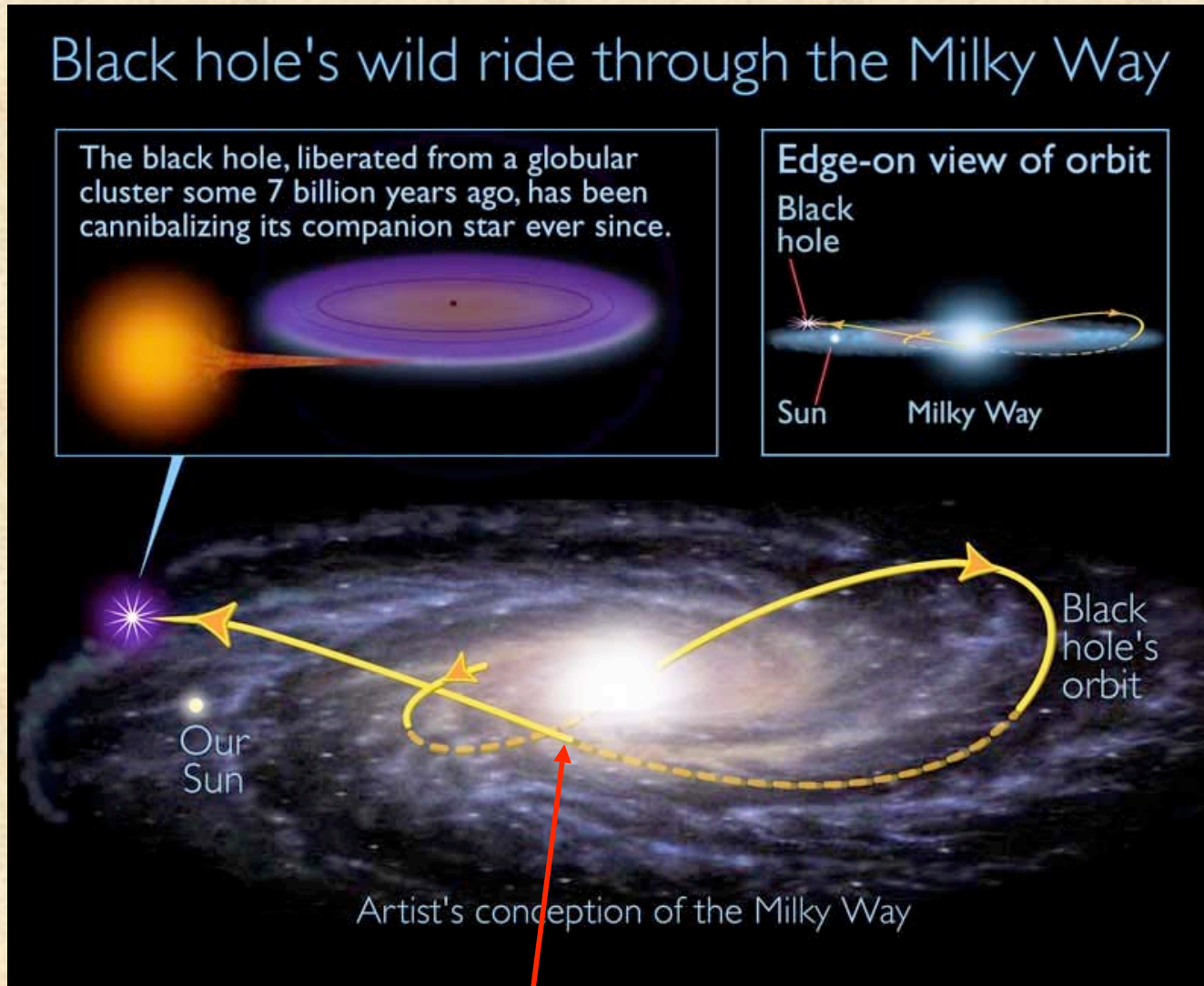
EMPARAN et al. 2002



Tabletop experiments:

$$L < 0.05 \text{ mm}$$

# The wild ride of XTE J1118+480 through the galaxy

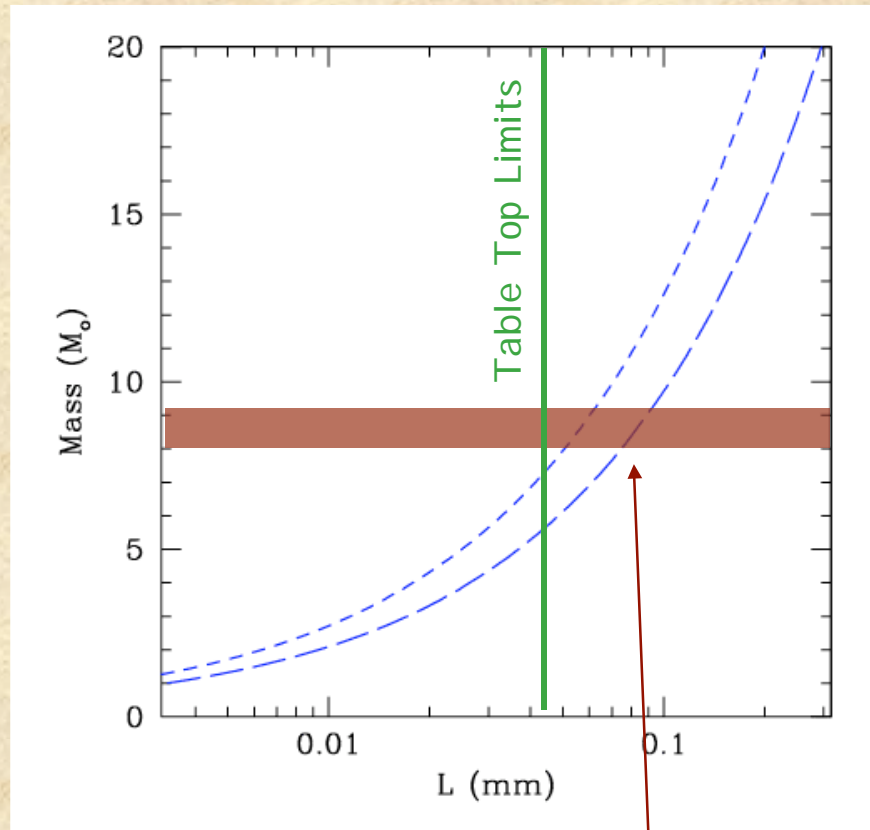
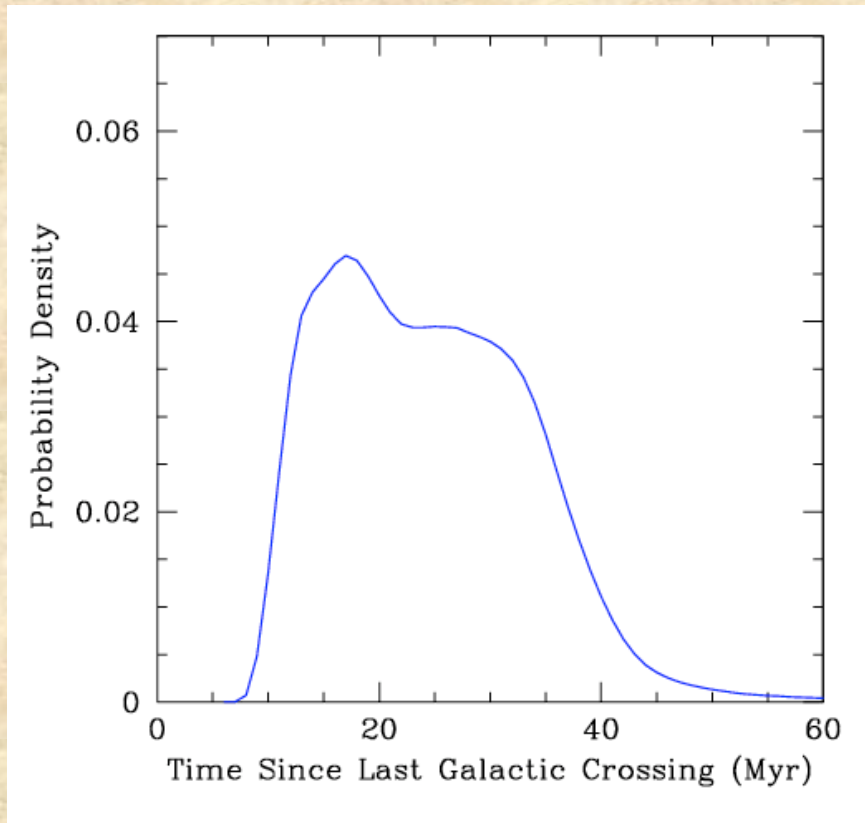


Mirabel et al. 2001

When did this happen?

# Constraining the AdS Curvature of Extra Dimensions I

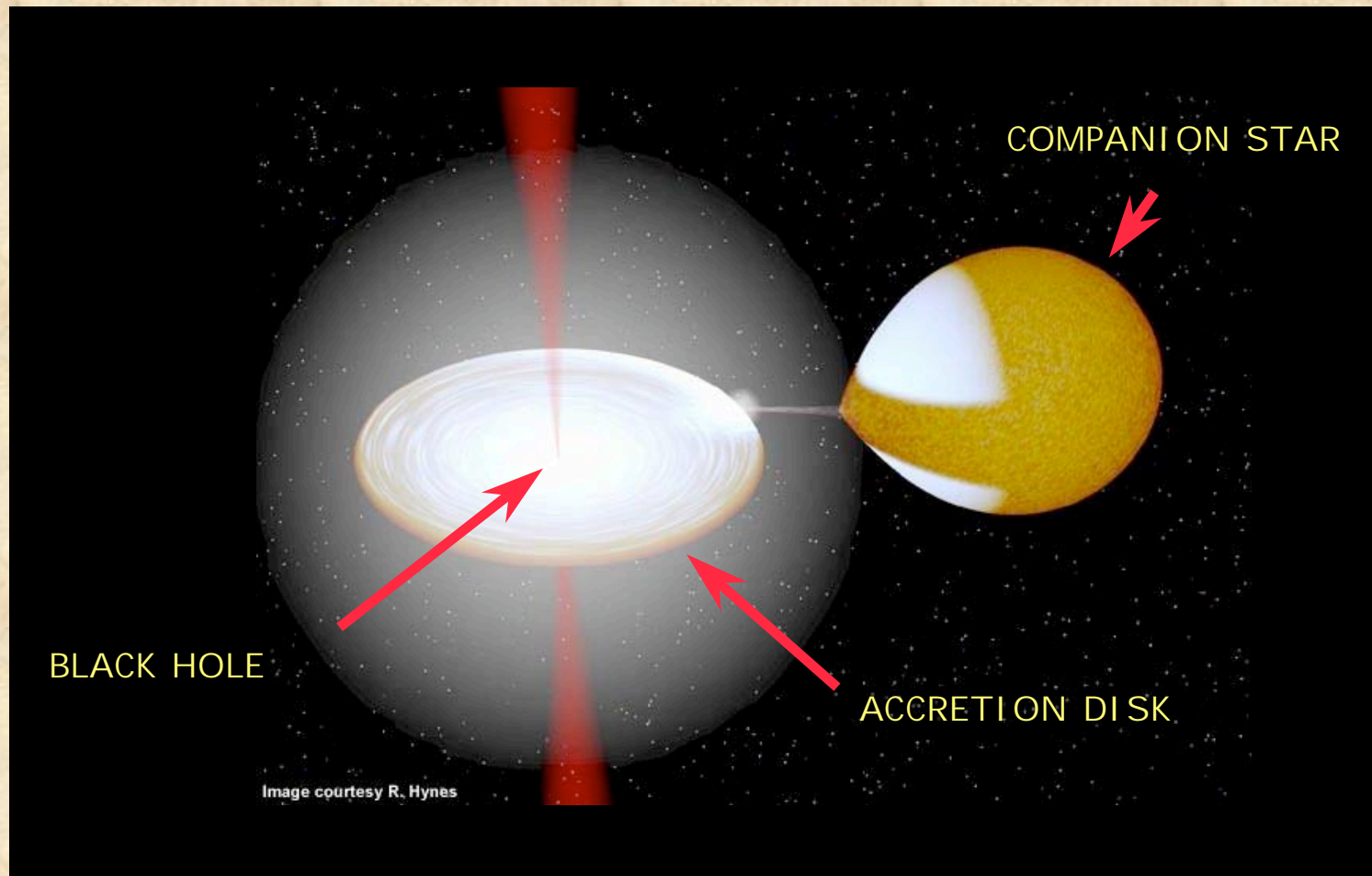
Psaltis 2007, PRL, 98, 1101



Astrophysical Limit:  $L < 0.08$  mm

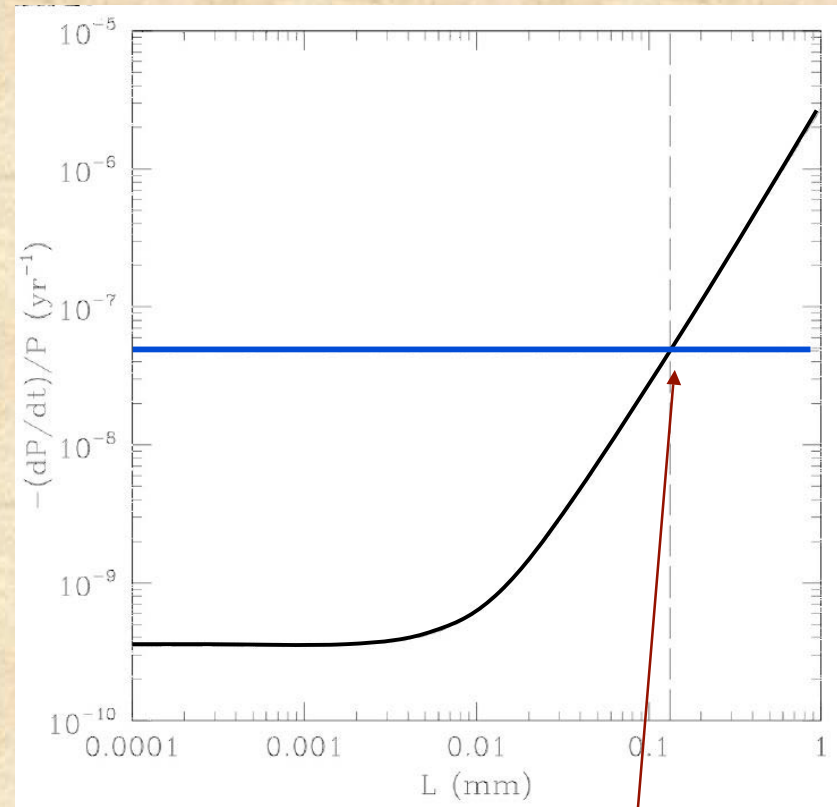
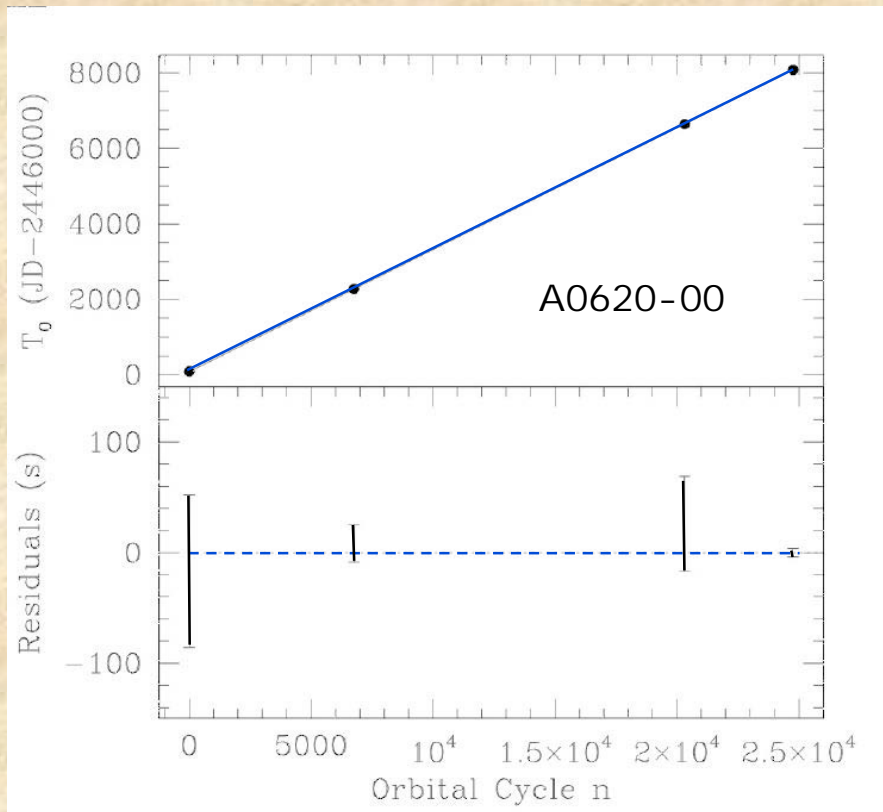
# Orbital Evolution of Black-Hole Binaries

Johannsen, Psaltis, McClintock 2008



# Constraining the AdS Curvature of Extra Dimensions I I

Johannsen, Psaltis, McClintock 2008



Astrophysical Limit:  $L < 0.15$  mm

## CONCLUSIONS

- (I) Gravity in the Strong-Field Regime has not been tested
- (II) Different characteristics of Neutron Stars and Black Holes are significantly affected by gravity
  - ⇒ a great laboratory to perform gravitational tests
- (III) We are in need of a framework for gravity tests beyond the post-Newtonian limit!
- (IV) Current observations provide stringent constraints on
  - ⇒ scalar-tensor gravities
  - ⇒ braneworld gravity theories