



**CORRIGENDUM ON THE PAPER: 'LOWER BOUNDS FOR THE INFIMUM OF
THE SPECTRUM OF THE SCHRÖDINGER OPERATOR IN \mathbb{R}^N AND THE
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E.J.M. VELING

DELFT UNIVERSITY OF TECHNOLOGY
FACULTY OF CIVIL ENGINEERING AND GEOSCIENCES
SECTION FOR HYDROLOGY AND ECOLOGY
P.O. Box 5048, NL-2600 GA DELFT
THE NETHERLANDS.
Ed.Veling@CiTG.TUdelft.nl

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ABSTRACT. This paper is a corrigendum on a paper published in an earlier volume of JIPAM, 'Lower Bounds for the Infimum of the Spectrum of the Schrödinger Operator in \mathbb{R}^N and the Sobolev Inequalities' published in JIPAM, vol. 3, no. 4. (2002), Article 63. It concerns of a number of misprints.

Key words and phrases: Optimal lower bound, infimum spectrum Schrödinger operator, Sobolev inequality.

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1. RESULTS

The following list of misprints have been brought to the attention of the author by the review in Mathematical Reviews #1923362 by Jan Kříž. It appeared that these misprints had crept in during the process of text-editing of an earlier concept.

- (1) Page 2, formula (1.4) (definition of the form domain $Q(h)$):

$$Q(h) = H^1(\mathbb{R}^N) \cap \{u \mid u \in L^2(\mathbb{R}^N), \quad q_+^{1/2} \in L^2(\mathbb{R}^N)\}.$$

to be replaced by [see second condition]

$$Q(h) = H^1(\mathbb{R}^N) \cap \{u \mid u \in L^2(\mathbb{R}^N), \quad q_+^{1/2}u \in L^2(\mathbb{R}^N)\}.$$

- (2) Page 3, brackets between formulas (1.12) and (1.13): the line with

$$(P = 1/\theta, Q = 1/(1 - \theta), a = \eta \|\nabla w\|_2^{2\theta}, b = \|w\|_2^{2\theta}/\eta).$$

to be replaced by [see exponent in expression for b]

$$(P = 1/\theta, Q = 1/(1 - \theta), a = \eta \|\nabla w\|_2^{2\theta}, b = \|w\|_2^{2(1-\theta)}/\eta).$$

(3) Page 4, formula (1.22), integral in the numerator:

$$l(N, \theta) = \inf_{q_- \in L^p(\mathbb{R}^N)} \inf_{u \in H^1(\mathbb{R}^N)} \frac{\|\nabla u\|_2^2 + \int_{\mathbb{R}^N} q |u|_2^2 dx}{\|u\|_2^2} \|q_-\|_p^{-1/(1-\theta)}.$$

to be replaced by [see $|u|^2$ in integrand in integral in numerator]

$$l(N, \theta) = \inf_{q_- \in L^p(\mathbb{R}^N)} \inf_{u \in H^1(\mathbb{R}^N)} \frac{\|\nabla u\|_2^2 + \int_{\mathbb{R}^N} q |u|^2 dx}{\|u\|_2^2} \|q_-\|_p^{-1/(1-\theta)}.$$

(4) Page 5, formulas (1.28) and (1.29), integrals (0,infinity) in the numerators:

$$\inf_{q_- \in L^p(\mathbb{R}^+)} \inf_{u \in \mathcal{D}(T_0)} \frac{\|u'\|_2^2 + \int_0^\infty q |u|_2^2 dx}{\|u\|_2^2} \|q_-\|_p^{-2p/(2p-1)} = l(1, 1/(2p)),$$

$$\inf_{q_- \in L^p(\mathbb{R}^+)} \inf_{u \in \mathcal{D}(T_{\pi/2})} \frac{\|u'\|_2^2 + \int_0^\infty q |u|_2^2 dx}{\|u\|_2^2} \|q_-\|_p^{-2p/(2p-1)} = 2^{2/(2p-1)} l(1, 1/(2p)).$$

to be replaced by [see $|u|^2$ in integrand integral numerator], respectively

$$\inf_{q_- \in L^p(\mathbb{R}^+)} \inf_{u \in \mathcal{D}(T_0)} \frac{\|u'\|_2^2 + \int_0^\infty q |u|^2 dx}{\|u\|_2^2} \|q_-\|_p^{-2p/(2p-1)} = l(1, 1/(2p)),$$

$$\inf_{q_- \in L^p(\mathbb{R}^+)} \inf_{u \in \mathcal{D}(T_{\pi/2})} \frac{\|u'\|_2^2 + \int_0^\infty q |u|^2 dx}{\|u\|_2^2} \|q_-\|_p^{-2p/(2p-1)} = 2^{2/(2p-1)} l(1, 1/(2p)).$$

(5) Page 7, Lemma 2.1: "defined in (6)" should be replaced by "defined in (1.6)".

(6) Page 9, formula (2.15):

$$h(u, u) = -b^Q/Q = -(1 - \theta)\theta^{\theta/(1-\theta)} \lambda_{N,\theta}^{-2/(1-\theta)} \|q_-\|_p^{1/(1-\theta)} \|u\|_2^2,$$

to be replaced by [first equality sign to be replaced by inequality sign]

$$h(u, u) \geq -b^Q/Q = -(1 - \theta)\theta^{\theta/(1-\theta)} \lambda_{N,\theta}^{-2/(1-\theta)} \|q_-\|_p^{1/(1-\theta)} \|u\|_2^2,$$

(7) Page 10, formula (2.25), integral in the numerator:

$$\frac{\|u'_j\|_2^2 + \int_{-\infty}^\infty q |u_j|_2^2 dx}{\|u_j\|_2^2} \|q_j\|_1^{-2} = -(1 + 1/j)^2/4 > -1/4 = l(1, 1/2).$$

to be replaced by [see q_j and $|u_j|^2$ in integrand integral numerator]

$$\frac{\|u'_j\|_2^2 + \int_{-\infty}^\infty q_j |u_j|^2 dx}{\|u_j\|_2^2} \|q_j\|_1^{-2} = -(1 + 1/j)^2/4 > -1/4 = l(1, 1/2).$$

Moreover, corrections have to be made in the following lines.

(1) Page 1, Abstract, line 4: change

" $\Lambda_{N,\theta}(\nu) = \|\nabla v\|_2^\theta \|v\|_2^{1-\theta} \|v\|_r^{-1}$, with ν element of the Sobolev space $H^1(\mathbb{R}^N)$ ", into

" $\Lambda_{N,\theta}(v) = \|\nabla v\|_2^\theta \|v\|_2^{1-\theta} \|v\|_r^{-1}$, with v element of the Sobolev space $H^1(\mathbb{R}^N)$ ".

(2) Page 1, line -2: change " $q = q_+ + q_-$ " into " $q = q_+ - q_-$ ".

(3) Page 6, line 12: change " $l(3, 3/4) = -1.750180_{10^{-4}}$ " into " $l(3, 3/4) \simeq -1.750180_{10^{-4}}$ ".

(4) Page 8: label (2.4) refers the expression, one line higher; label (2.5) refers to the expression two lines higher.

(5) Page 9: change formula (2.16) " $q = q_-$ " into " $q = -q_-$ ".

(6) Page 11, line 9: change "side of (31)" into "side of (1.31)".